



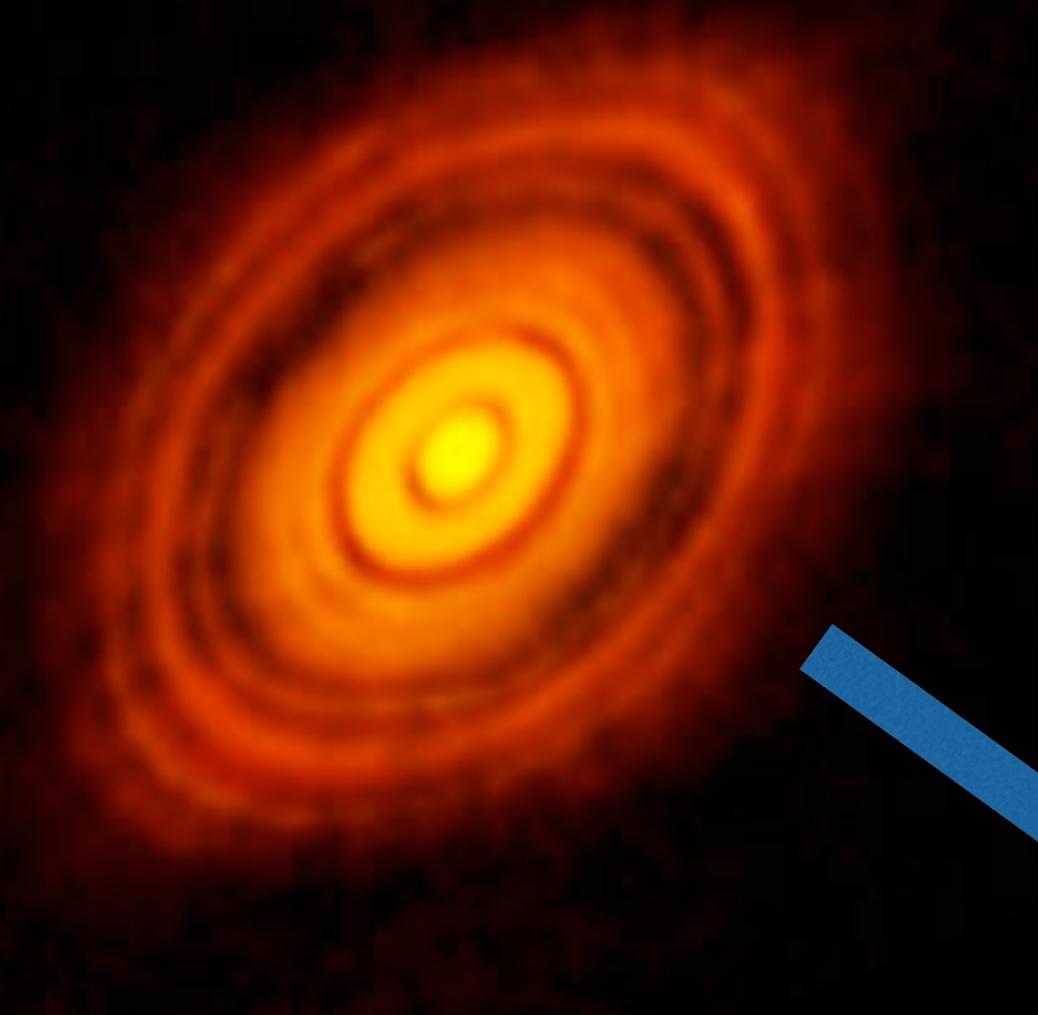
Formation of planetary systems

Sean Raymond

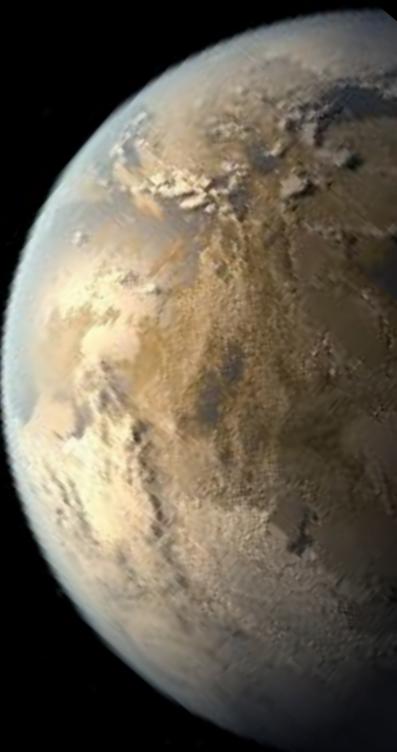
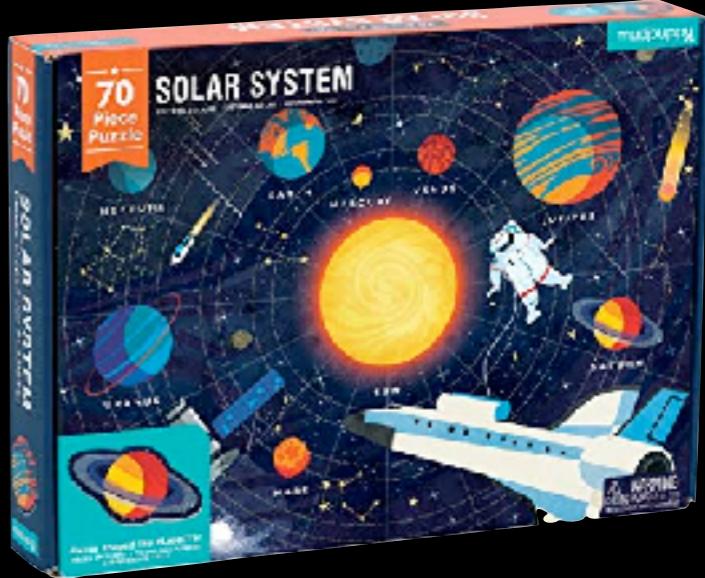
CNRS *Directeur de Recherche*
Laboratoire d'Astrophysique de Bordeaux
planetplanet.net

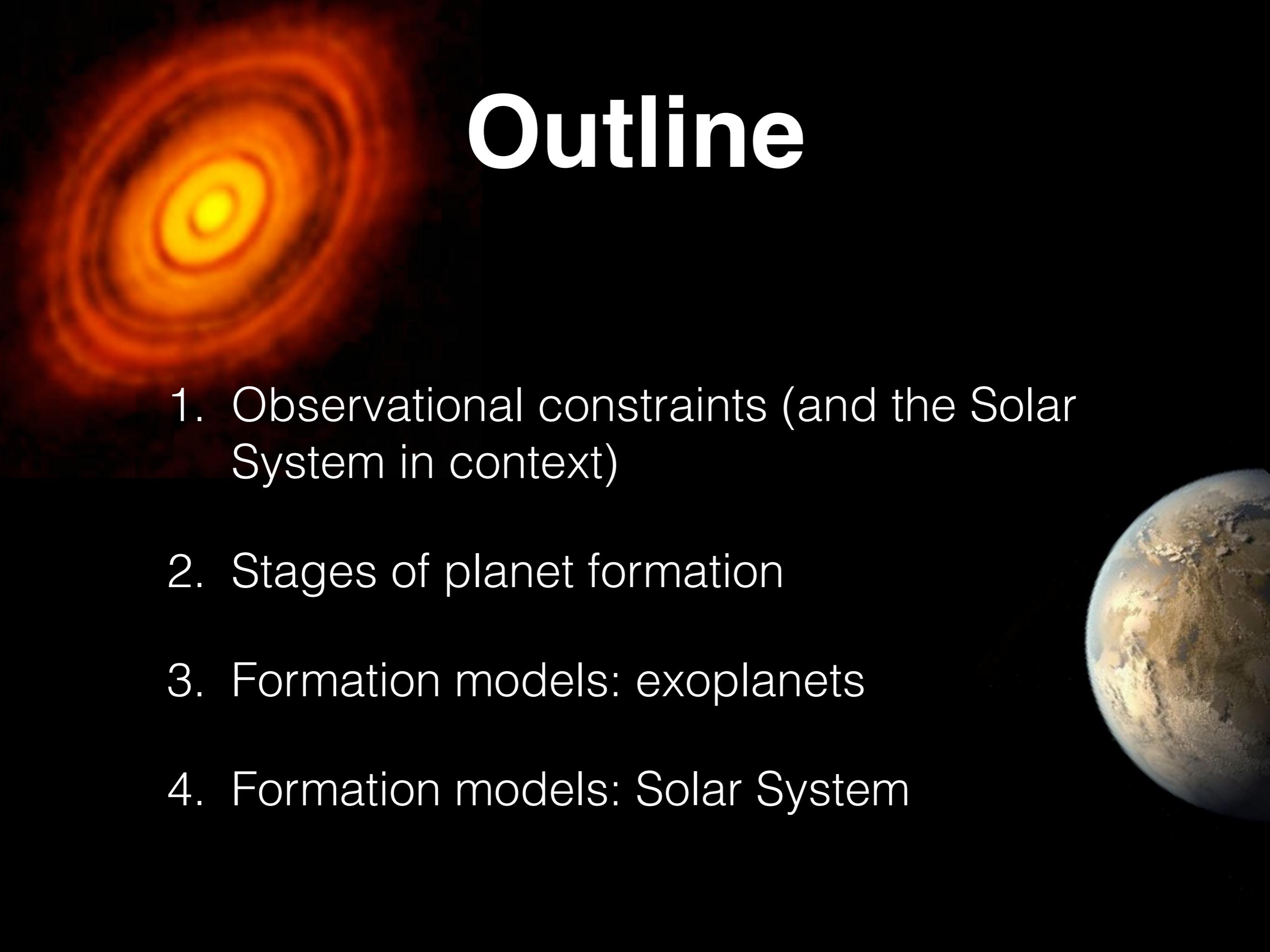


(with a few slides from A. Izidoro, P. Armitage, M. Lambrechts, A. Morbidelli)



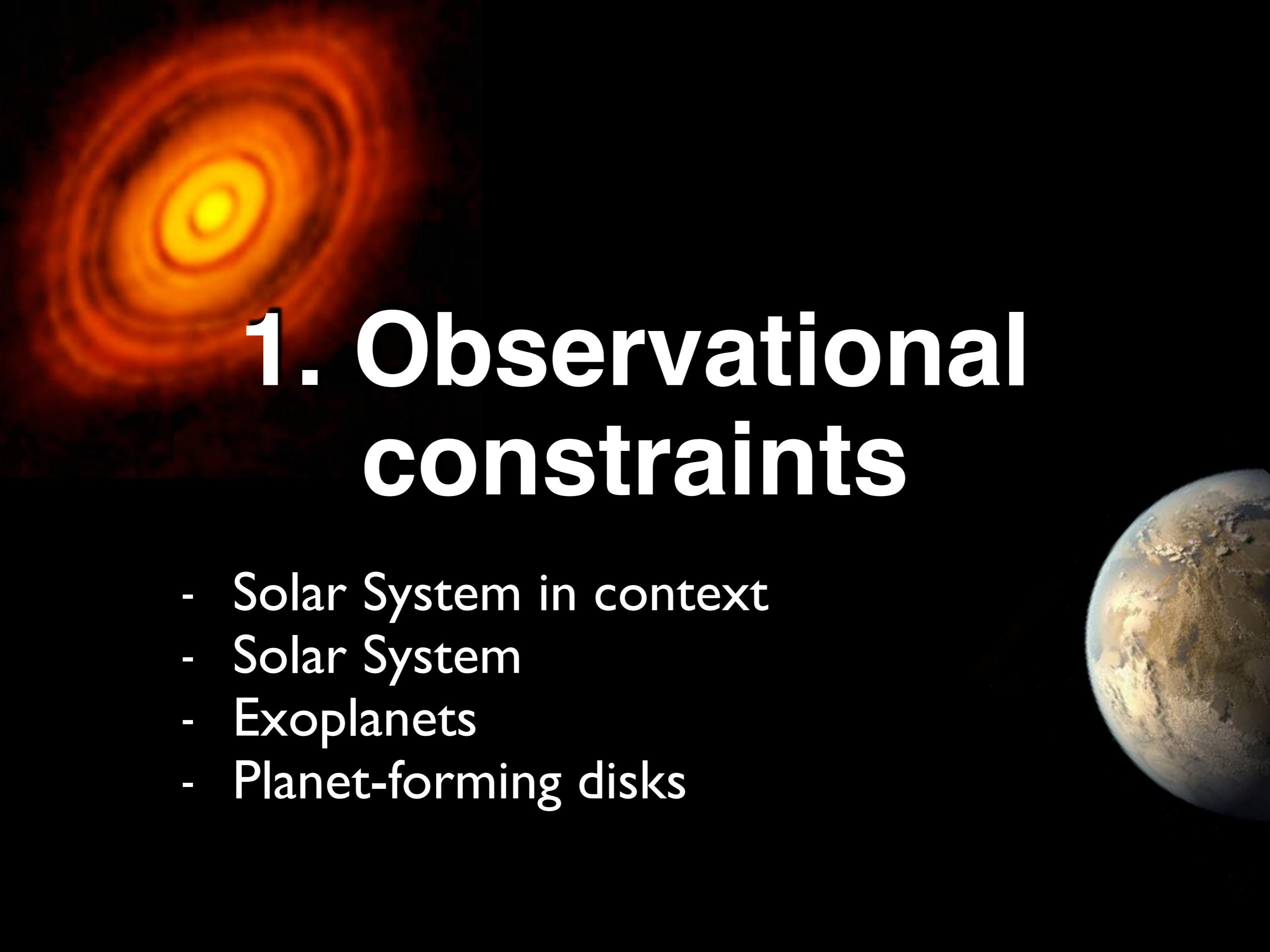
“planet formation”





Outline

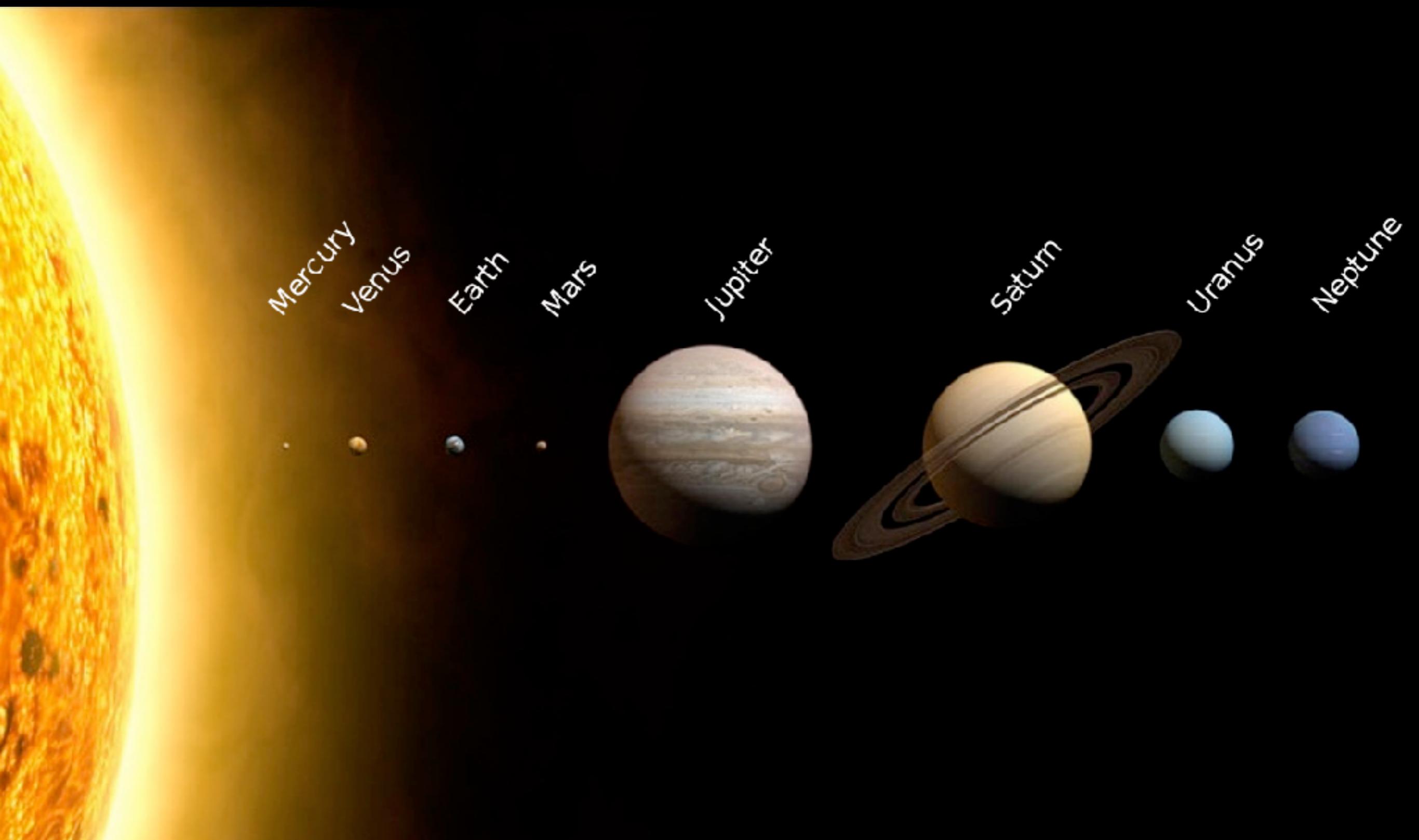
1. Observational constraints (and the Solar System in context)
2. Stages of planet formation
3. Formation models: exoplanets
4. Formation models: Solar System



1. Observational constraints

- Solar System in context
- Solar System
- Exoplanets
- Planet-forming disks

The Solar System



The exo-Solar System

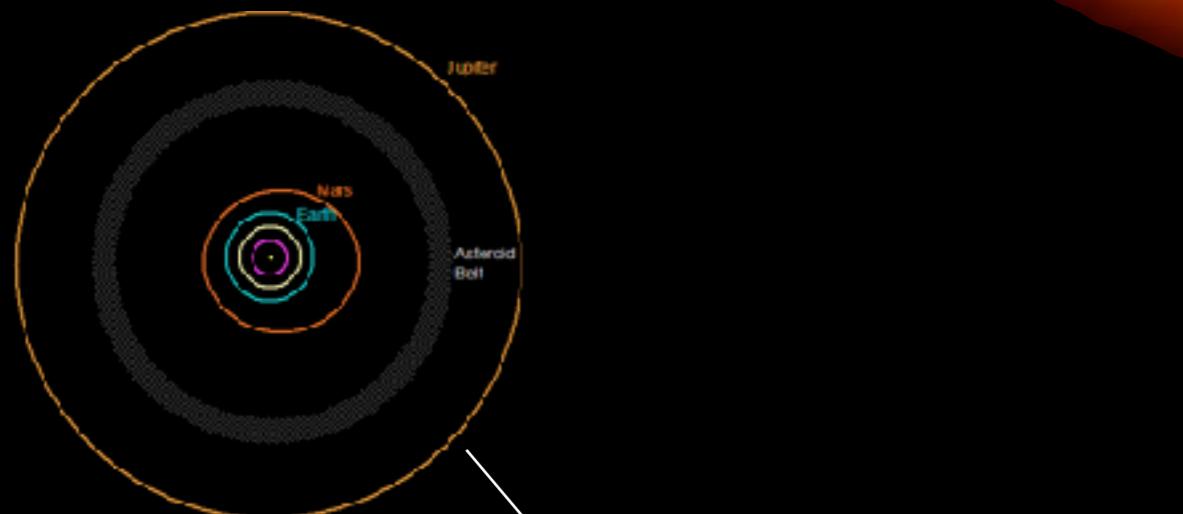
Measure:

- mass ($M_{Jup} \sin i$)
- orbital size
- orbital shape (eccentricity)



(Sun's radial velocity amplitude due to
Jupiter ~ 12 m/s, $P=12$ yr)

Solar System-like
(~1% of total)

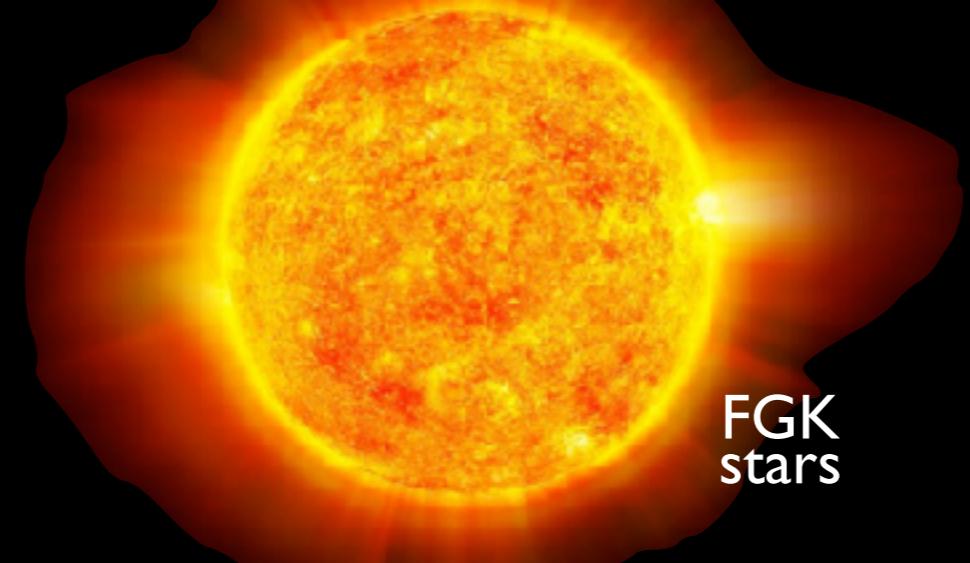


~10%

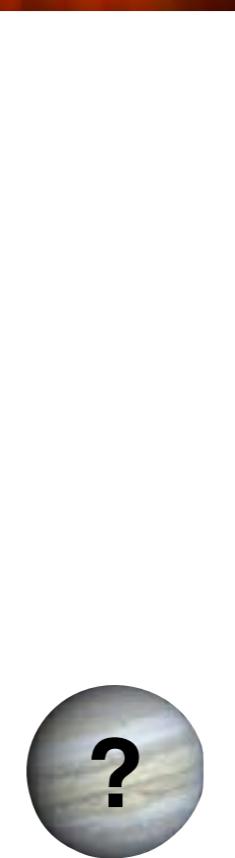
~10%

~90%

Eccentric giants
(and some hot Jupiters)

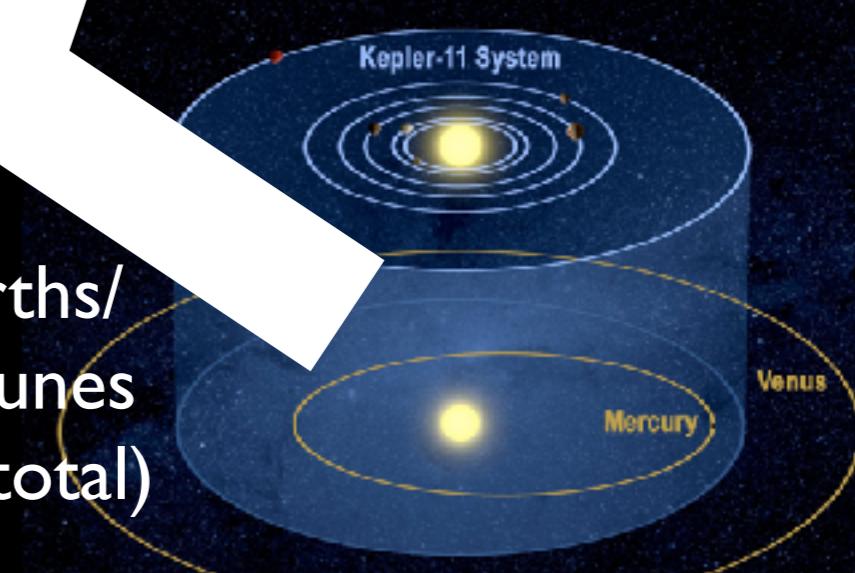
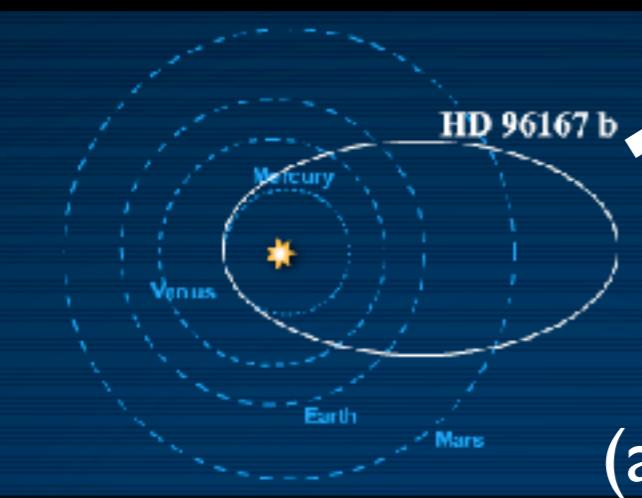


FGK
stars



~90%

super-Earths/
sub-Neptunes
(~50% of total)

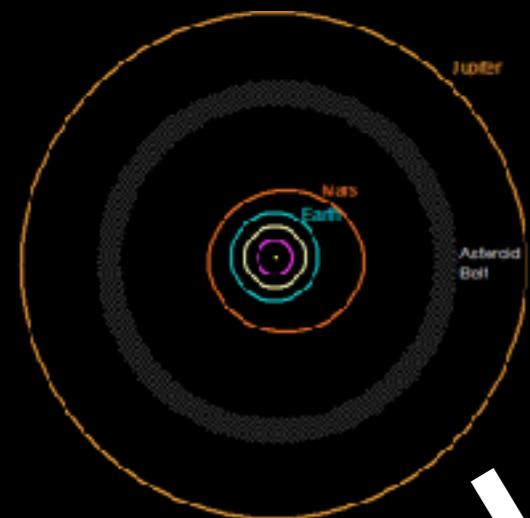


No planets
detected to date

Planet formation



Disk evolution



Pebble/planetesimal accretion



Planetesimal formation

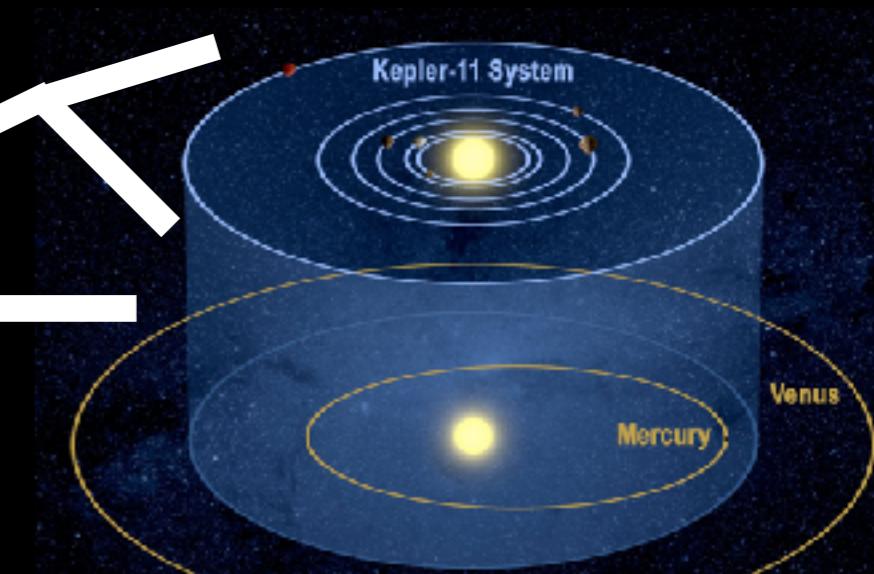
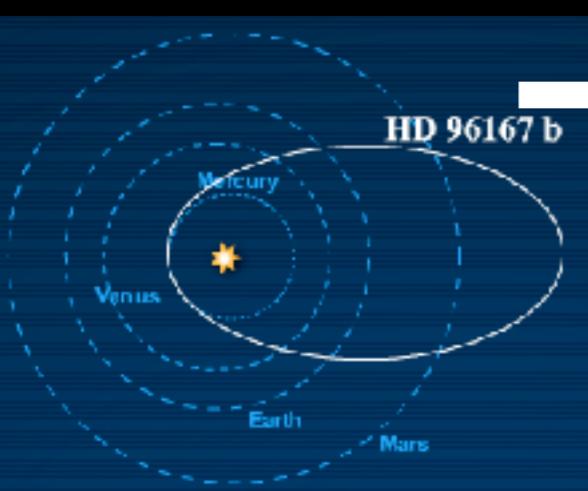


Giant impacts



Gas accretion

Orbital migration

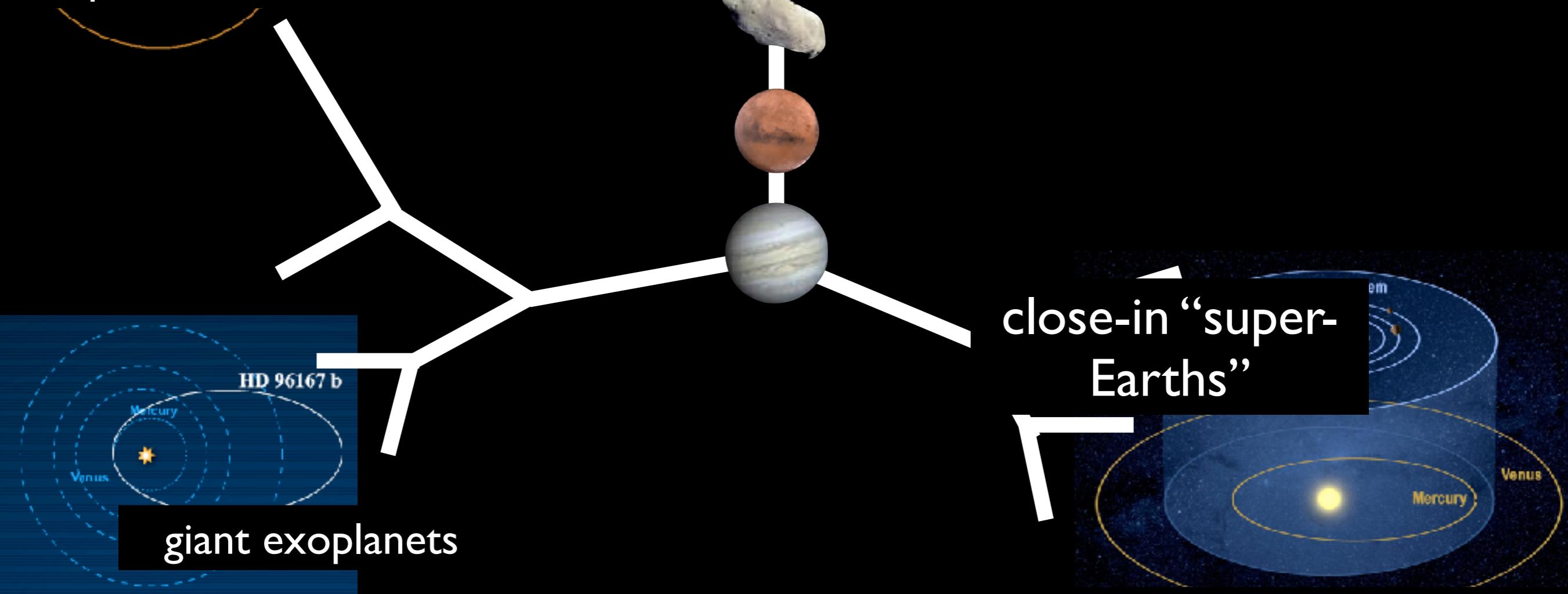


Constraints

protoplanetary
disks

Solar System

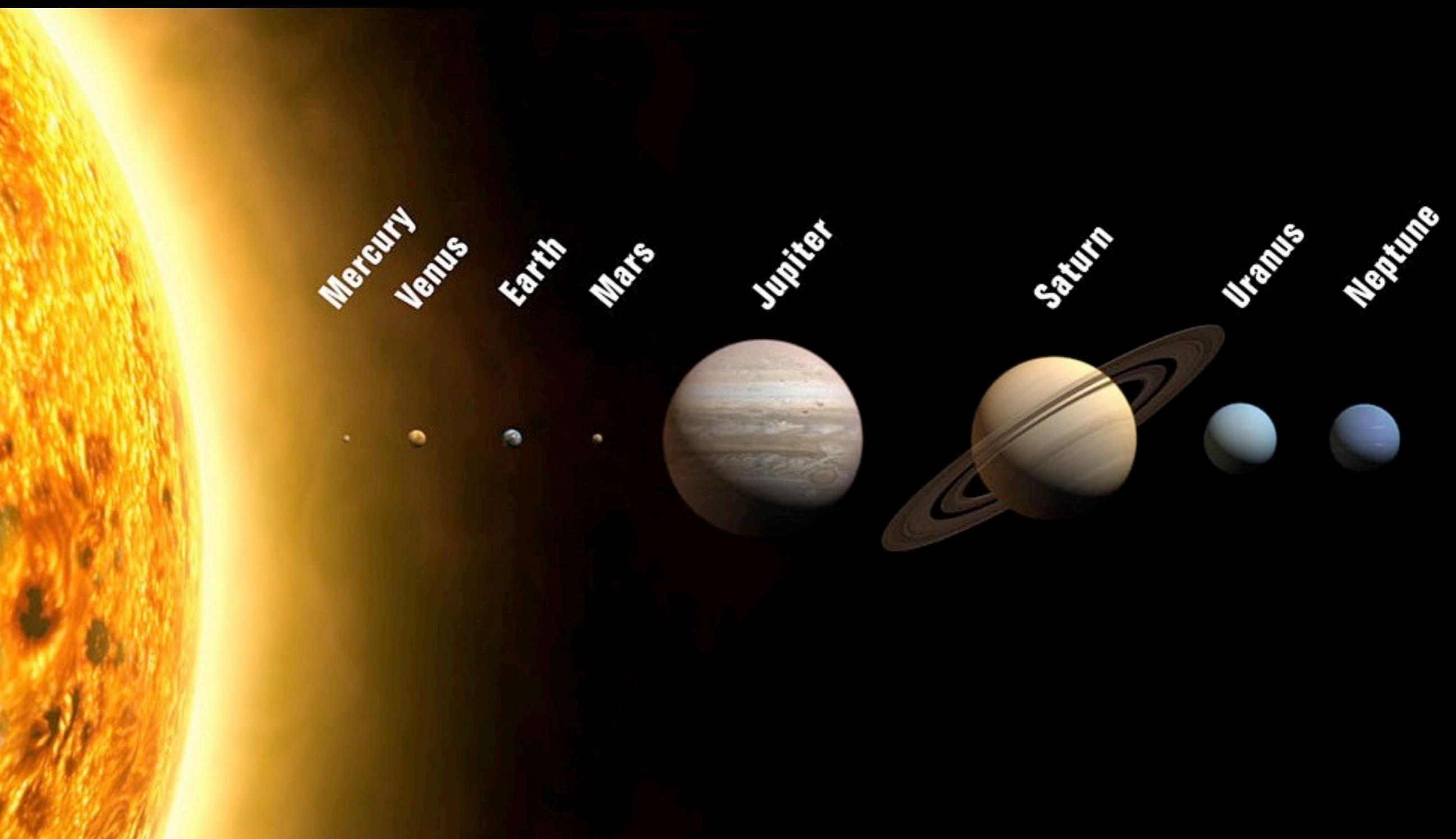
- meteorites
- asteroids and comets
- planets



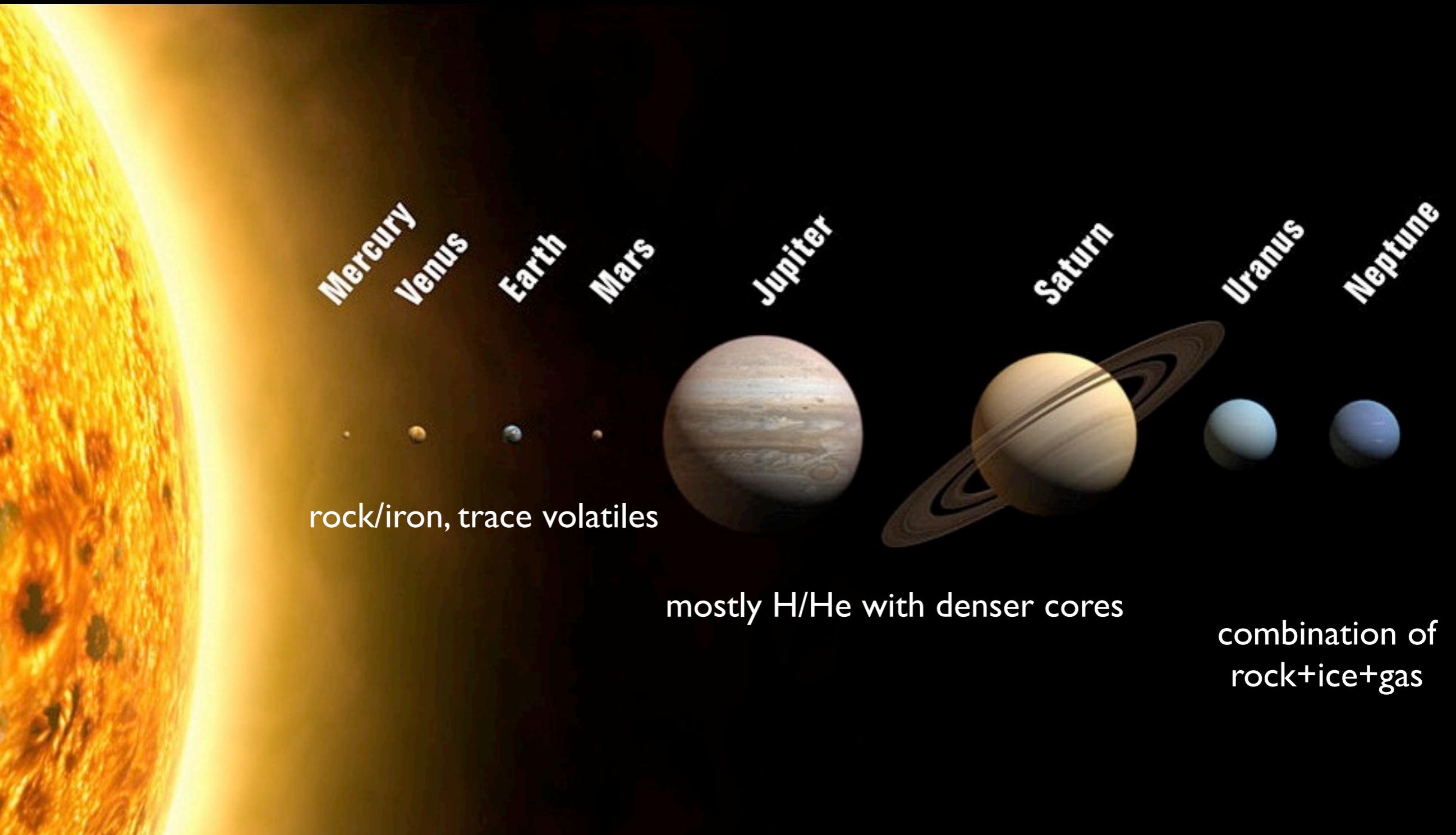
giant exoplanets

close-in “super-
Earths”

Solar System constraints

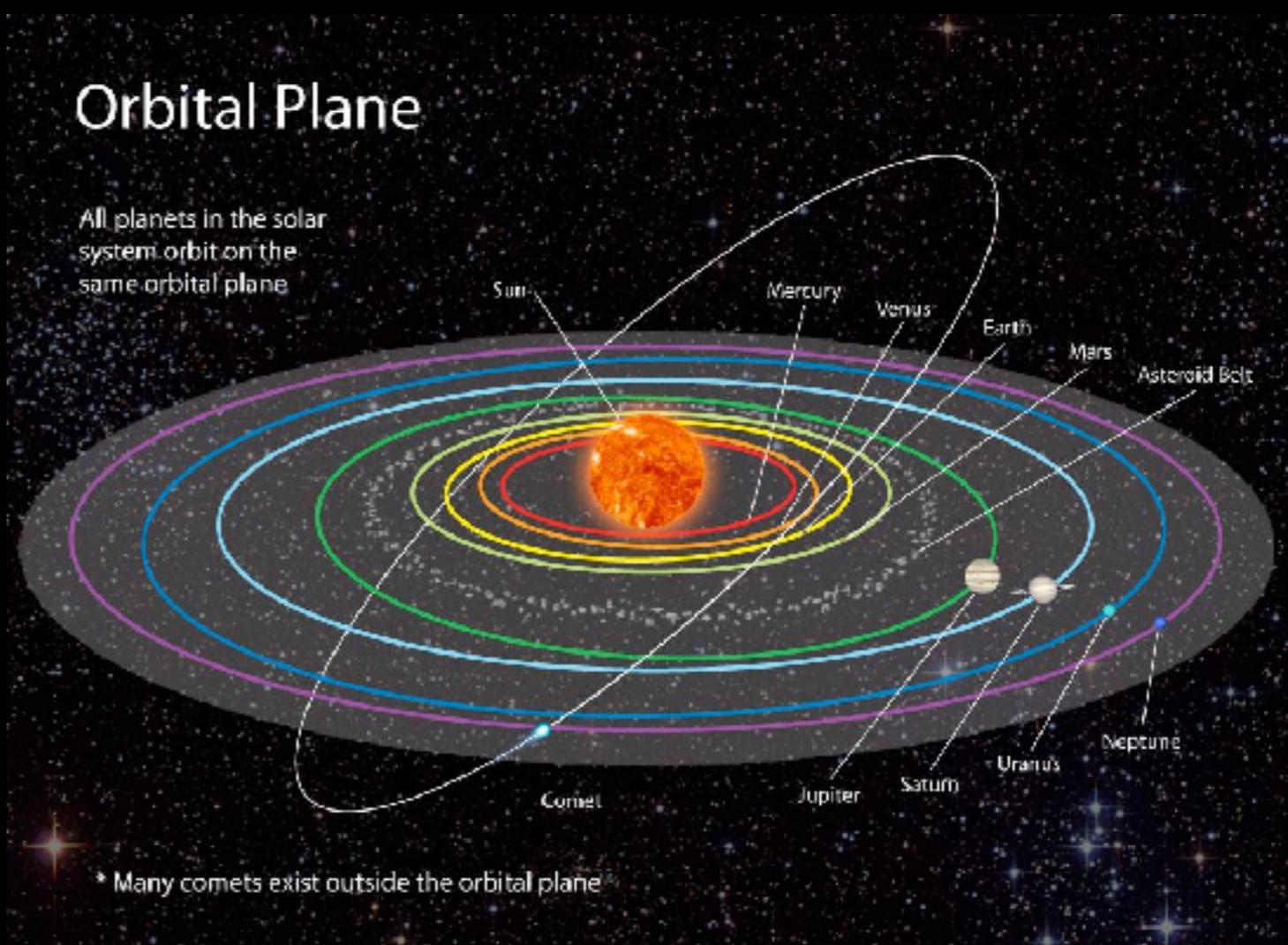


Planetary masses and compositions

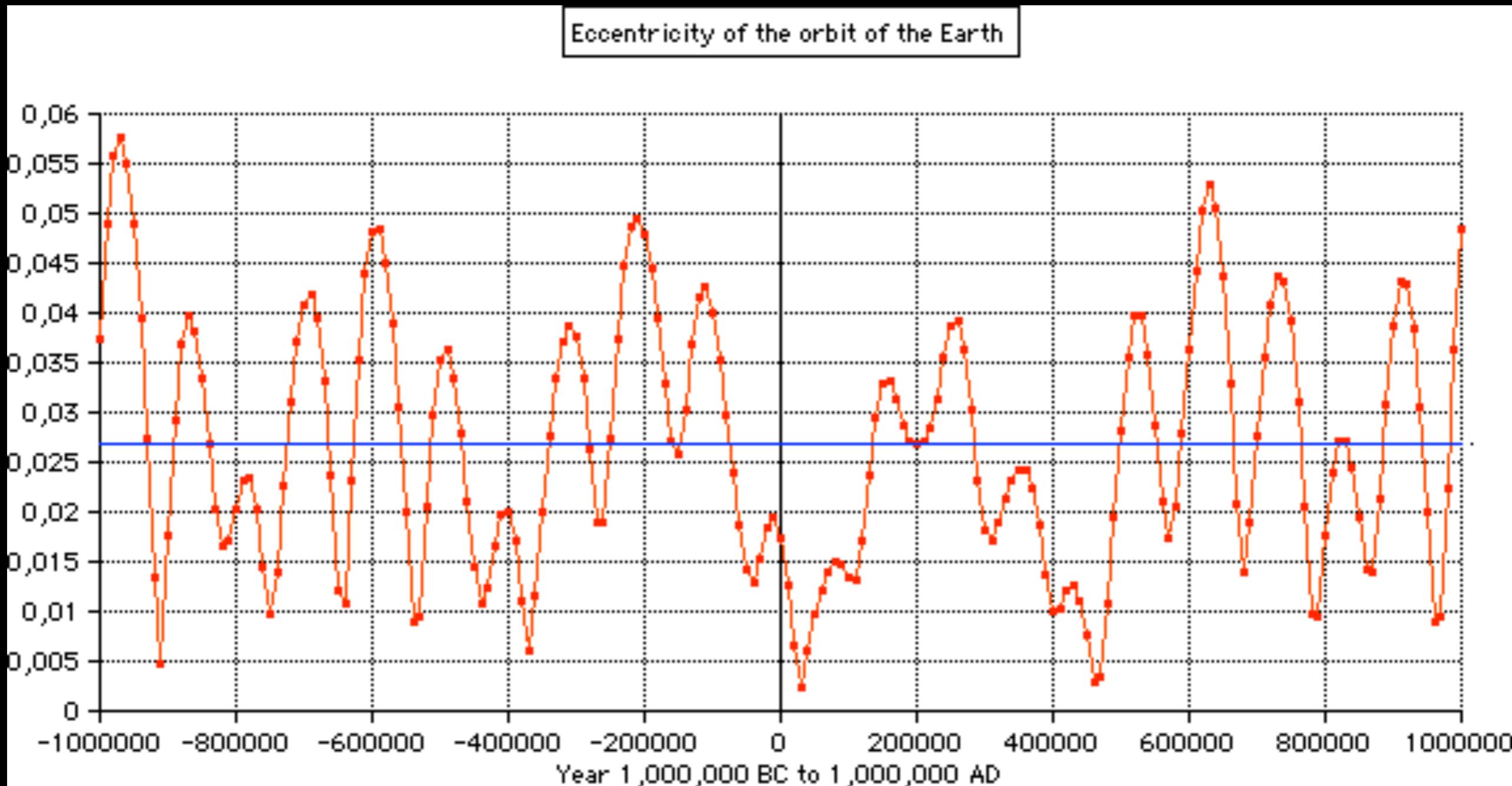


Planetary orbits

- low eccentricities
($e \sim 0.05$ for Jup/Sat,
terrestrial planets)
- low inclinations
(<few degrees)

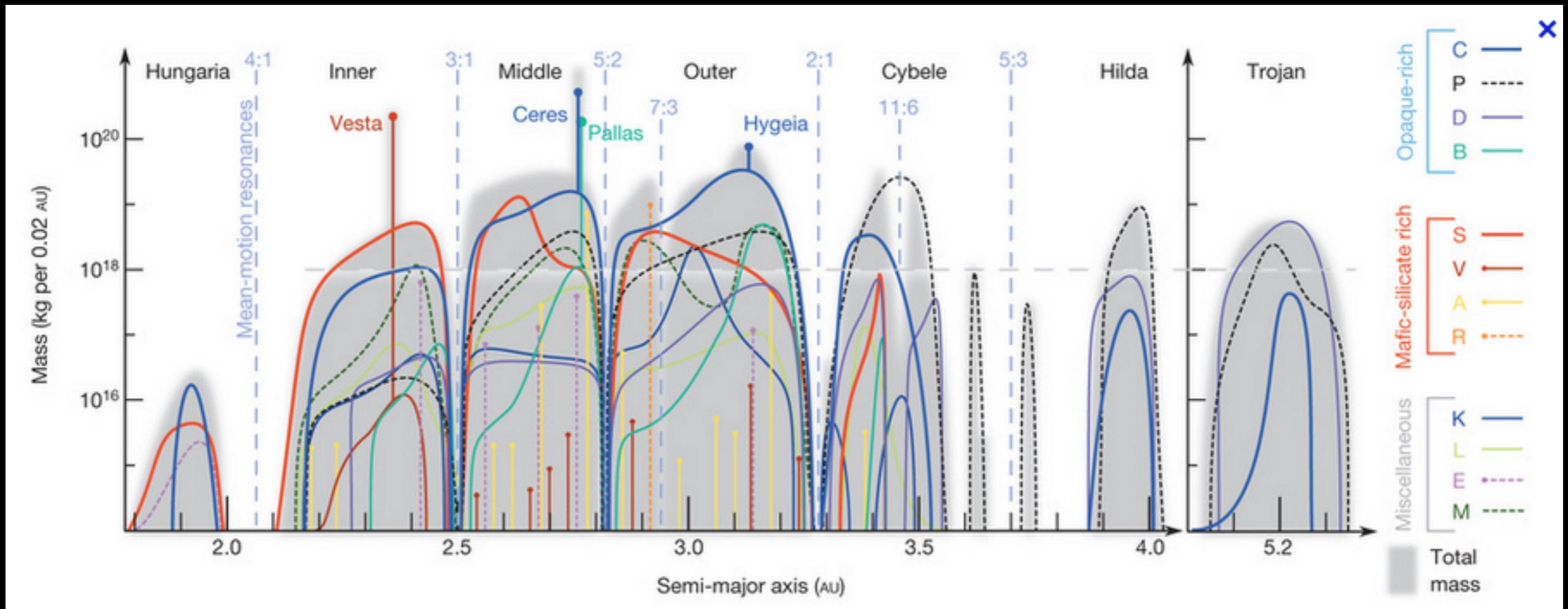


Planetary orbits not fixed in time



(link to climate via Milankovitch cycles)

Asteroid belt

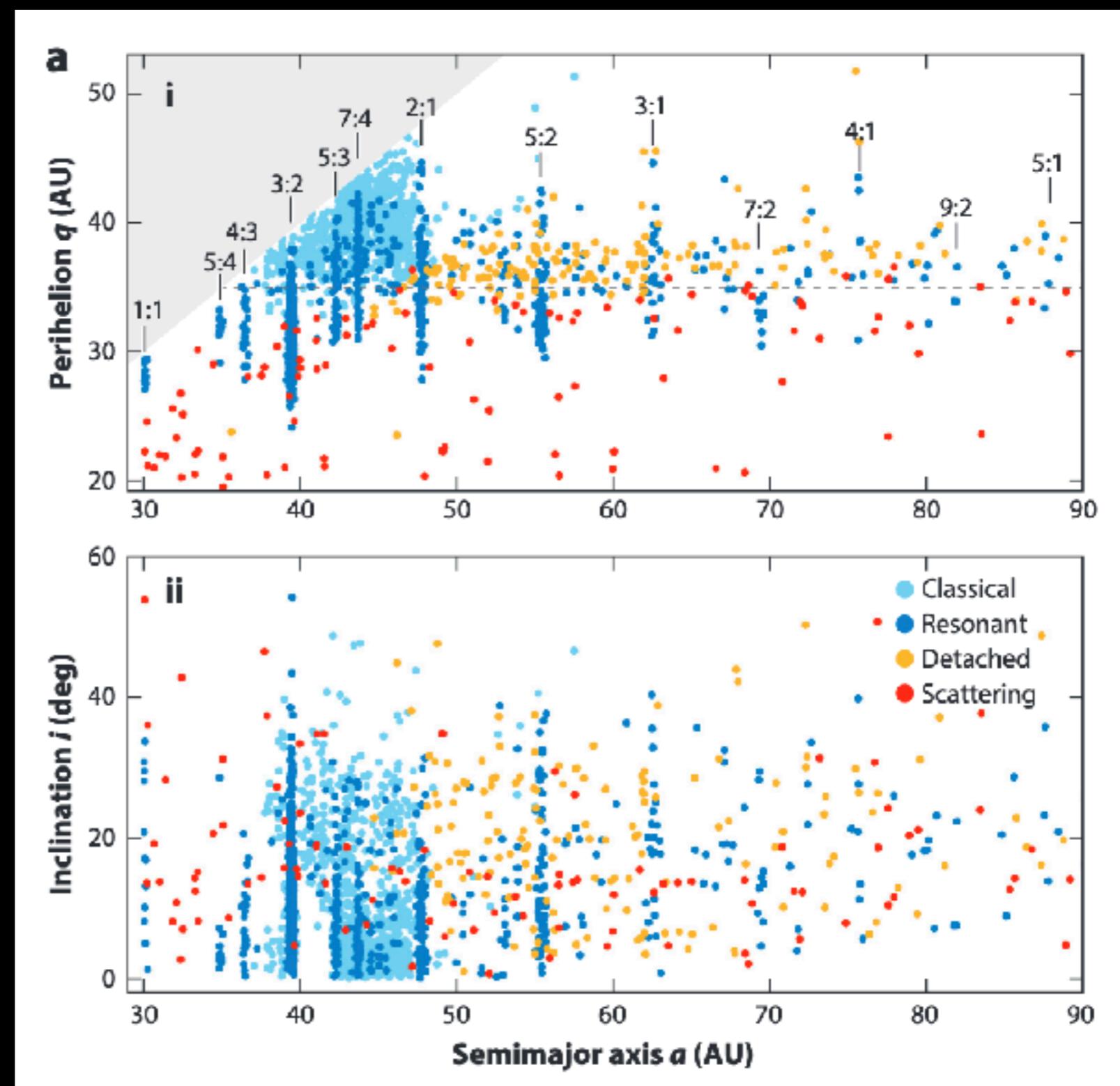


Demeo & Carry 2014

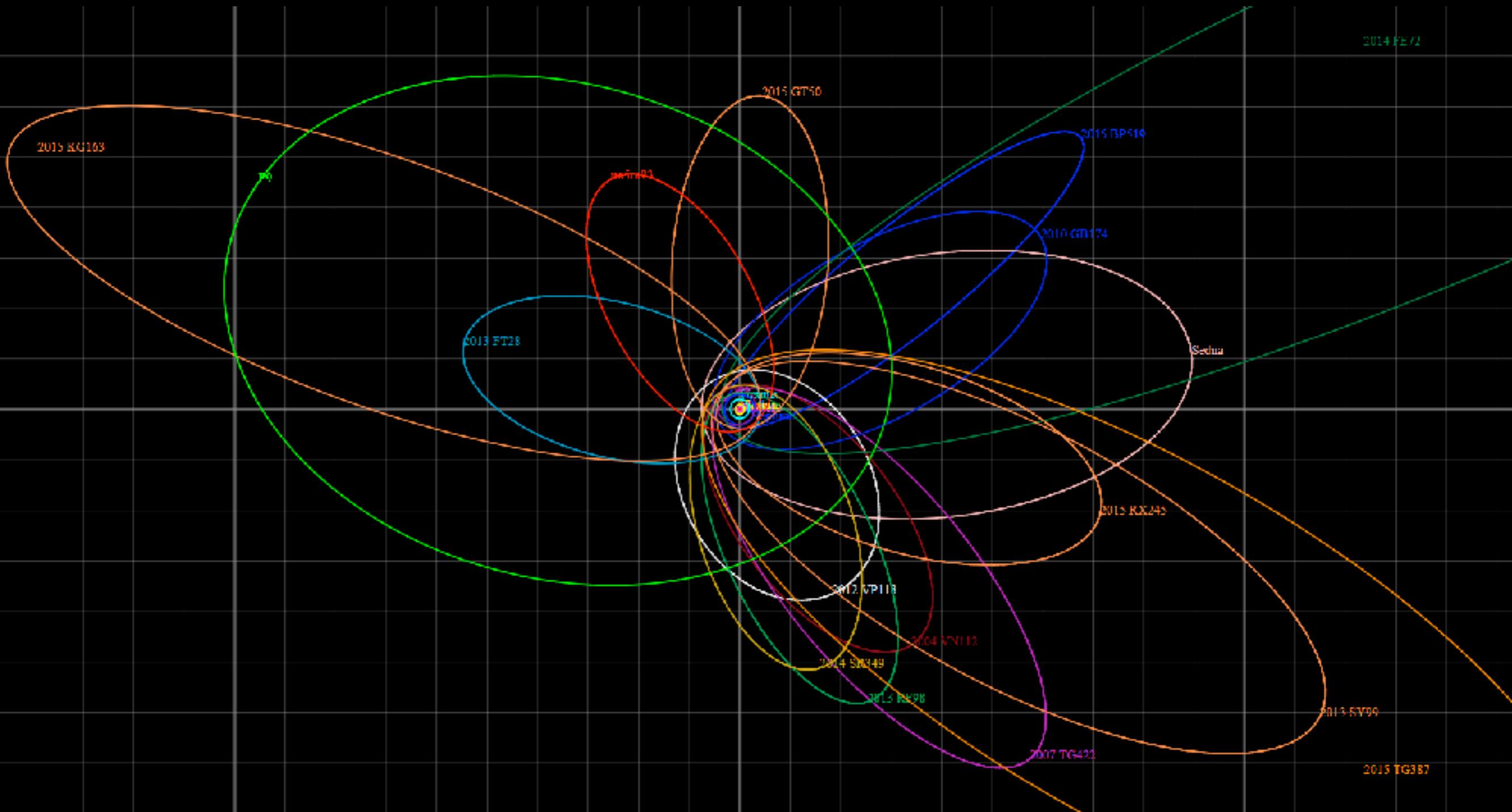
- Total mass $\sim 5 \times 10^{-4} M_{\text{Earth}}$
- Diversity in composition
 - Rough inner (S-type)/outer (C-type) dichotomy

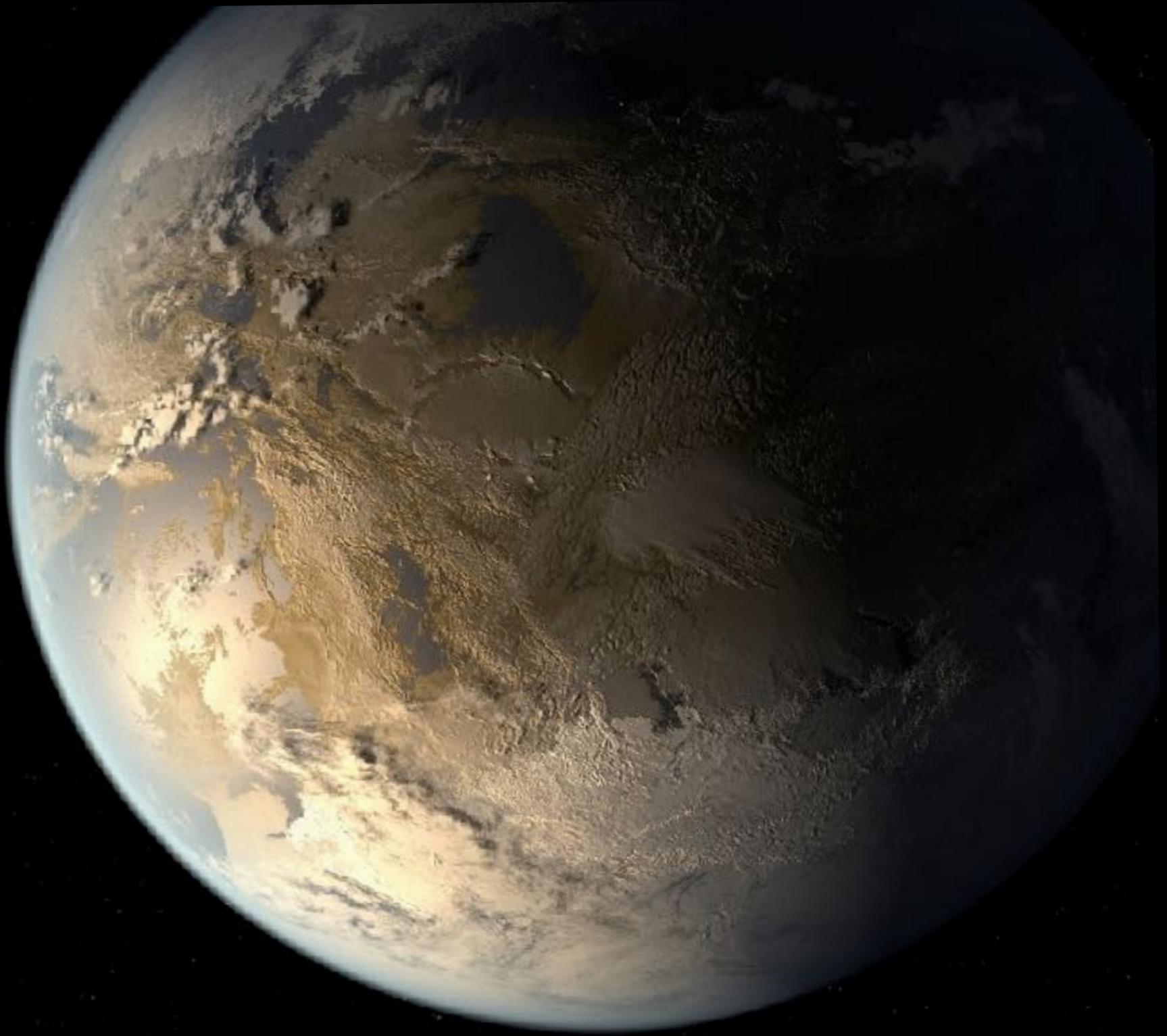
Kuiper belt

- Total mass $\sim 0.1 M_{\text{Earth}}$
- Variety of dynamical classes

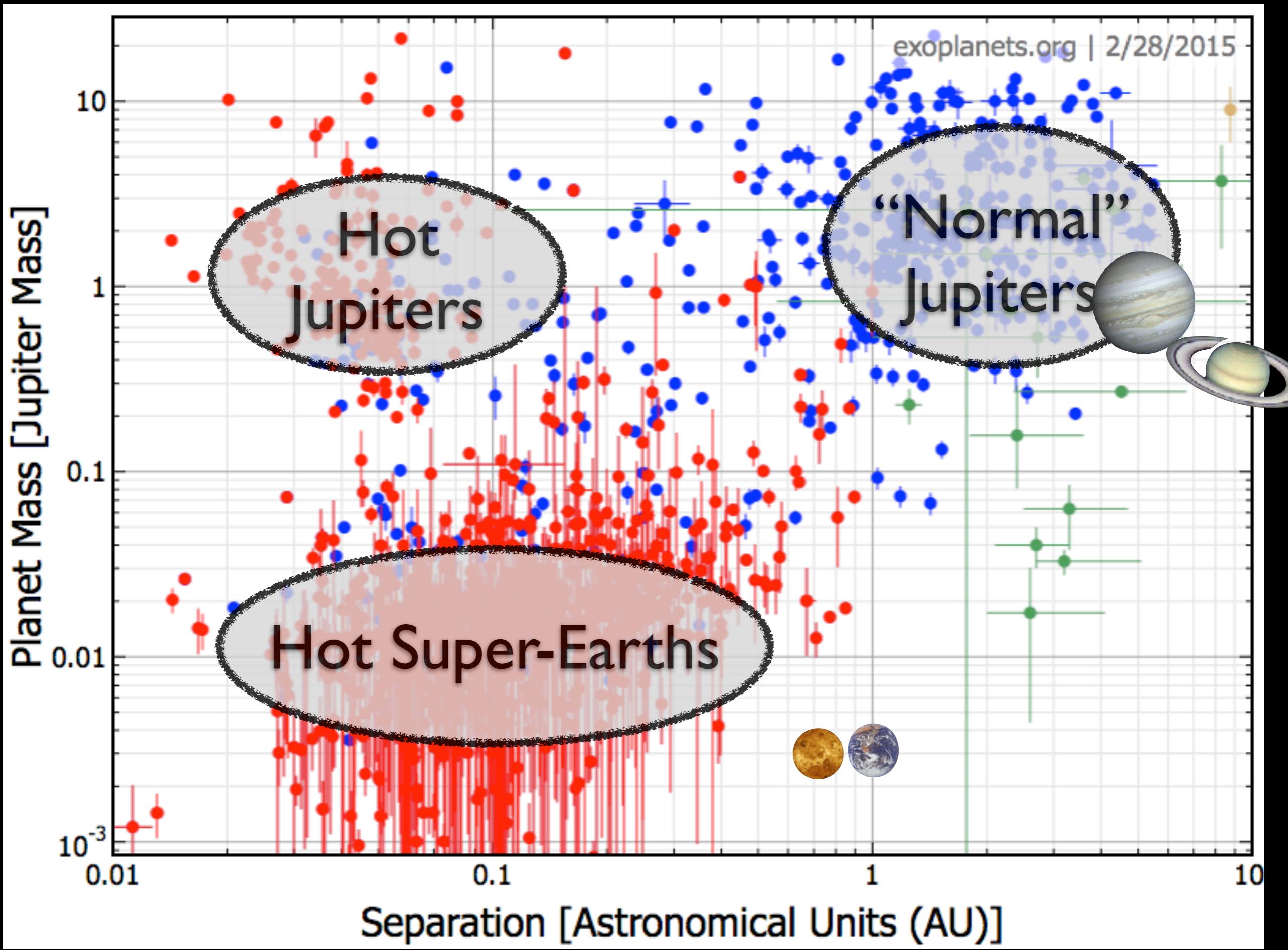


Evidence for “Planet Nine”?

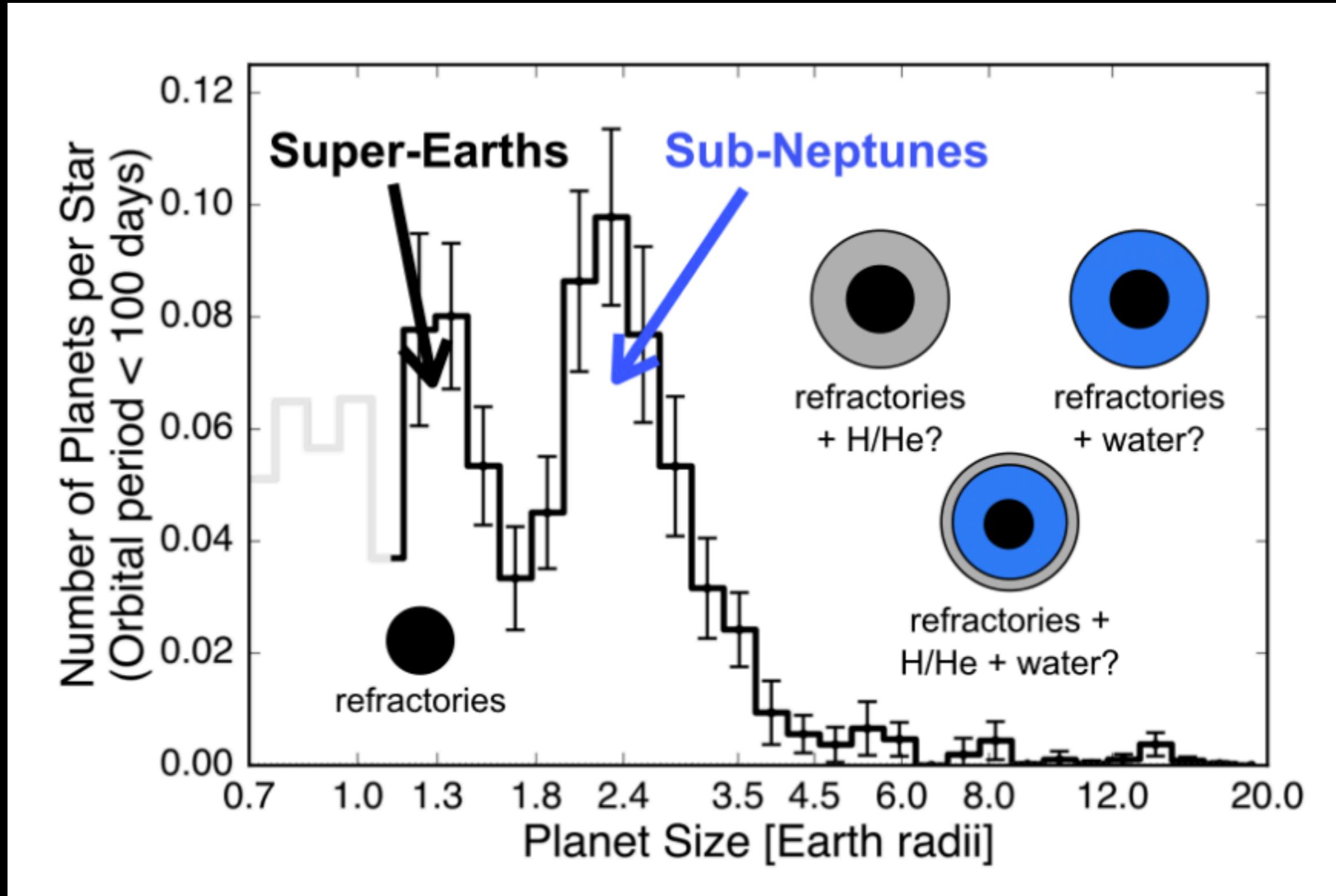




Exoplanet constraints



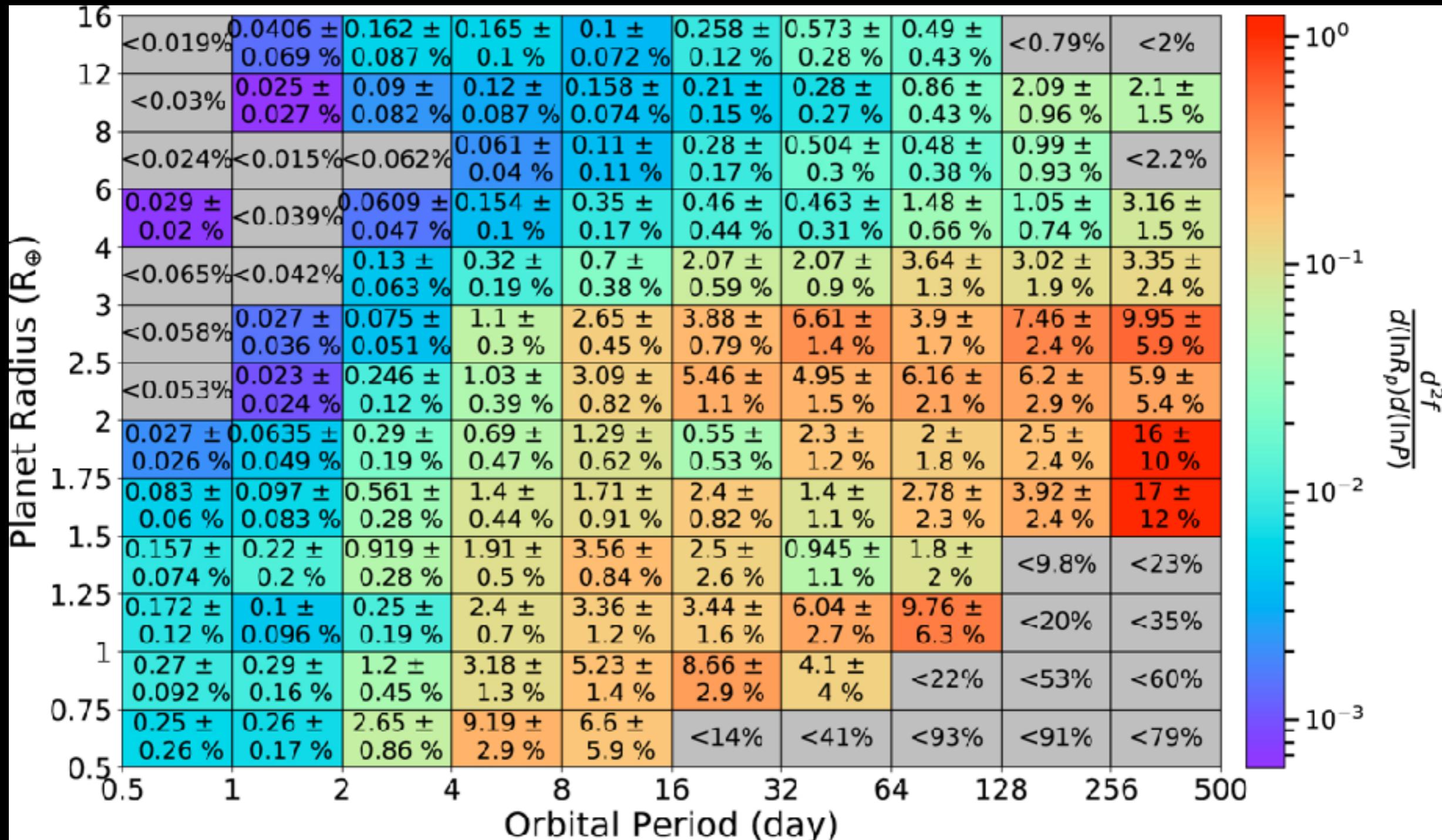
Exoplanet size distribution



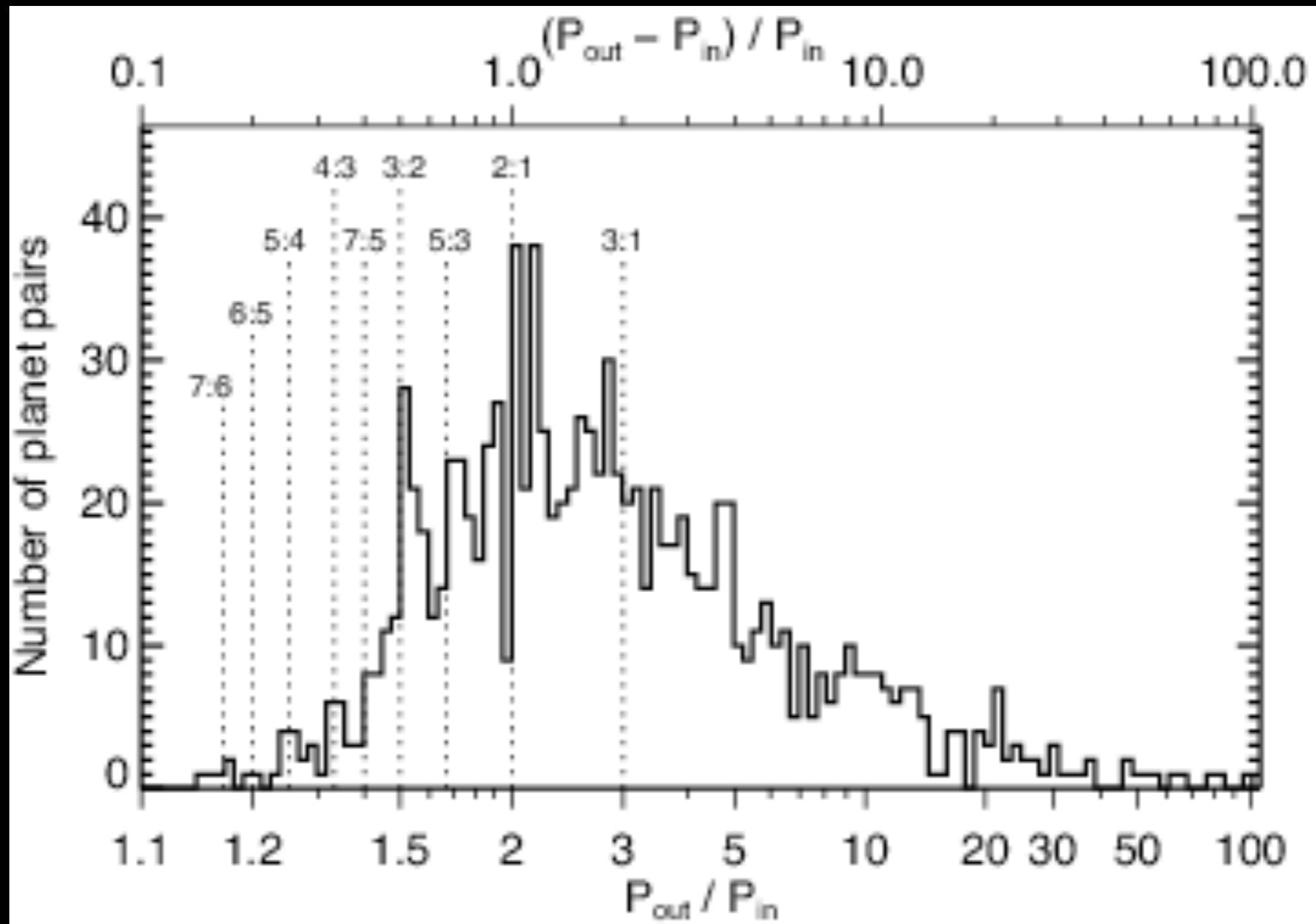
Cloutier (2024)

after Fulton et al (2017); Fulton & Petigura (2018); van Eylen et al (2018), ...

Exoplanet occurrence rate

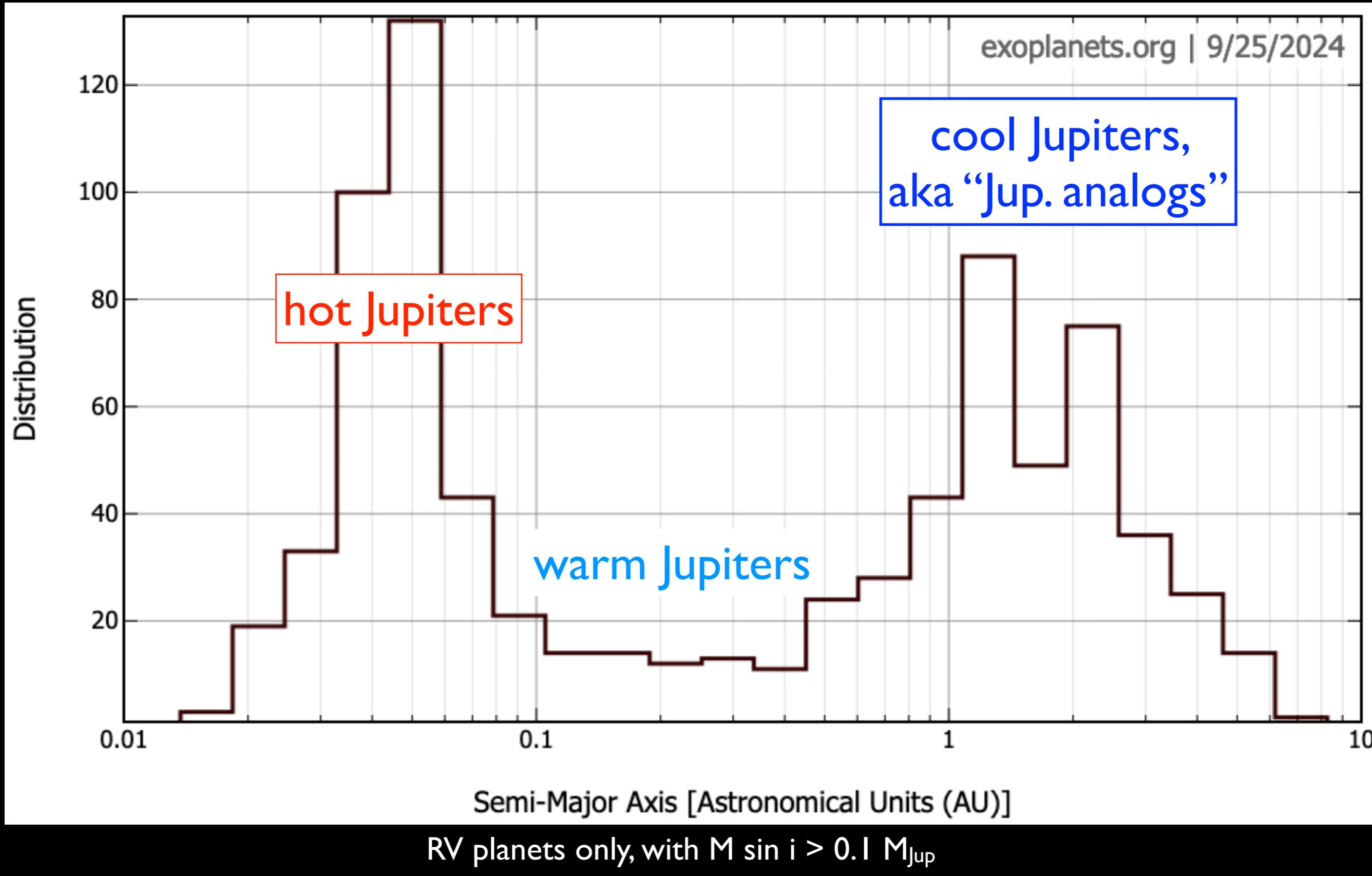


Period Ratio distribution

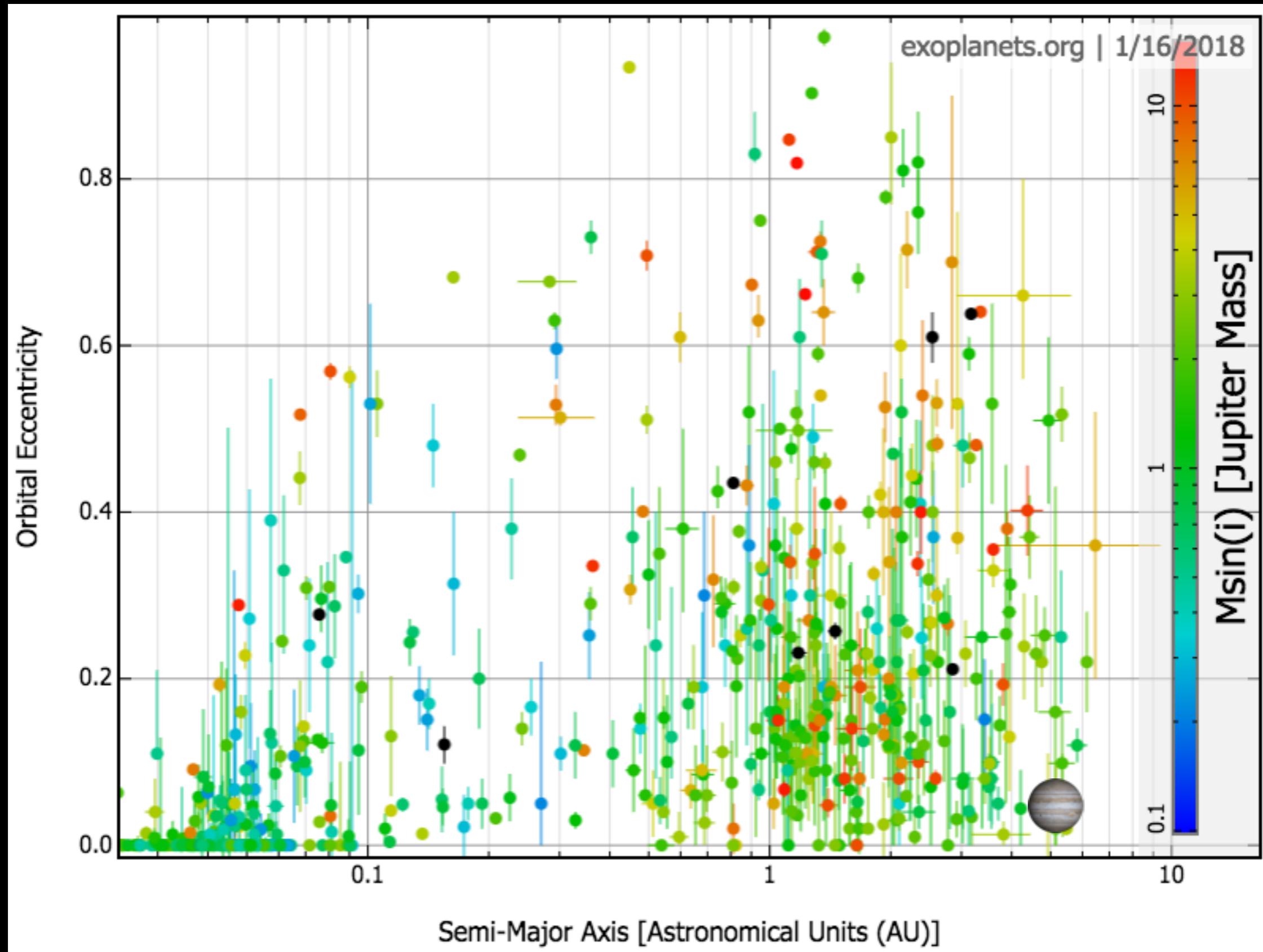


Winn & Fabrycky 2015

Radial distribution of gas giants

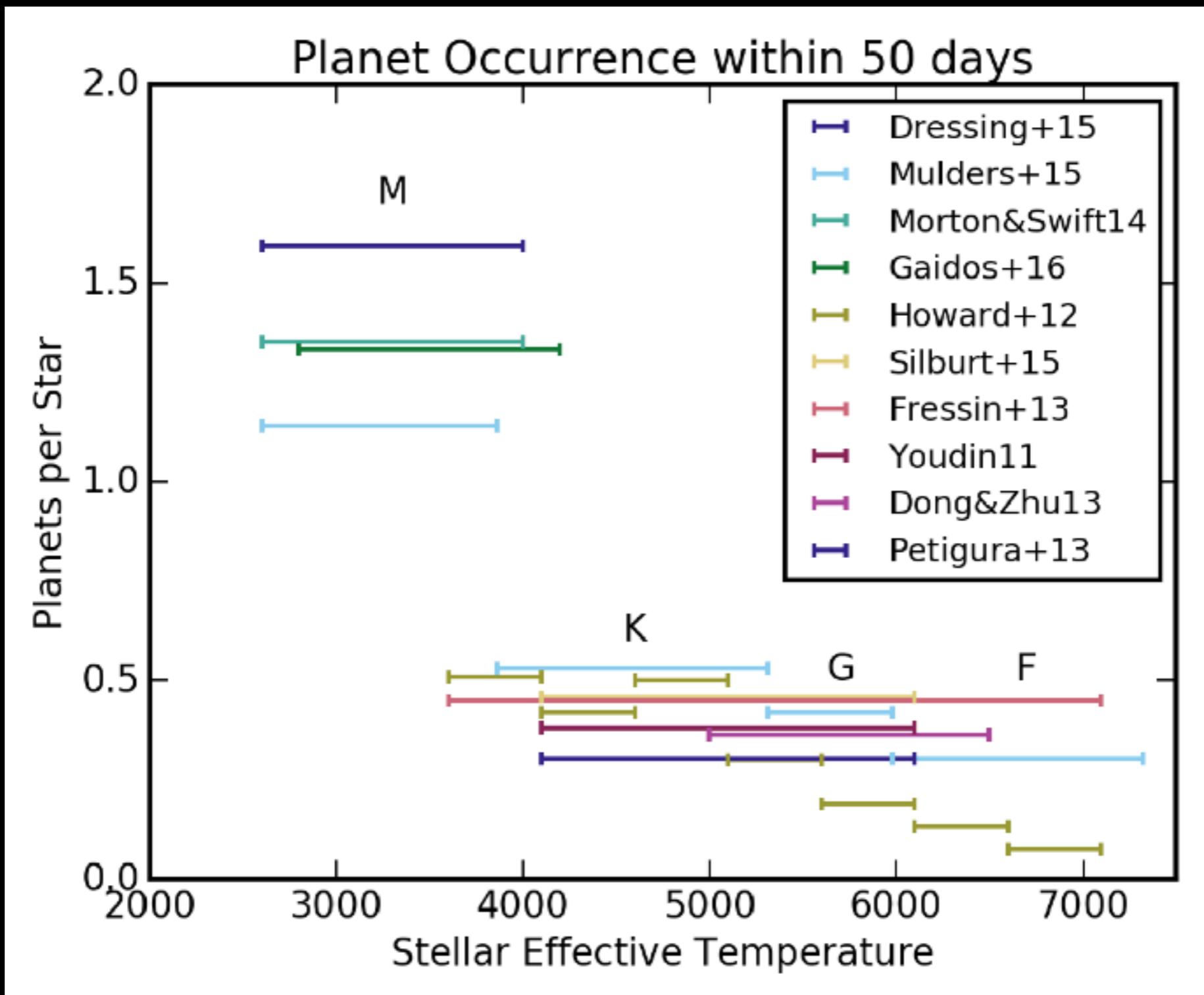


Eccentricity distribution (giants)



Wright et al 2011

Low-mass stars have more close-in planets

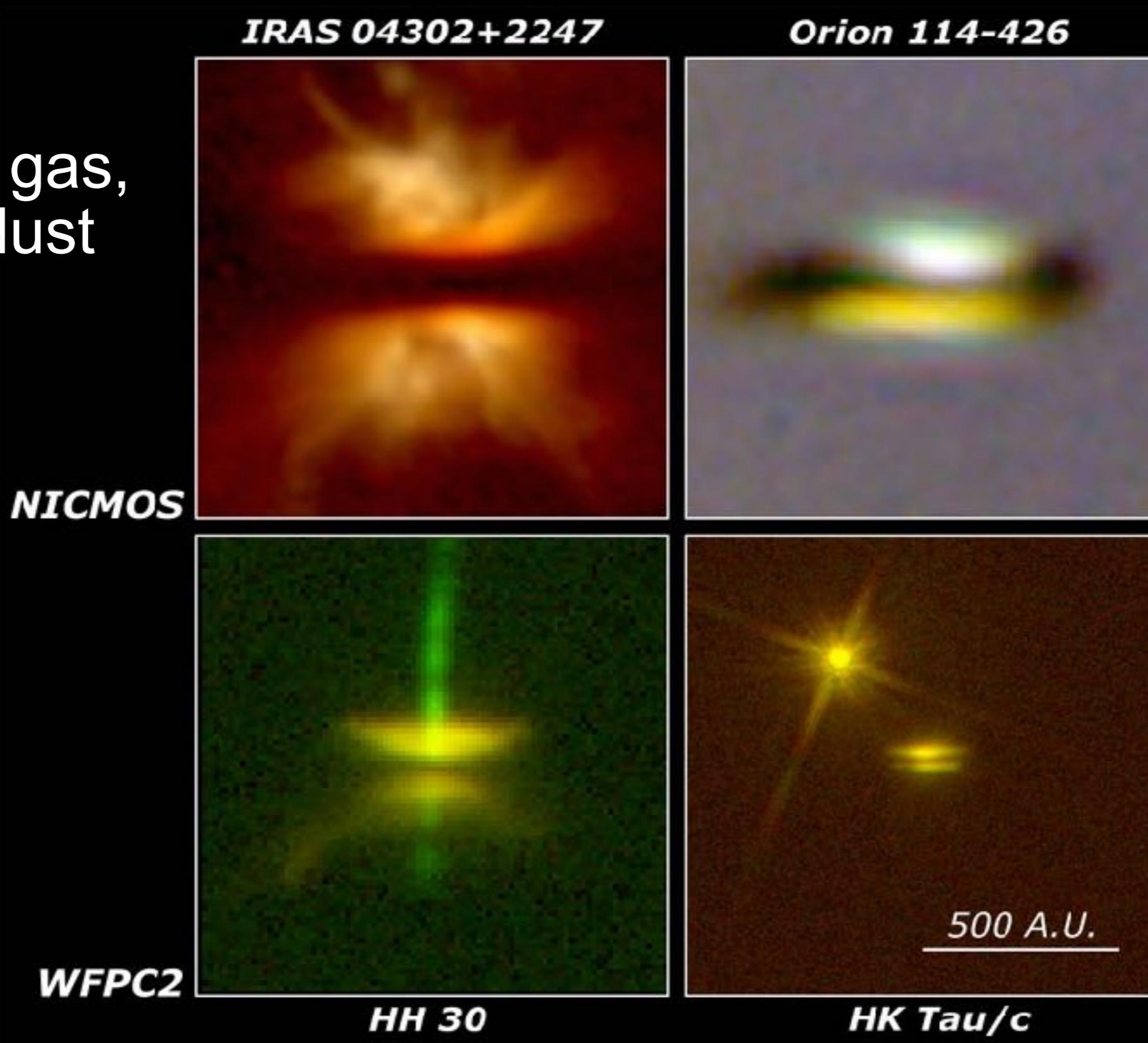


Protoplanetary disks



Disks around young stars: Hubble

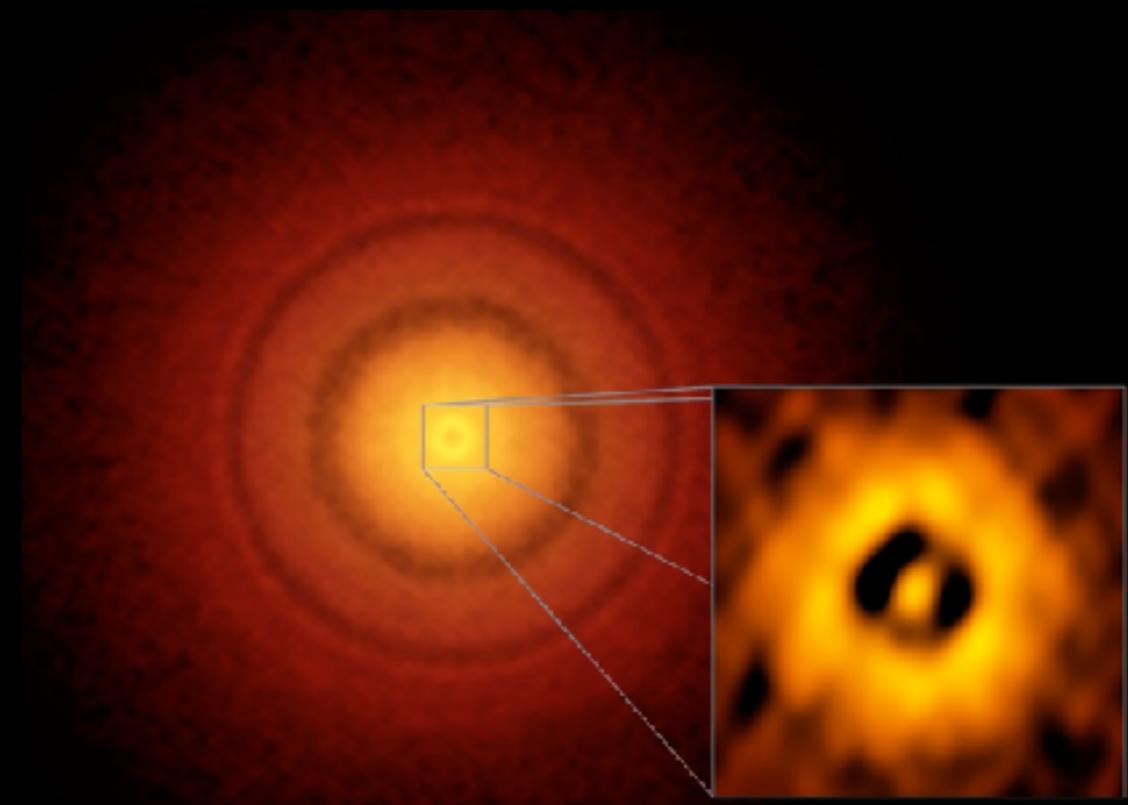
- 99% gas,
1% dust



ALMA Images of young disks

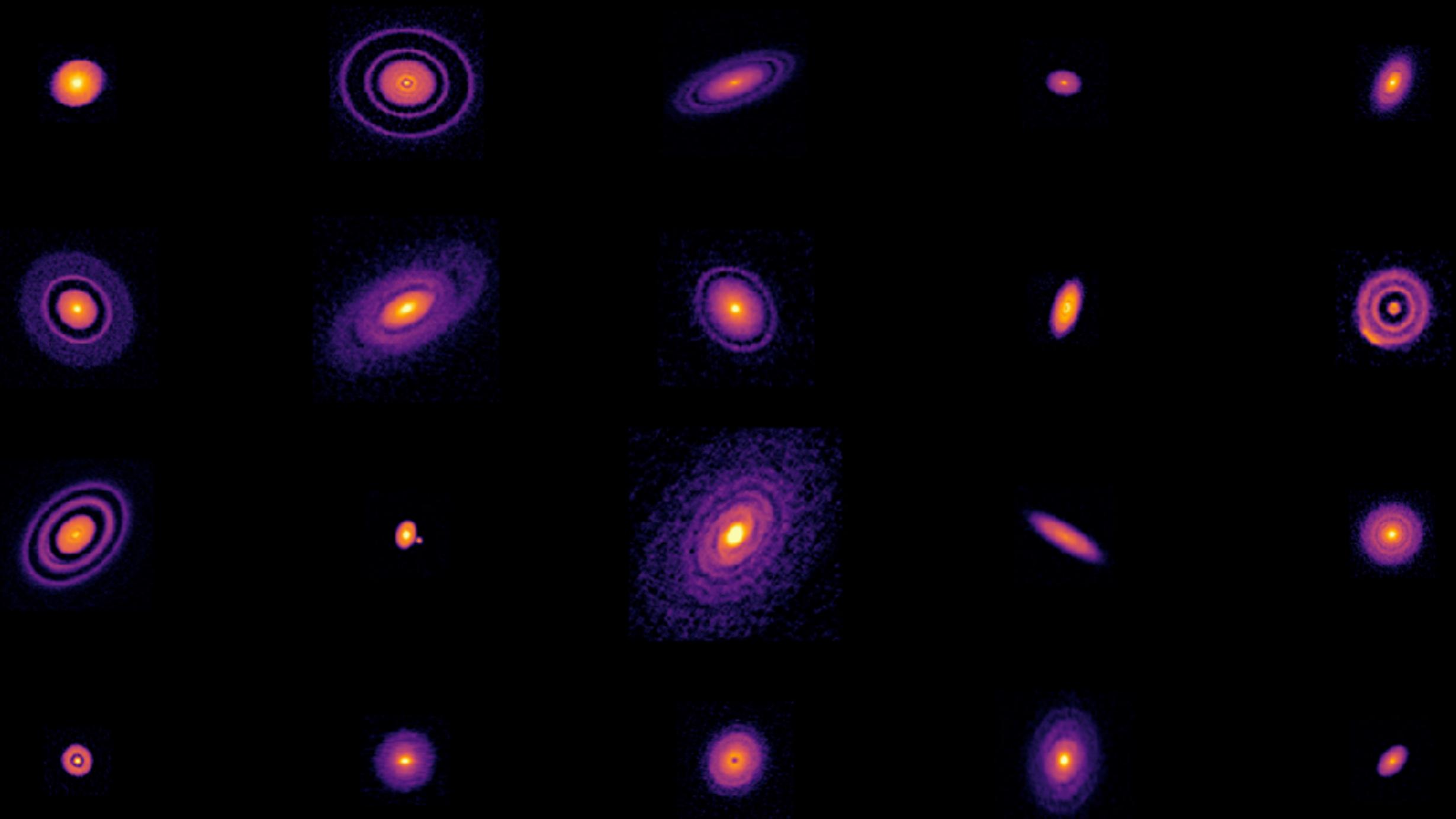


ALMA Partnership 2015

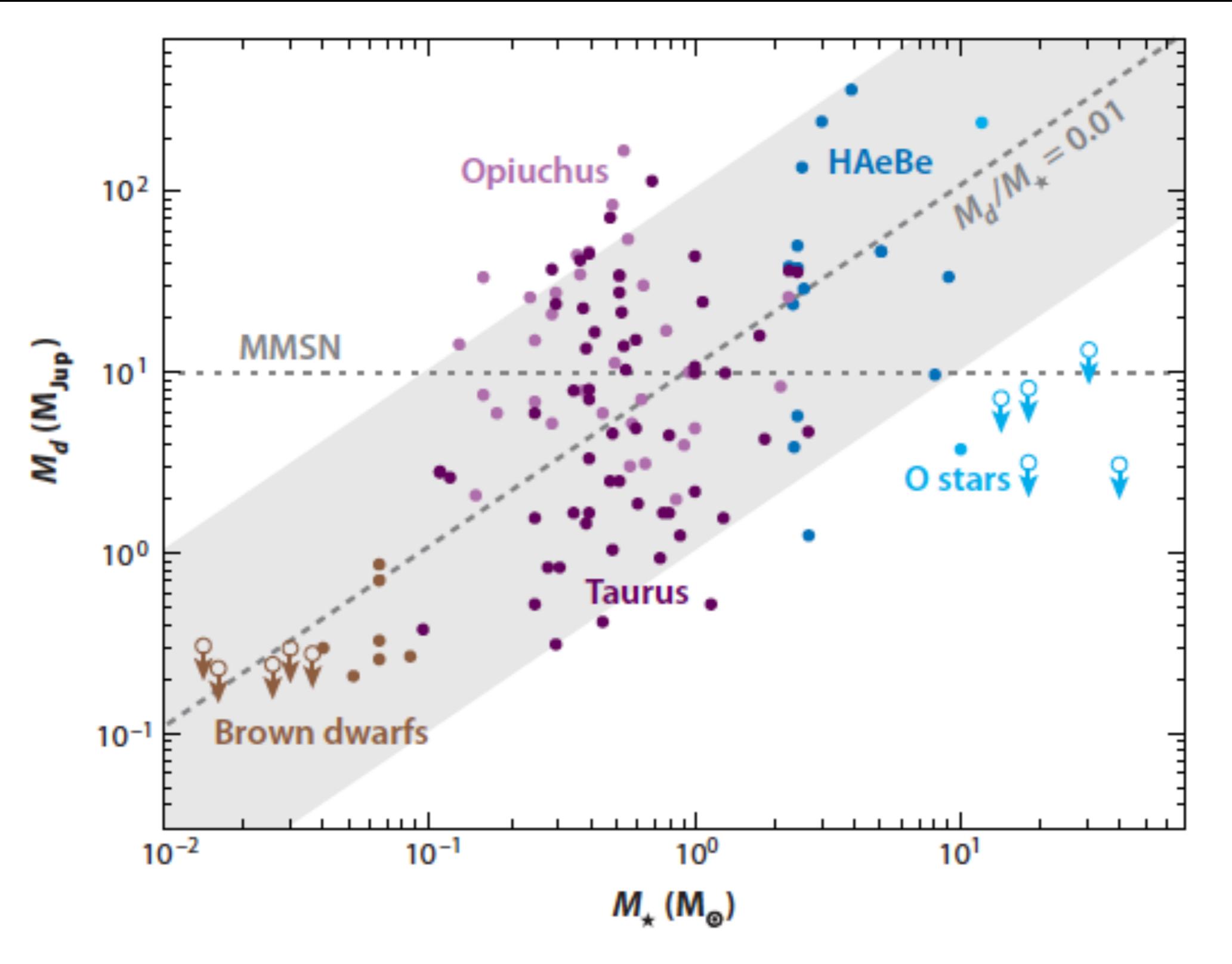


Andrews et al (2016)

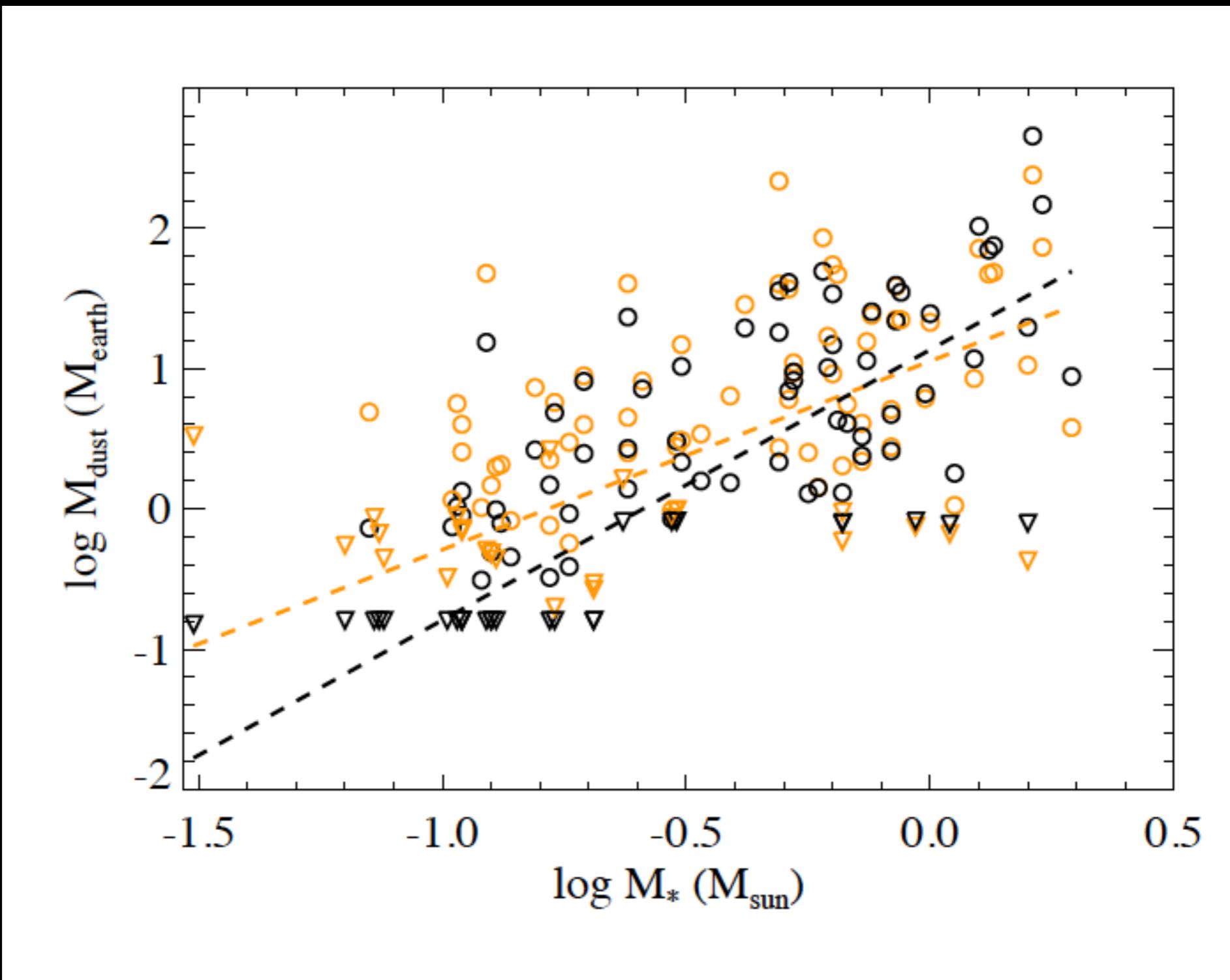
DSHARP disks (ALMA)



Disk masses

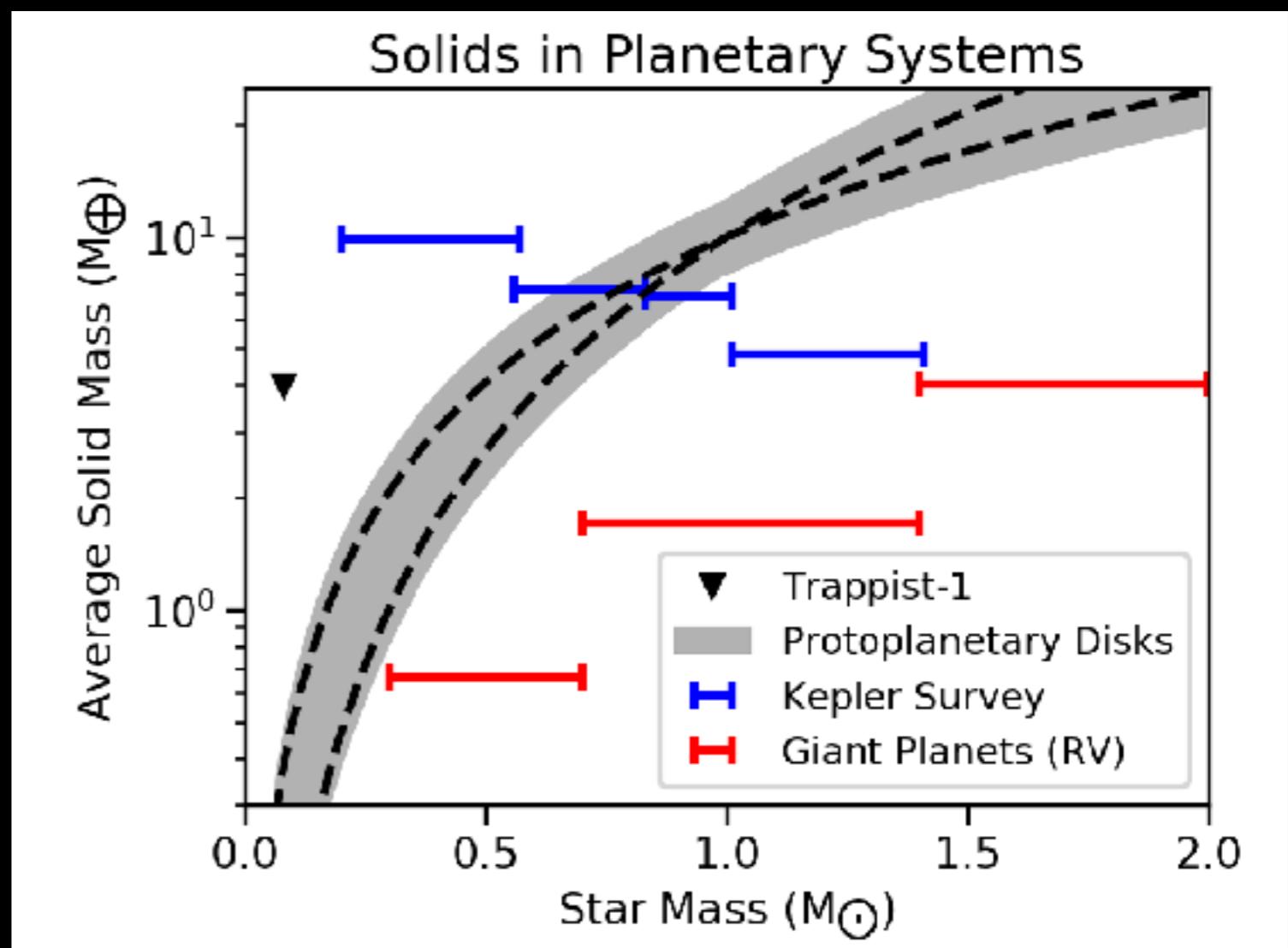


Mdisk-Mstar correlation ($M_d \sim M_{\star}^{1.6}$) — but lots of scatter



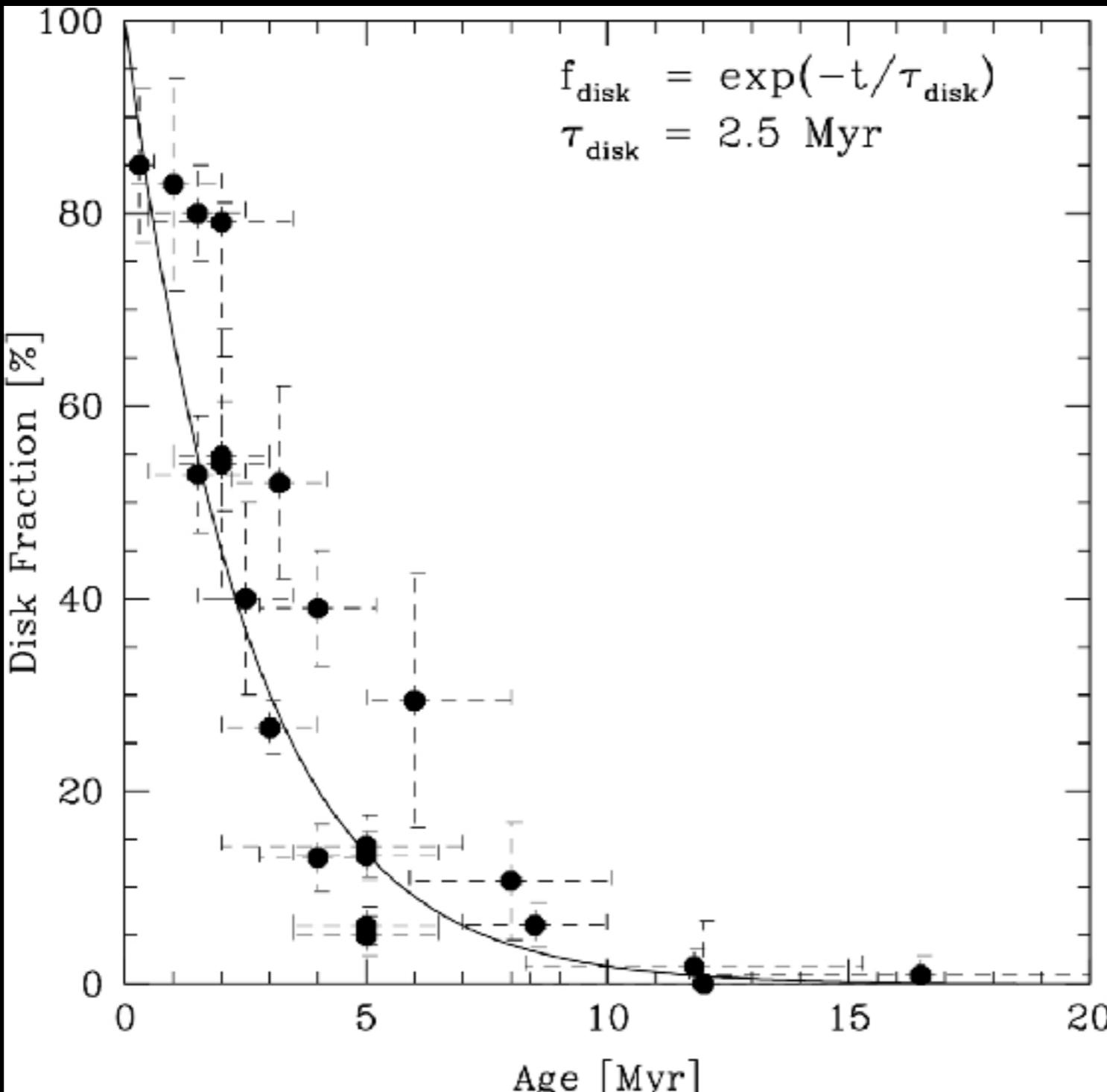
Are disk masses underestimated?

Disk masses appear too small to explain the masses in observed planetary systems

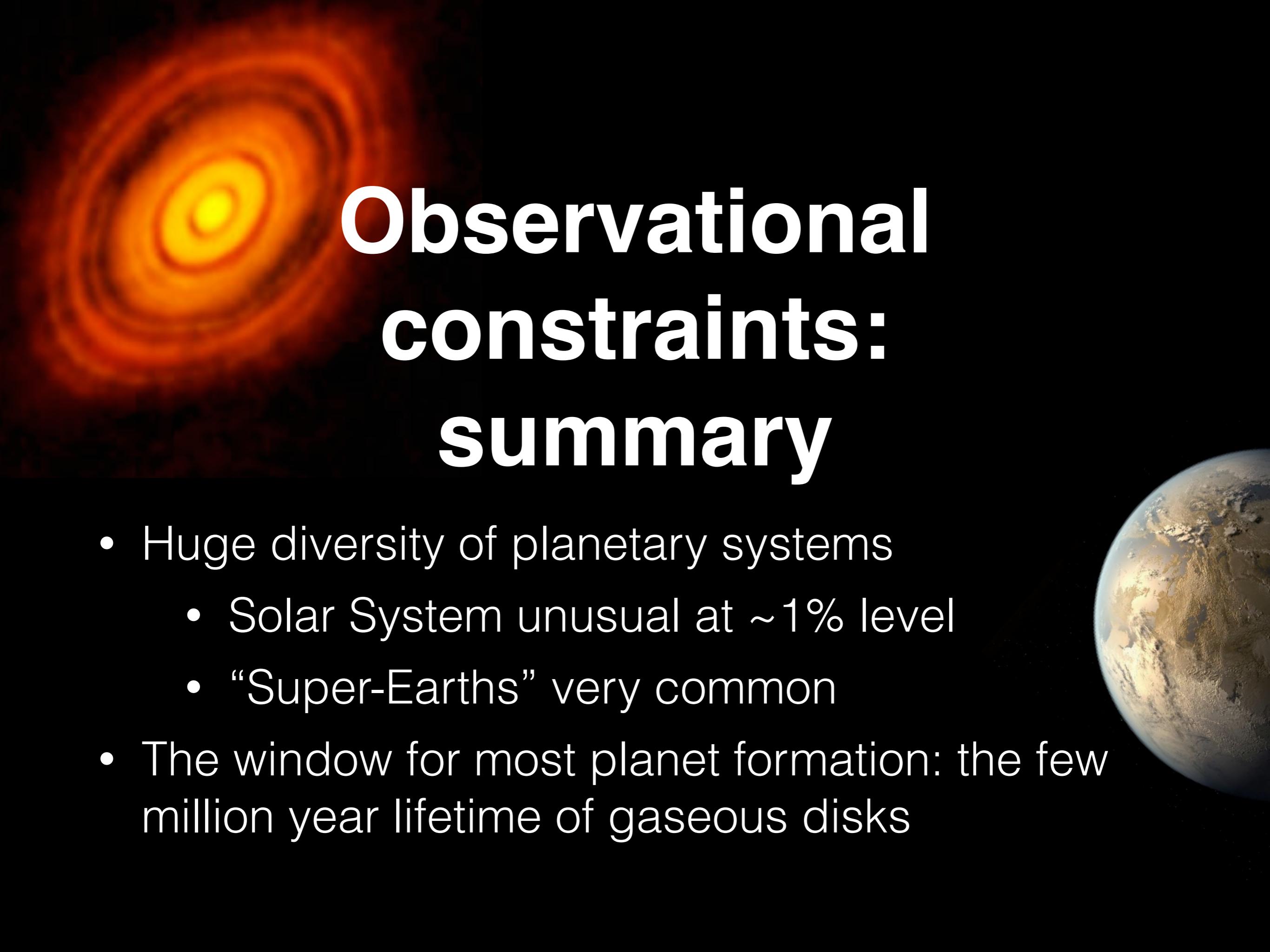


Mulders (2018)

Gas disks (inferred from hot dust) dissipate on a few Myr timescale



Mamajek 2009

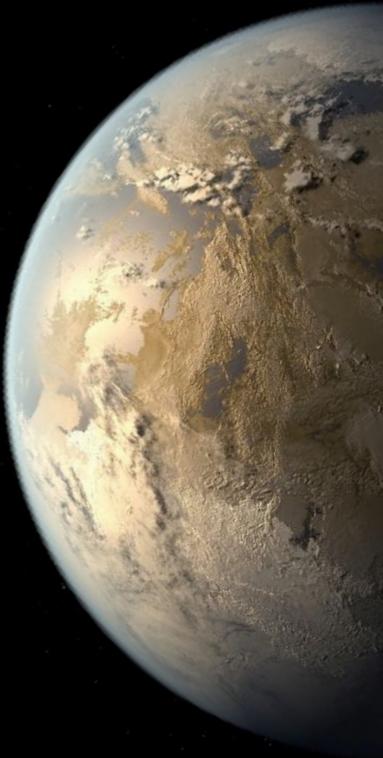


Observational constraints: summary

- Huge diversity of planetary systems
 - Solar System unusual at ~1% level
 - “Super-Earths” very common
- The window for most planet formation: the few million year lifetime of gaseous disks



2. Stages of planet formation

- planetesimal formation
 - pebble/planetesimal accretion
 - orbital migration
 - giant impacts
 - gas accretion
 - giant planet scattering
- 

Planet formation: the cast of characters

pebbles:
~1mm-10cm

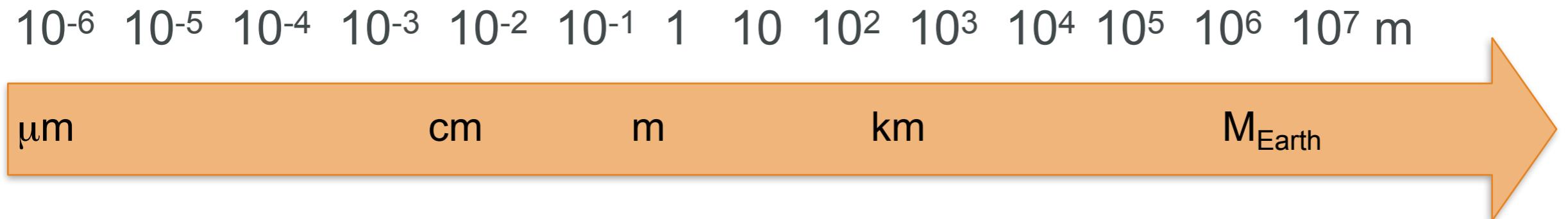


planetesimals:
~10-1000km

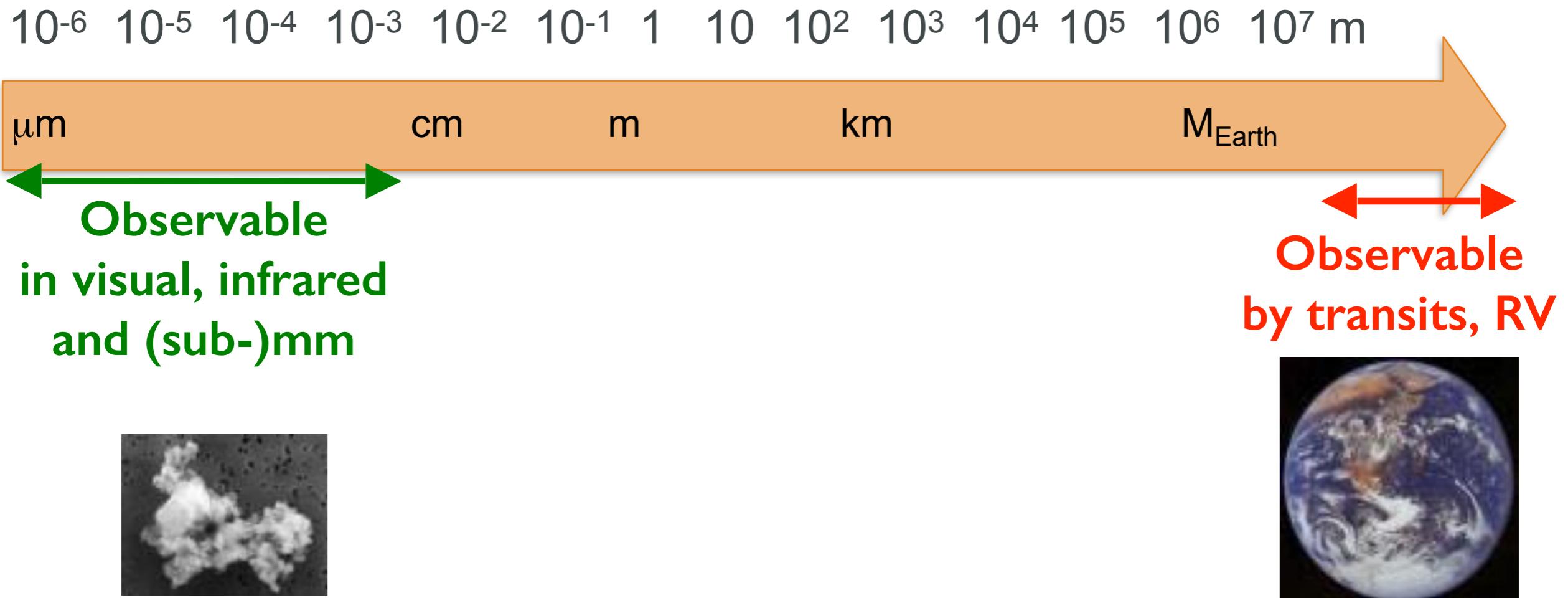


*terrestrial planetary
embryos (=protoplanets):*
~Moon-sized or larger

Physics of growth between μm and 10^4 km



Physics of growth between μm and 10^4 km



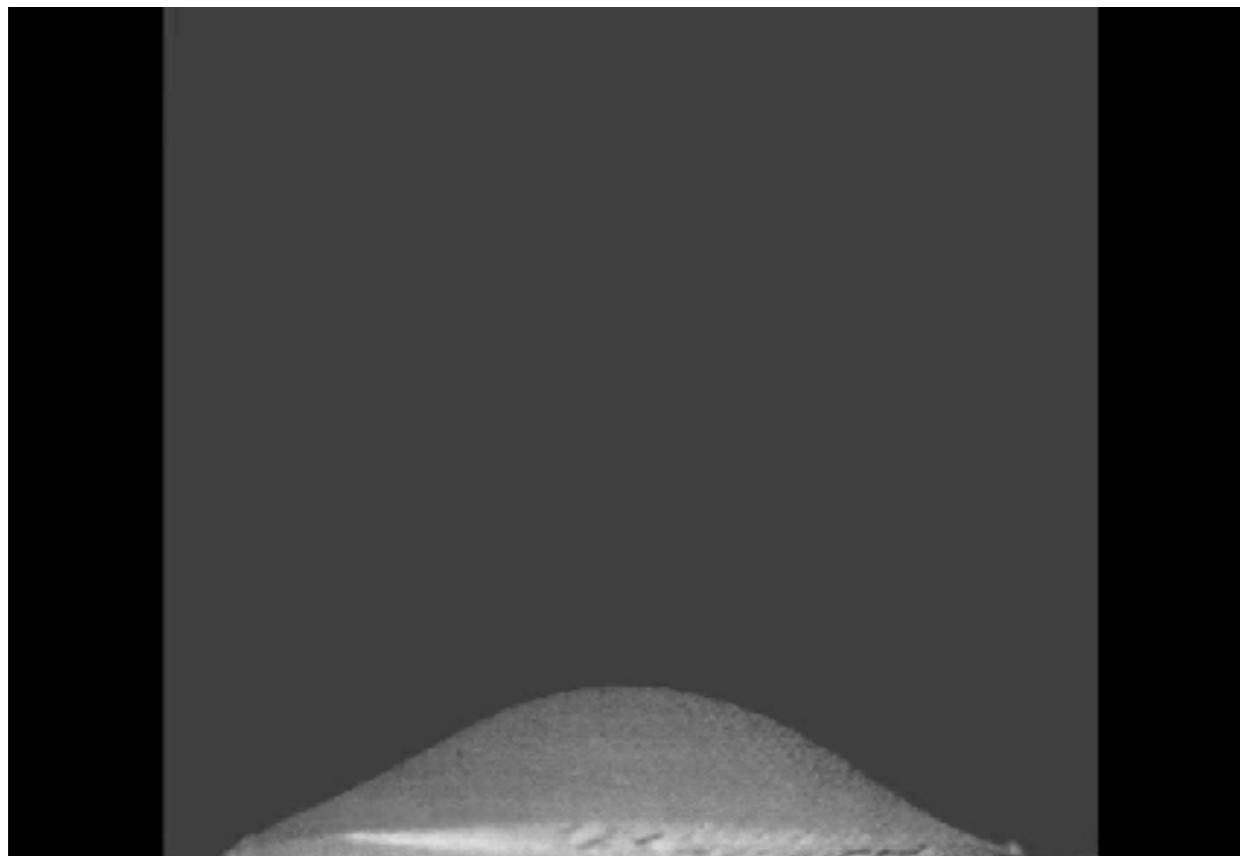
Physics of growth between μm and 10^4 km

$10^{-6} \ 10^{-5} \ 10^{-4} \ 10^{-3} \ 10^{-2} \ 10^{-1} \ 1 \ 10 \ 10^2 \ 10^3 \ 10^4 \ 10^5 \ 10^6 \ 10^7 \text{ m}$

μm cm m km M_{Earth}

Collisions lead
to growth (silicates)

Collisions lead to
bouncing / fragmentation



Blum & Wurm (2008)

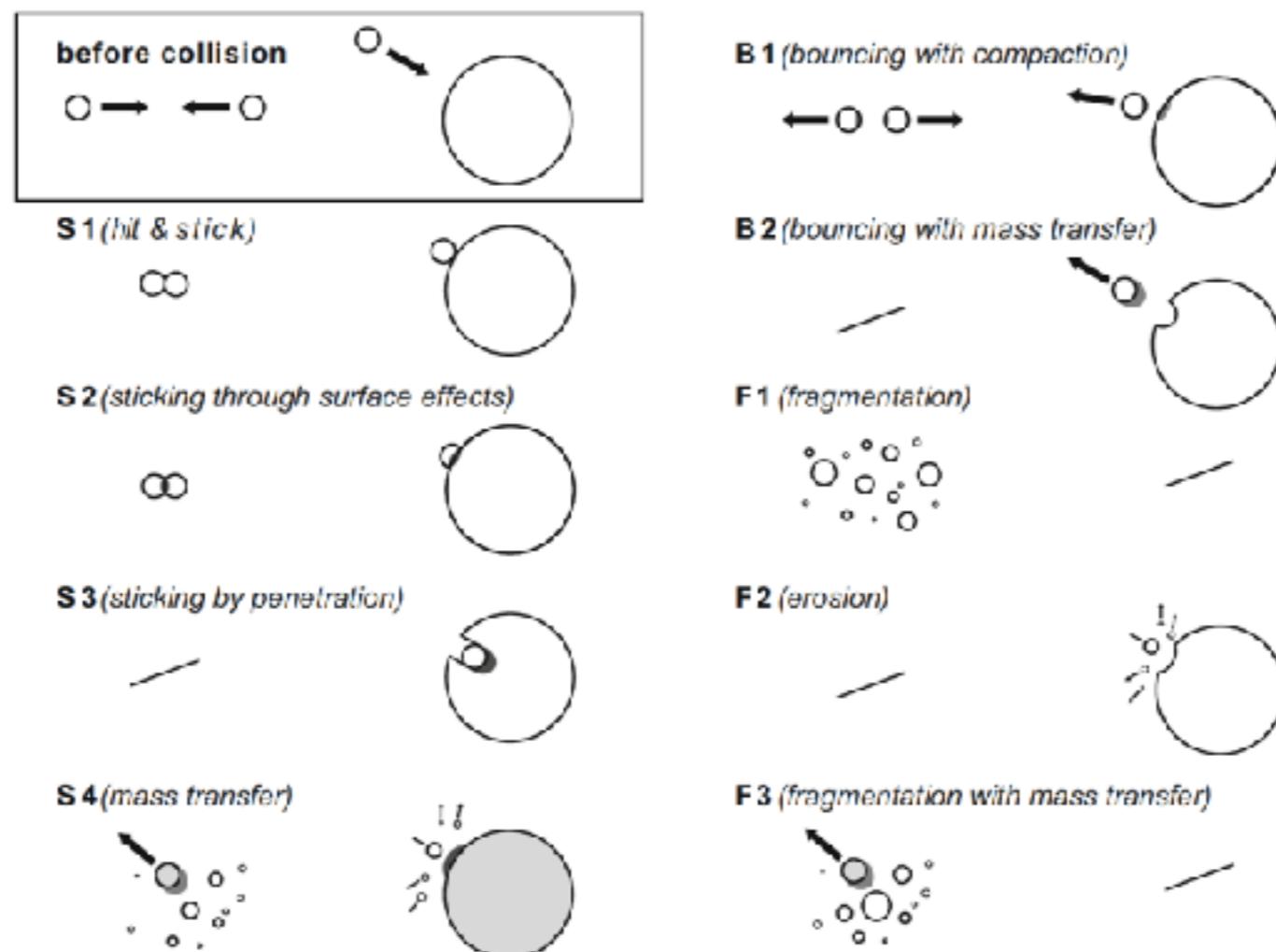
Physics of growth between μm and 10^4 km

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μm cm m km M_{Earth}

Collisions lead to growth (silicates)

Collisions lead to bouncing / fragmentation



Guttler et al (2010)

Physics of growth between μm and 10^4 km

$10^{-6} \ 10^{-5} \ 10^{-4} \ 10^{-3} \ 10^{-2} \ 10^{-1} \ 1 \ 10 \ 10^2 \ 10^3 \ 10^4 \ 10^5 \ 10^6 \ 10^7 \text{ m}$

μm cm m km M_{Earth}

Collisions lead
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Collisions lead to
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rapid inspiral ($\sim 10^3 \text{ yr}$)
due to aerodynamic drag

Physics of growth between μm and 10^4 km

$10^{-6} \ 10^{-5} \ 10^{-4} \ 10^{-3} \ 10^{-2} \ 10^{-1} \ 1 \ 10 \ 10^2 \ 10^3 \ 10^4 \ 10^5 \ 10^6 \ 10^7 \text{ m}$

μm cm m km M_{Earth}

collisions lead
to growth (silicates)

collisions lead to
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rapid inspiral ($\sim 10^3 \text{ yr}$)
due to aerodynamic drag

strength of bodies
set by material properties

strength set
by self-gravity

Physics of growth between μm and 10^4 km

$10^{-6} \ 10^{-5} \ 10^{-4} \ 10^{-3} \ 10^{-2} \ 10^{-1} \ 1 \ 10 \ 10^2 \ 10^3 \ 10^4 \ 10^5 \ 10^6 \ 10^7 \text{ m}$

μm cm m km M_{Earth}

collisions lead
to growth (silicates)

collisions lead to
bouncing / fragmentation

rapid inspiral ($\sim 10^3 \text{ yr}$)
due to aerodynamic drag

strength of bodies
set by material properties

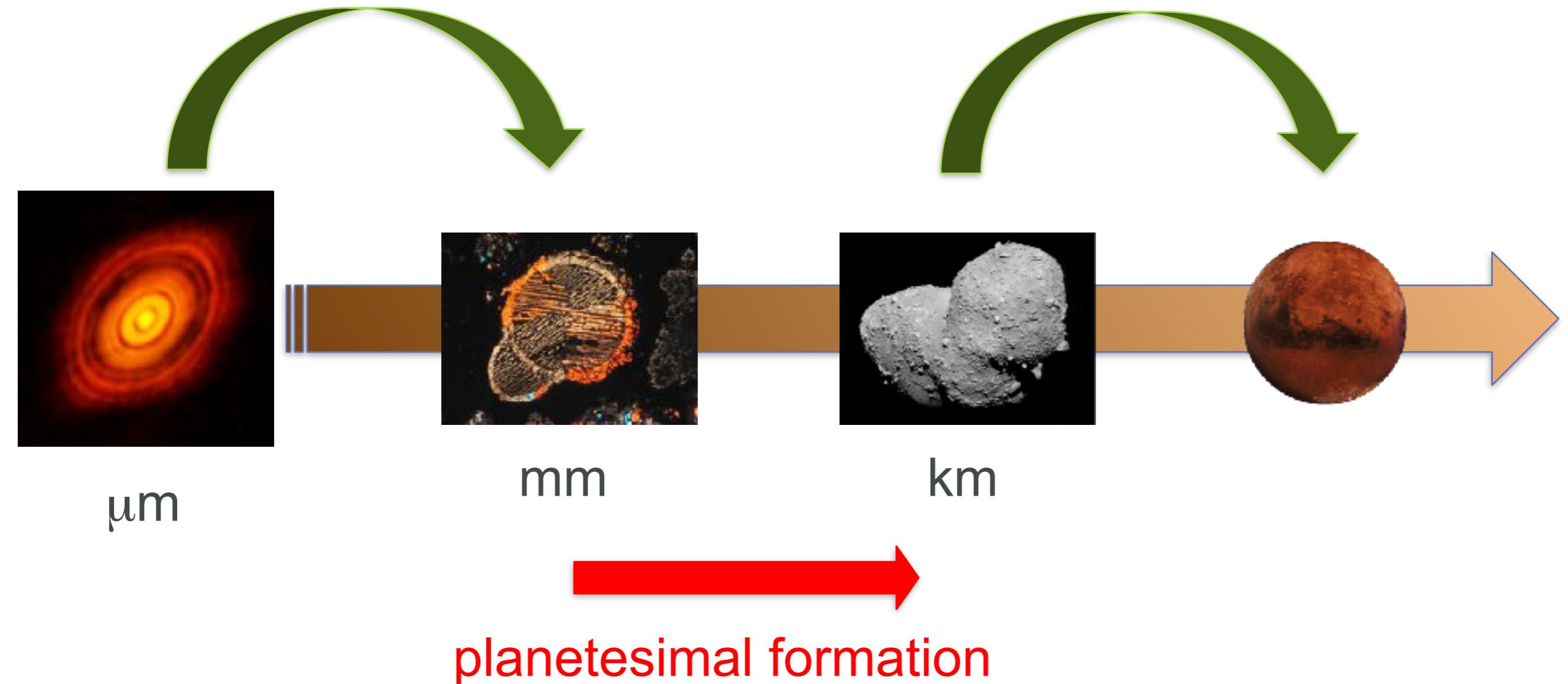
strength set
by self-gravity

gas disk
migration

Forming the first planetesimals

aerodynamic &
material forces

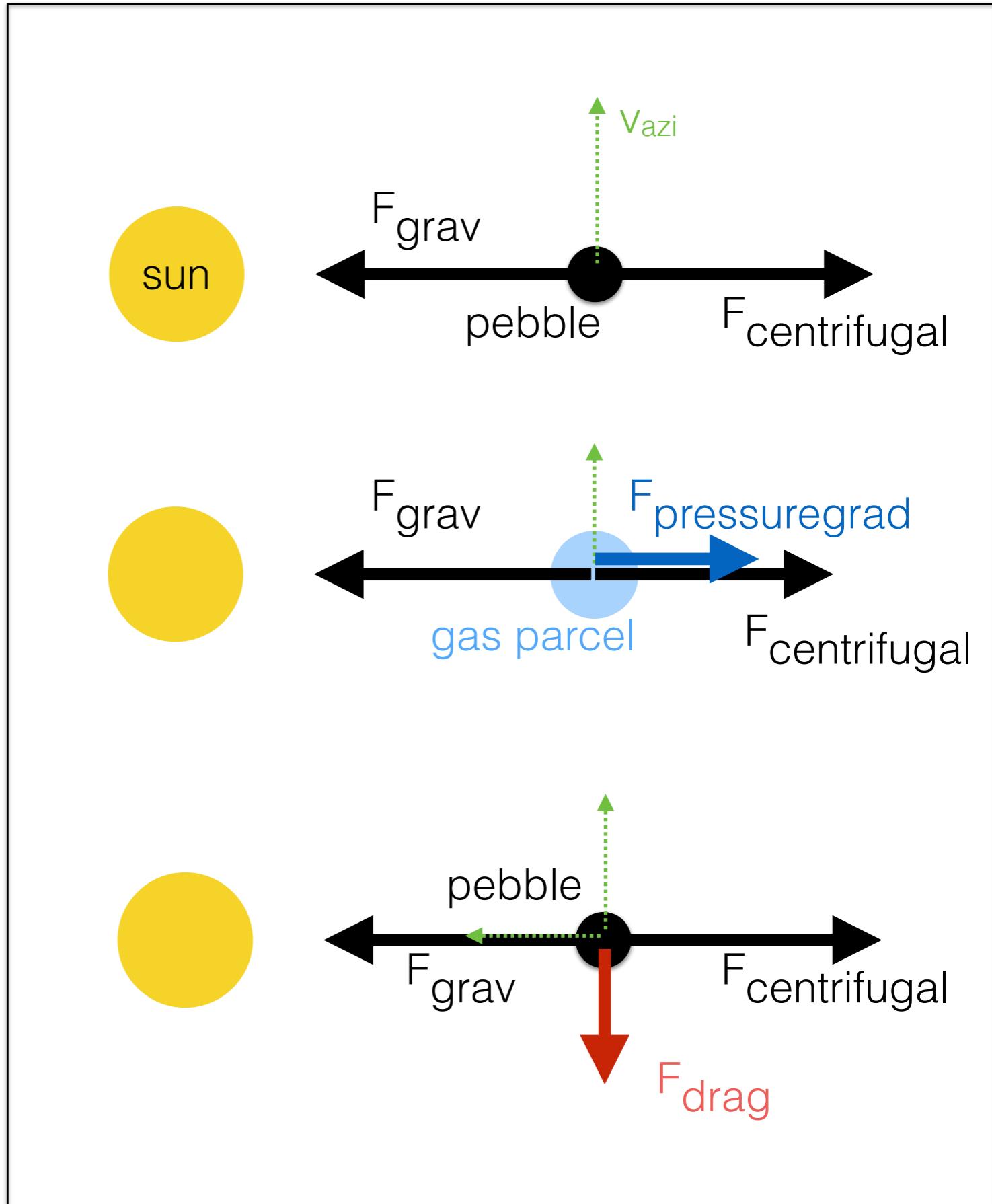
gravity



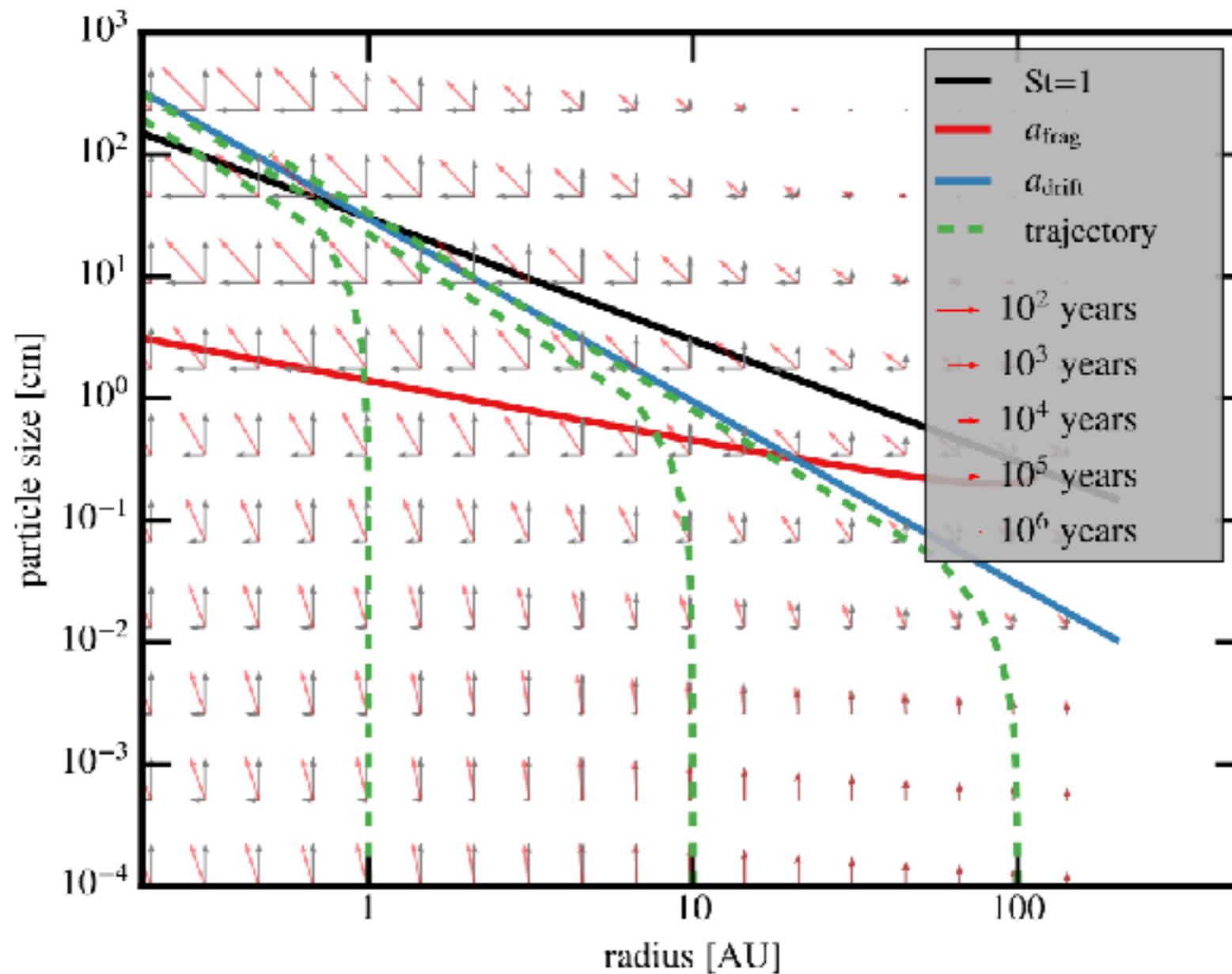
(ii) Particle drift

- pressure support on the gas reduces the orbital velocity of the gas
- particles feel a **headwind**
- gas drag forces the particles to drift inwards

$$a_{\text{drag}} = - \frac{v_p - u_g}{t_f}$$



Growth and inward drift of dust



Birnstiel et al (2016)

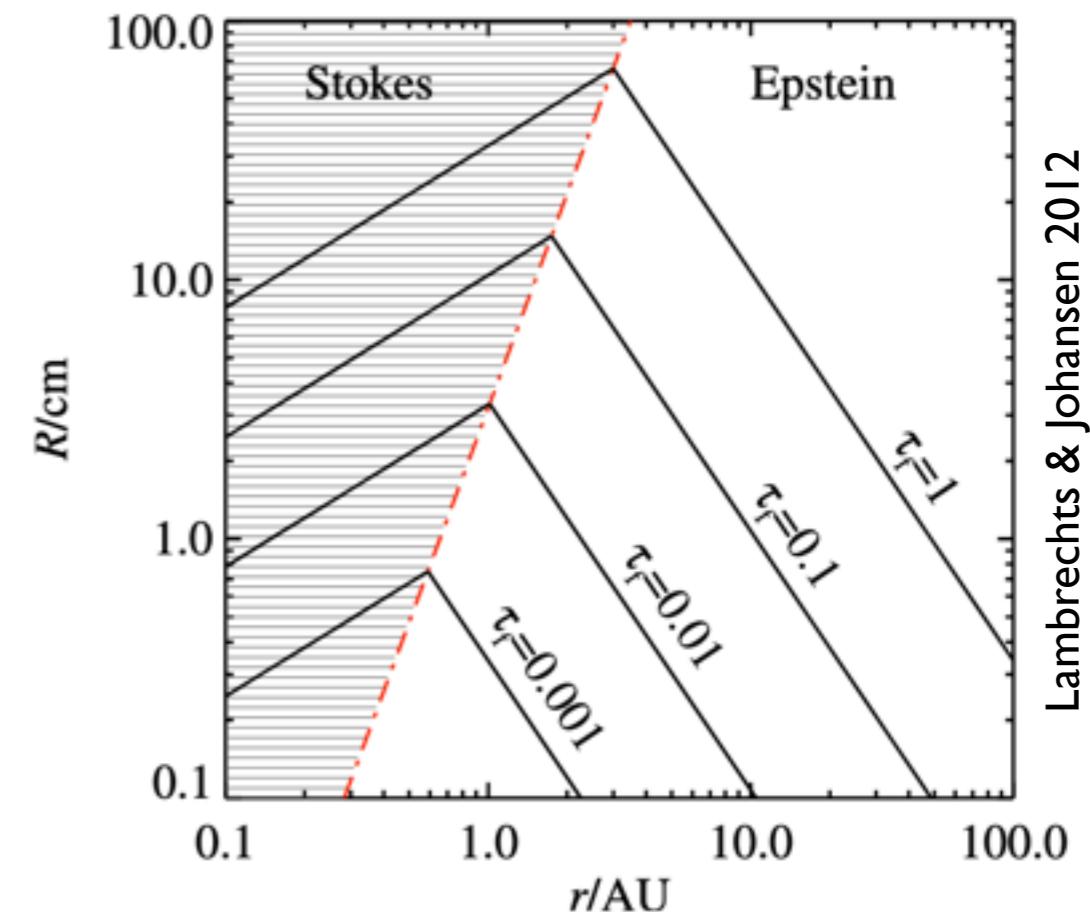
The Stokes number

- Stokes number = the stopping time (due to gas drag) / the orbital timescale

$$St = \frac{a \rho_s \pi}{\Sigma_g} \frac{2}{\tau}$$

Annotations:

- dust monomer size (points to a)
- dust monomer density (points to ρ_s)
- gas disk surface density (points to Σ_g)



Fastest drifting particle (“pebbles”) are where $St=1$

(“ $St = one$ ”), or “stones” — Aurelien Crida

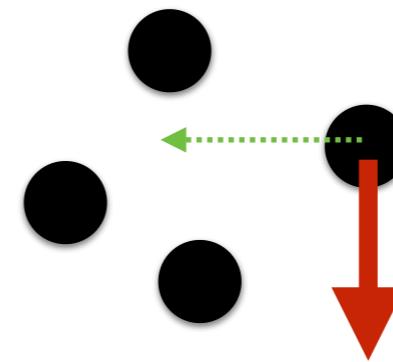
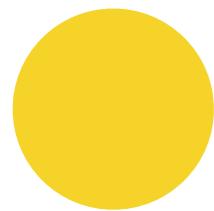
Streaming instability simplified

Youdin and Goodman, 2005, Johansen et al 2007, Bai and Stone, 2010, Kowalik et al 2013, Yang and Johansen 2016, Lambrechts et al, 2016



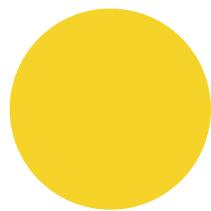
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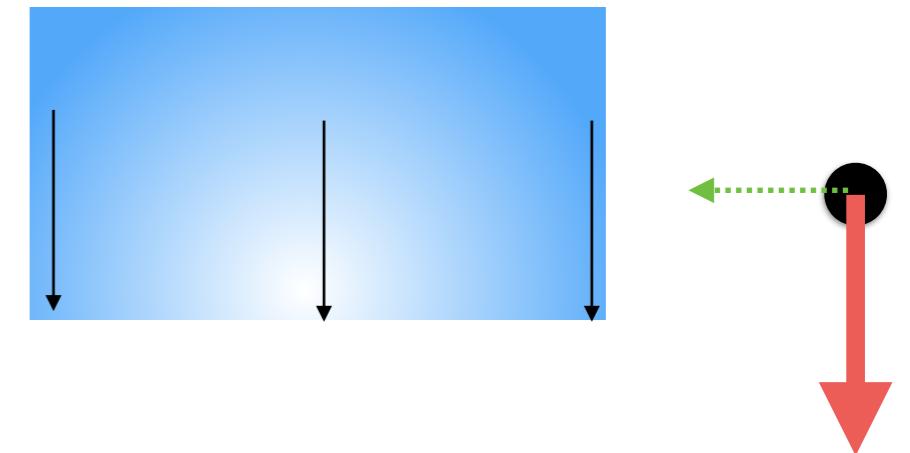
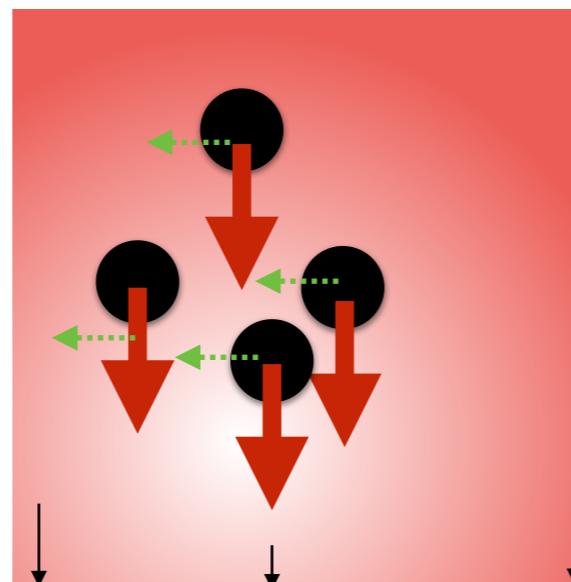


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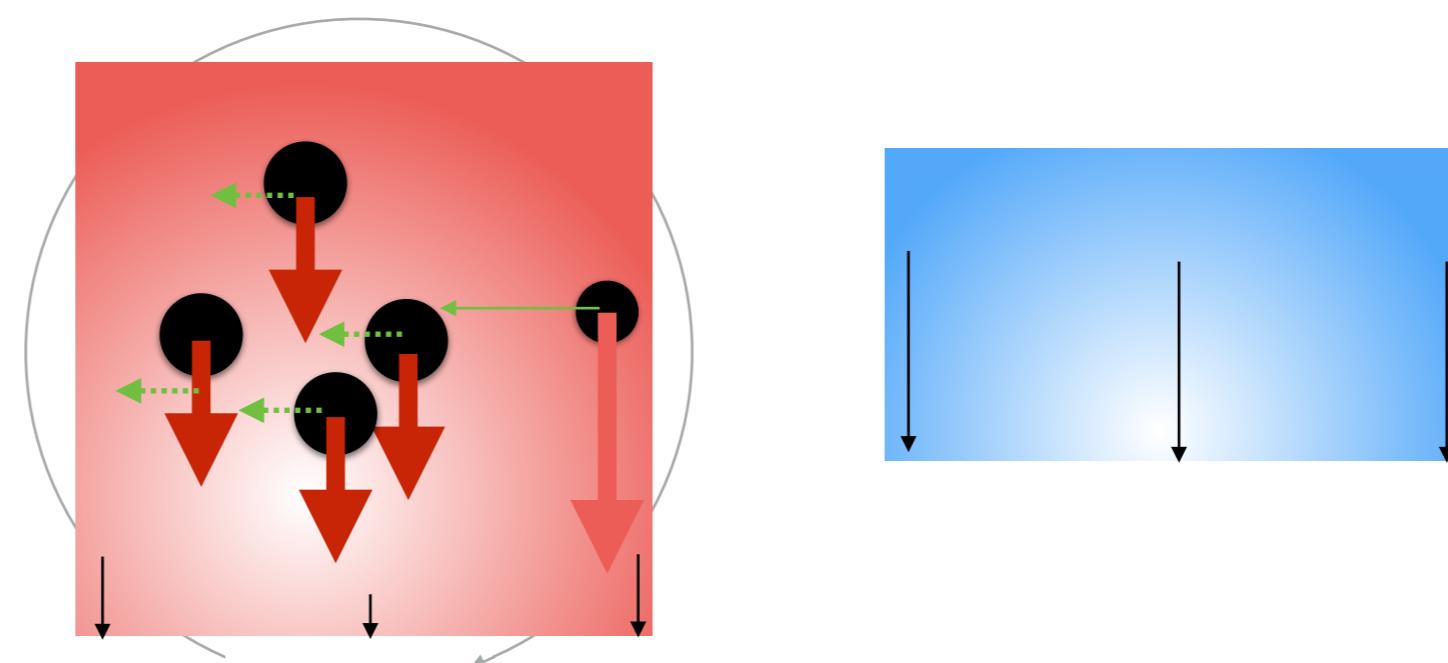
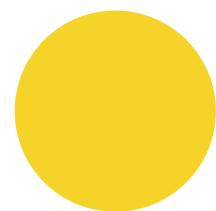


$$\rho_p / \rho_g \sim 1$$



Streaming instability simplified

Youdin and Goodman, 2005, Johansen et al 2007, Bai and Stone, 2010, Kowalik et al 2013, Yang and Johansen 2016, Lambrechts et al, 2016



- **Streaming instability** leads to local clustering
- gravitational collapse of overdensities to km+ scale planetesimals

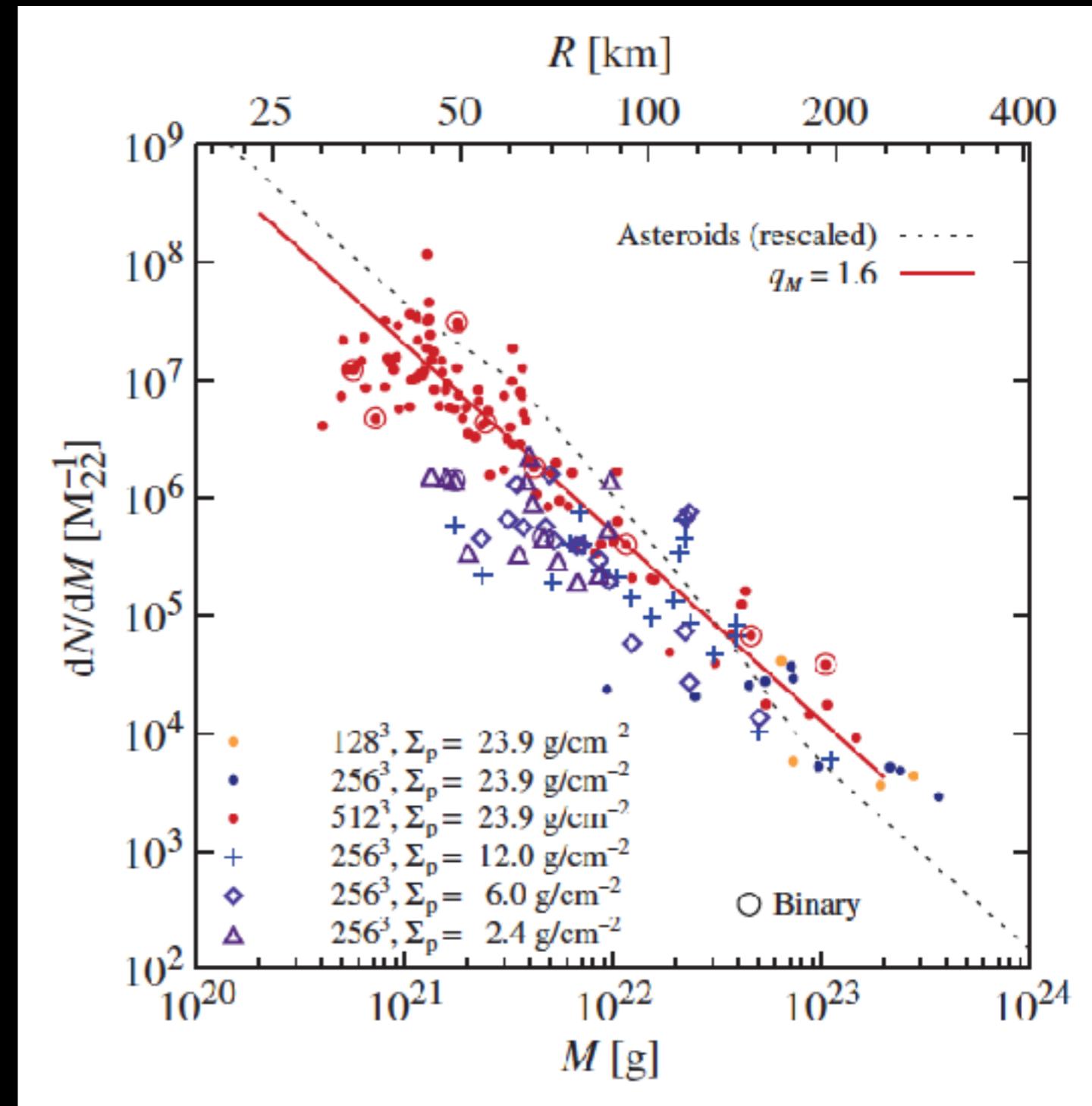


CALIFORNIA
ACADEMY OF
SCIENCES

Simulations: Jake Simon, Zhaoquan Zhu

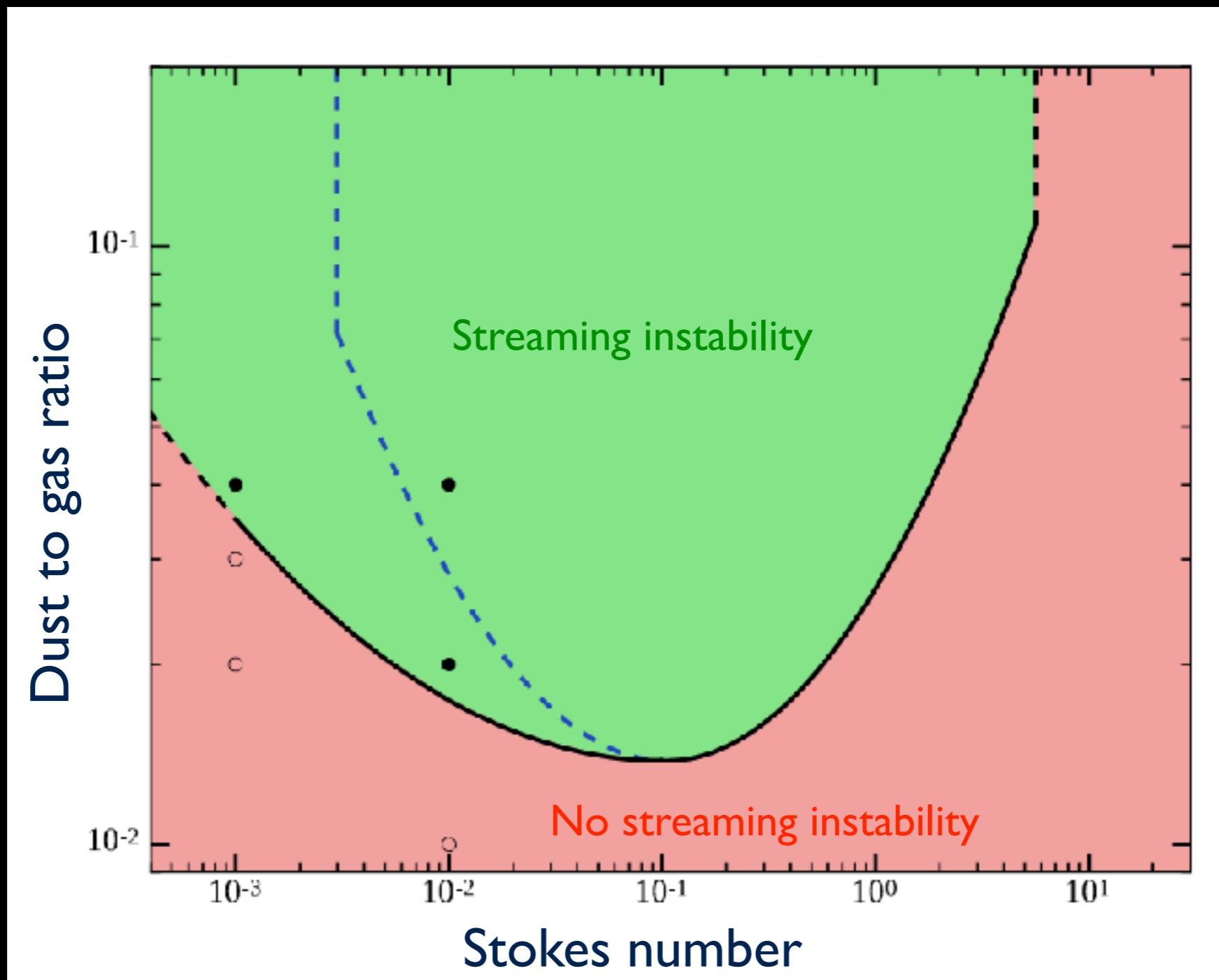
Streaming Instability

- Forms planetesimals up to $R \sim 300\text{km}$
- Characteristic birth size distribution similar to asteroids

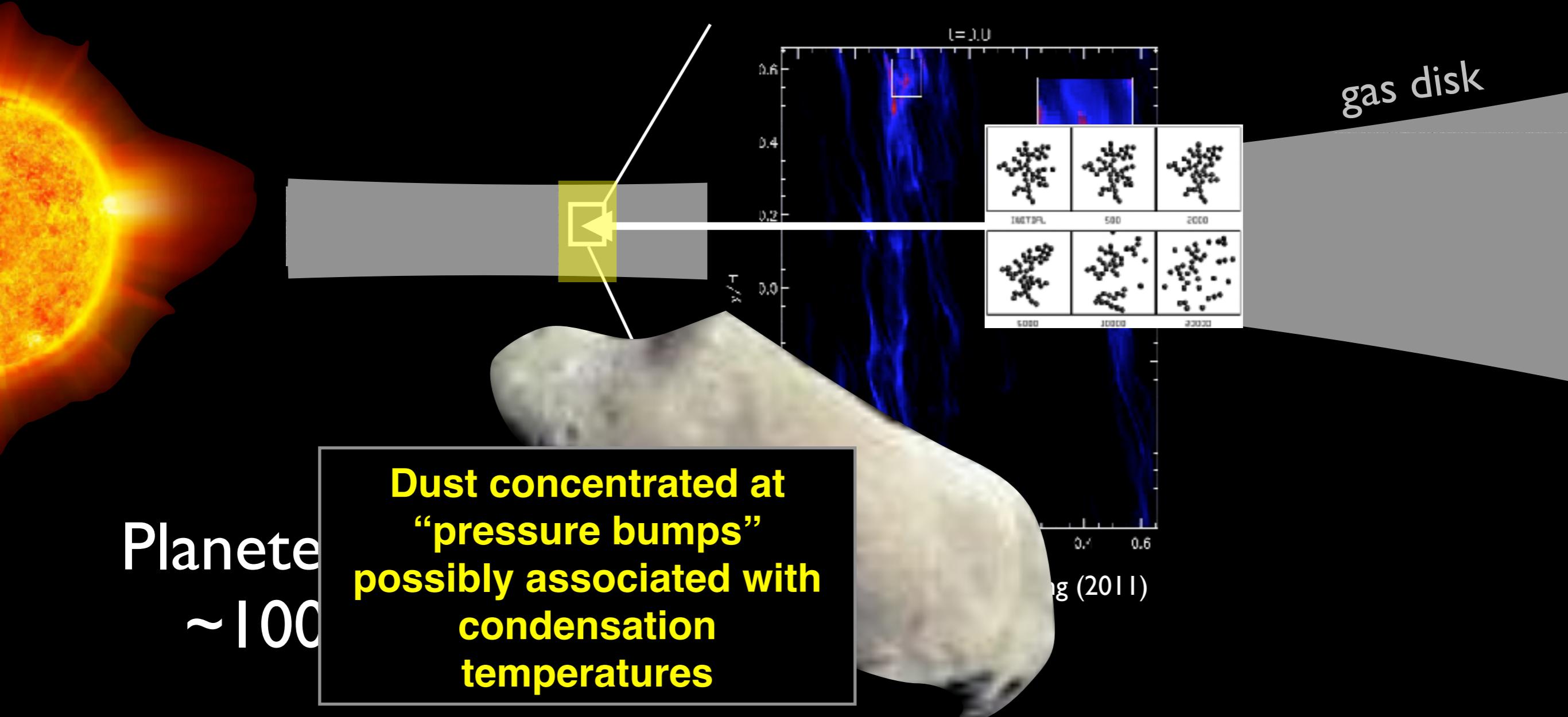


Johansen et al (2015); also Simon et al (2016)

The streaming instability requires an enhancement in the dust-to-gas ratio



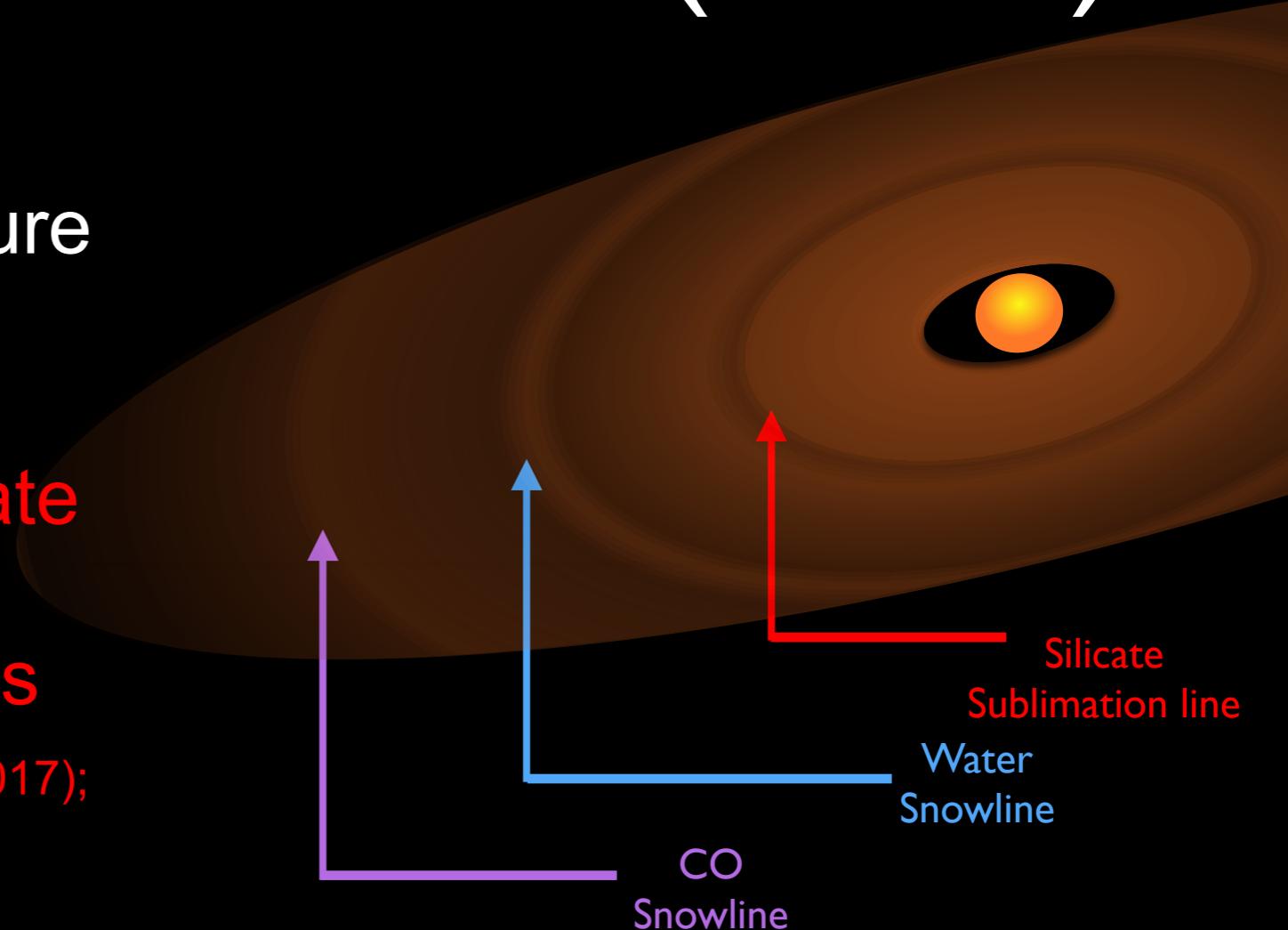
Planetesimal formation models: dust growth/drift with disk evolution



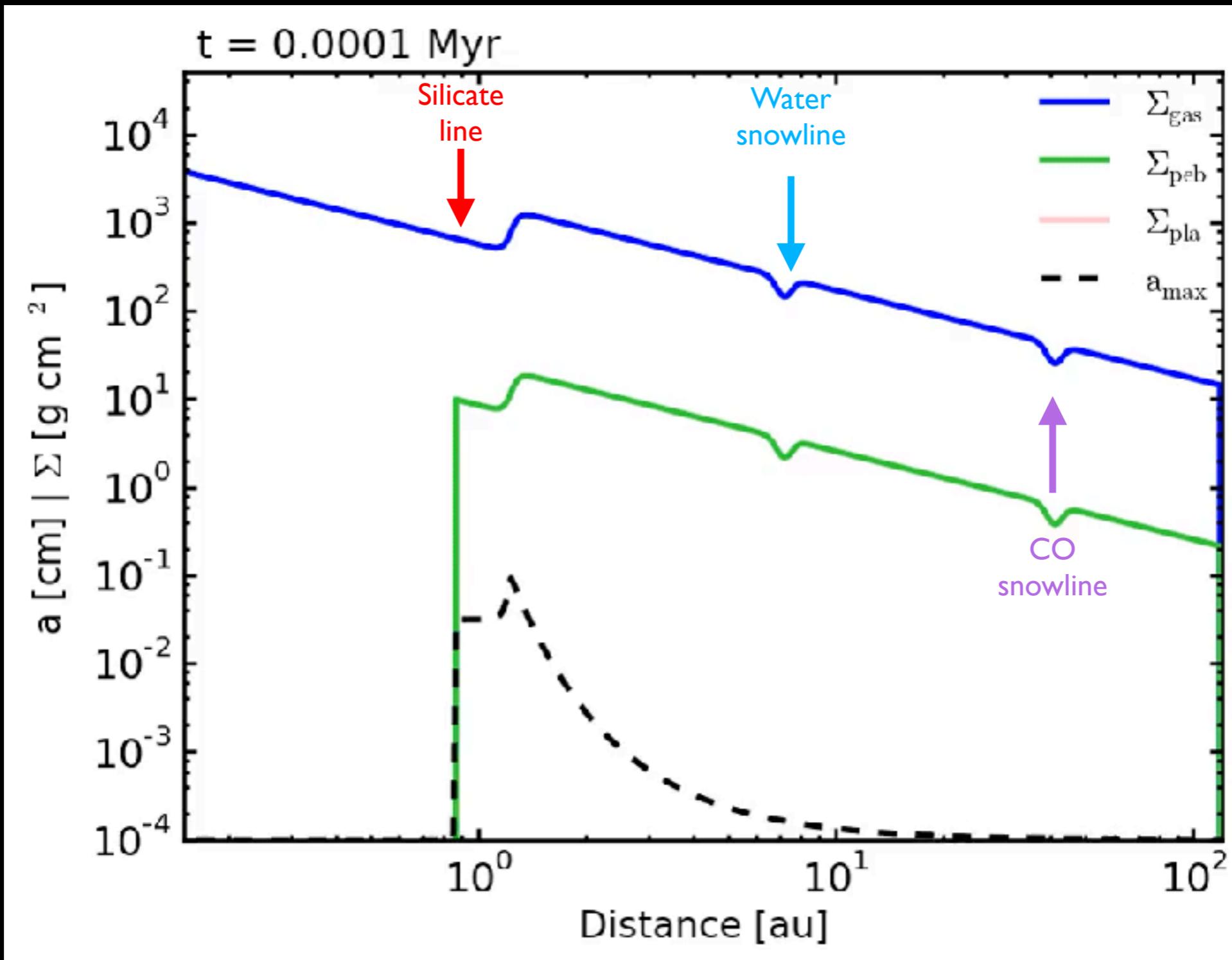
Model of Izidoro et al (2022)

Planetesimal formation in a gaseous disk assuming pressure bumps (traps)

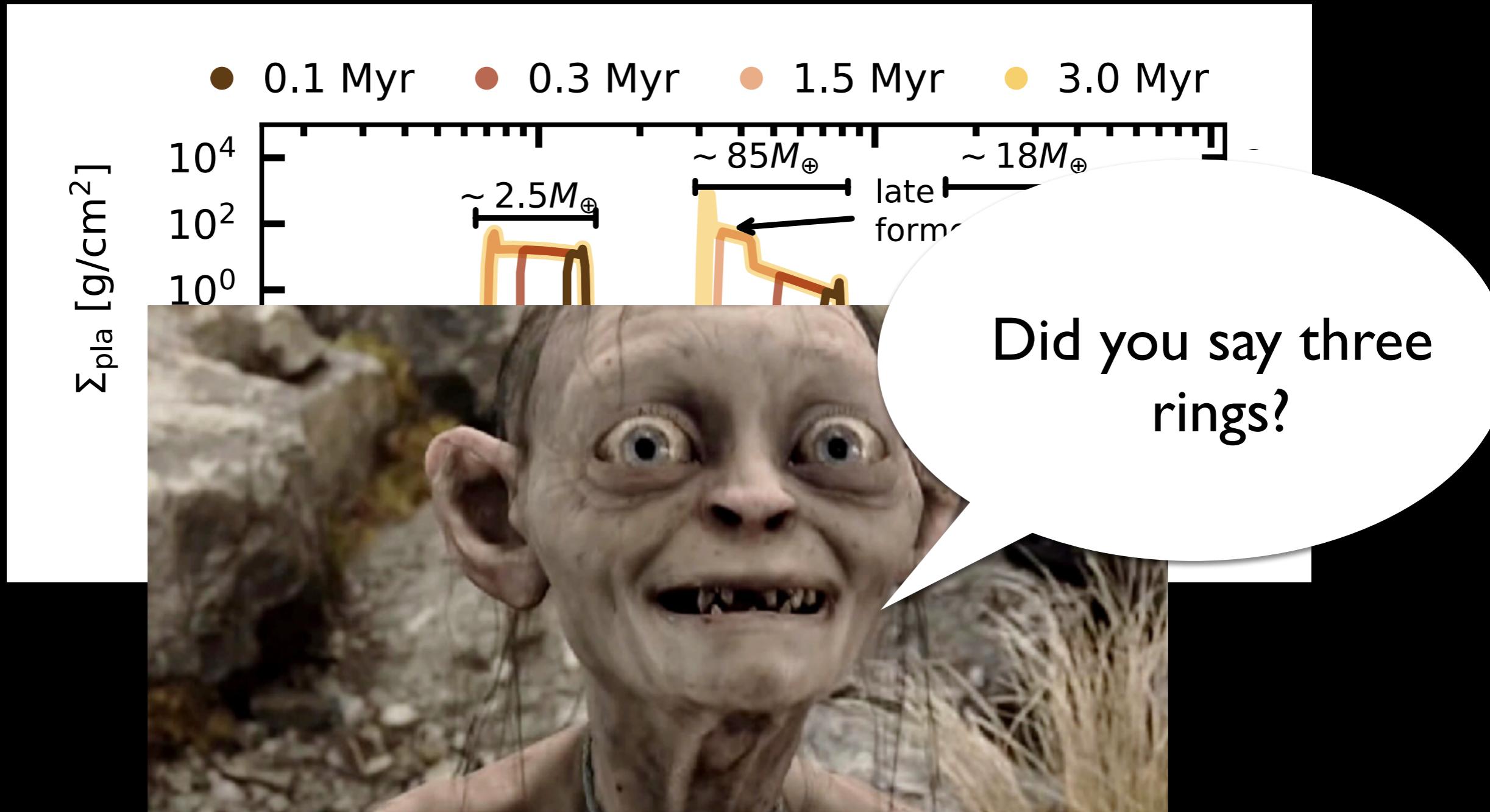
- 1) at $T \sim 1400$ K, near the silicate sublimation line due to thermal ionization of the gas disk (Desch & Turner 2015; Flock et al 2017);
- 2) at $T \sim 170$ K, the water snowline (Muller et al 2021, Charnoz et al 2021);
- 3) at $T \sim 30$ K, the CO-snowline (Qi et al 13, Flock et al 2015, Vanthoff et al 2017, Bosman & Banzatti 2019, Vericel & Gonzalez 20)



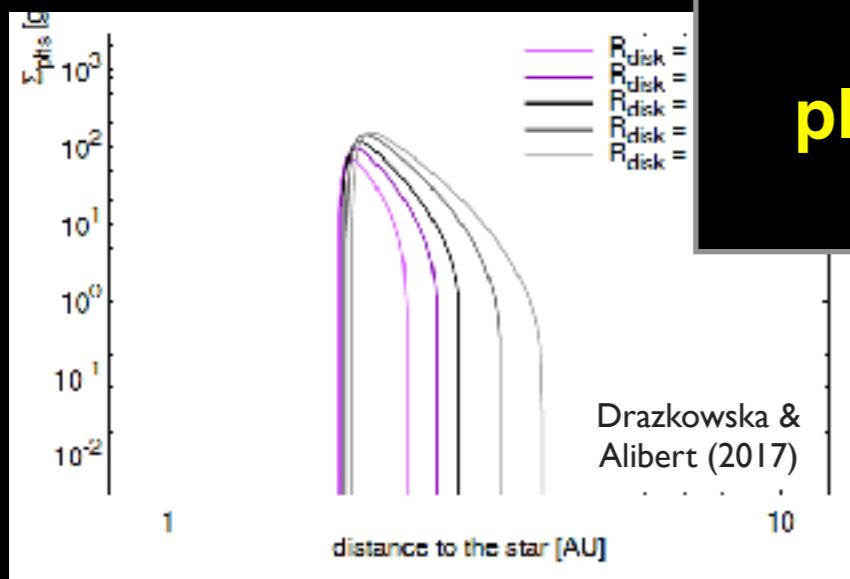
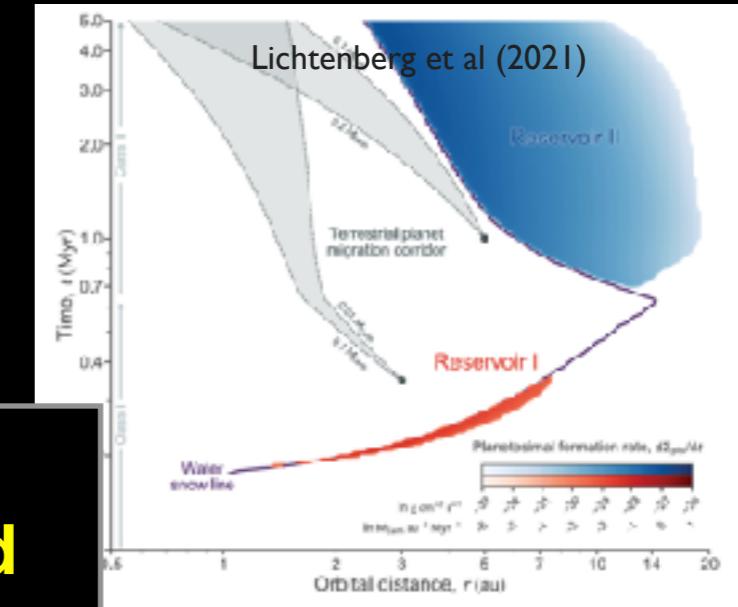
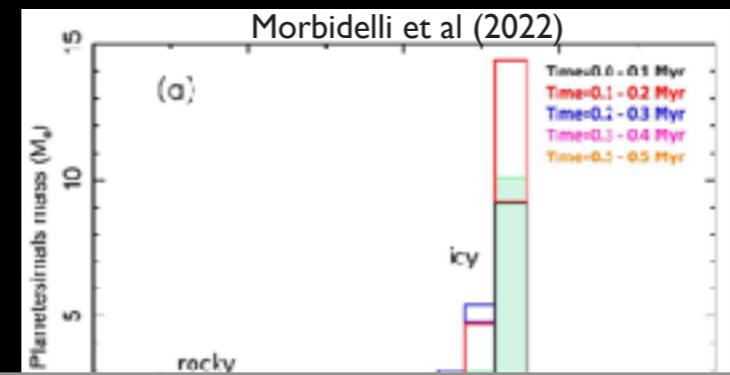
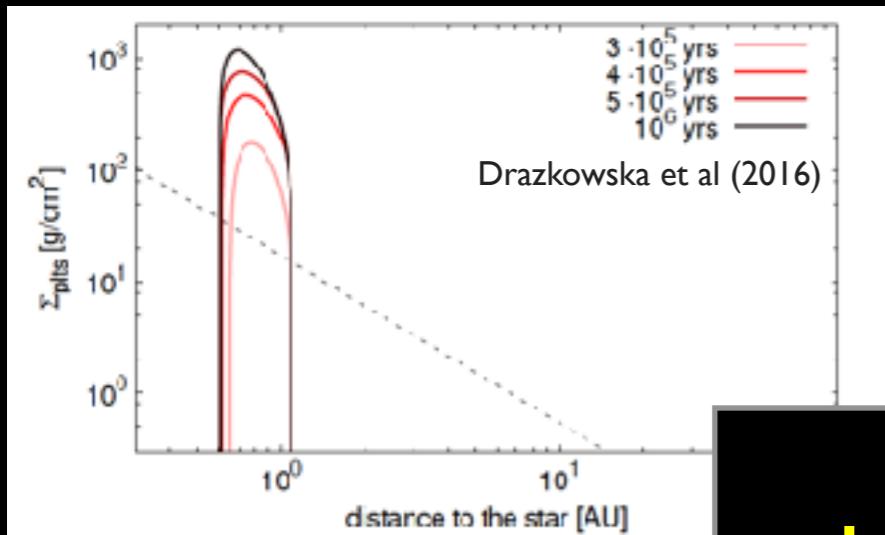
A model with dust coagulation/drift and three “pressure bumps”



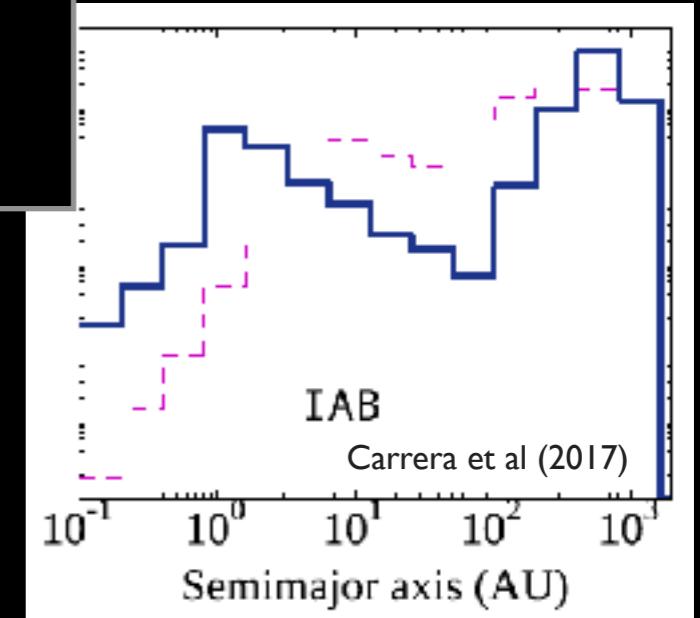
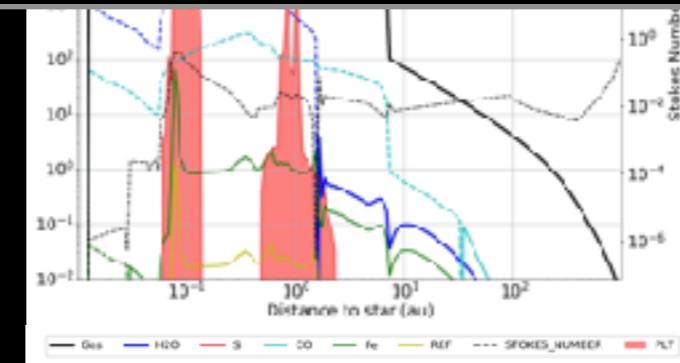
Three rings of planetesimals



Planetesimal formation models: dust growth/drift with disk evolution

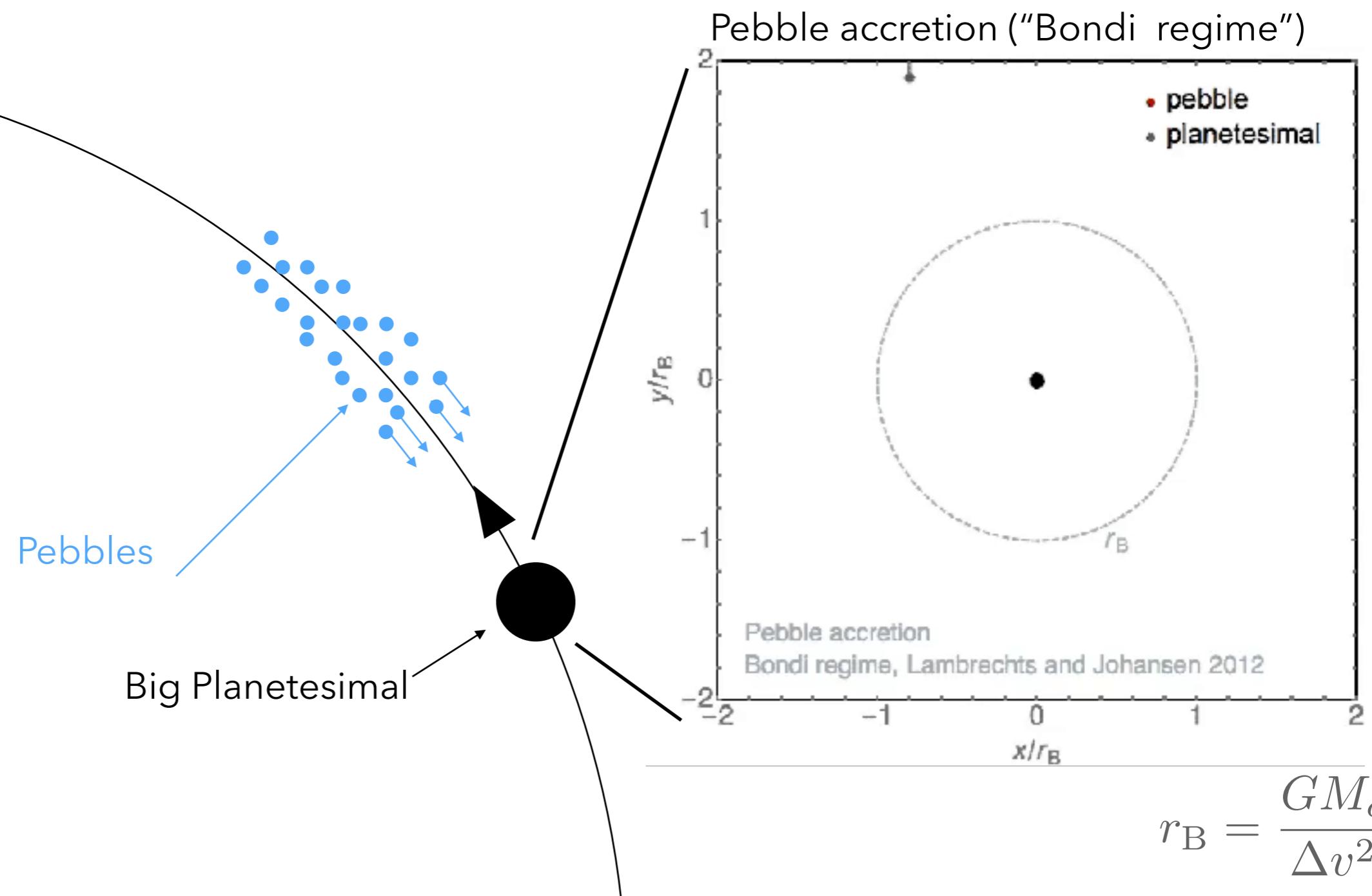


**General agreement that
planetesimal formation is linked
with condensation lines:
planetesimals probably form in
rings, not disks**

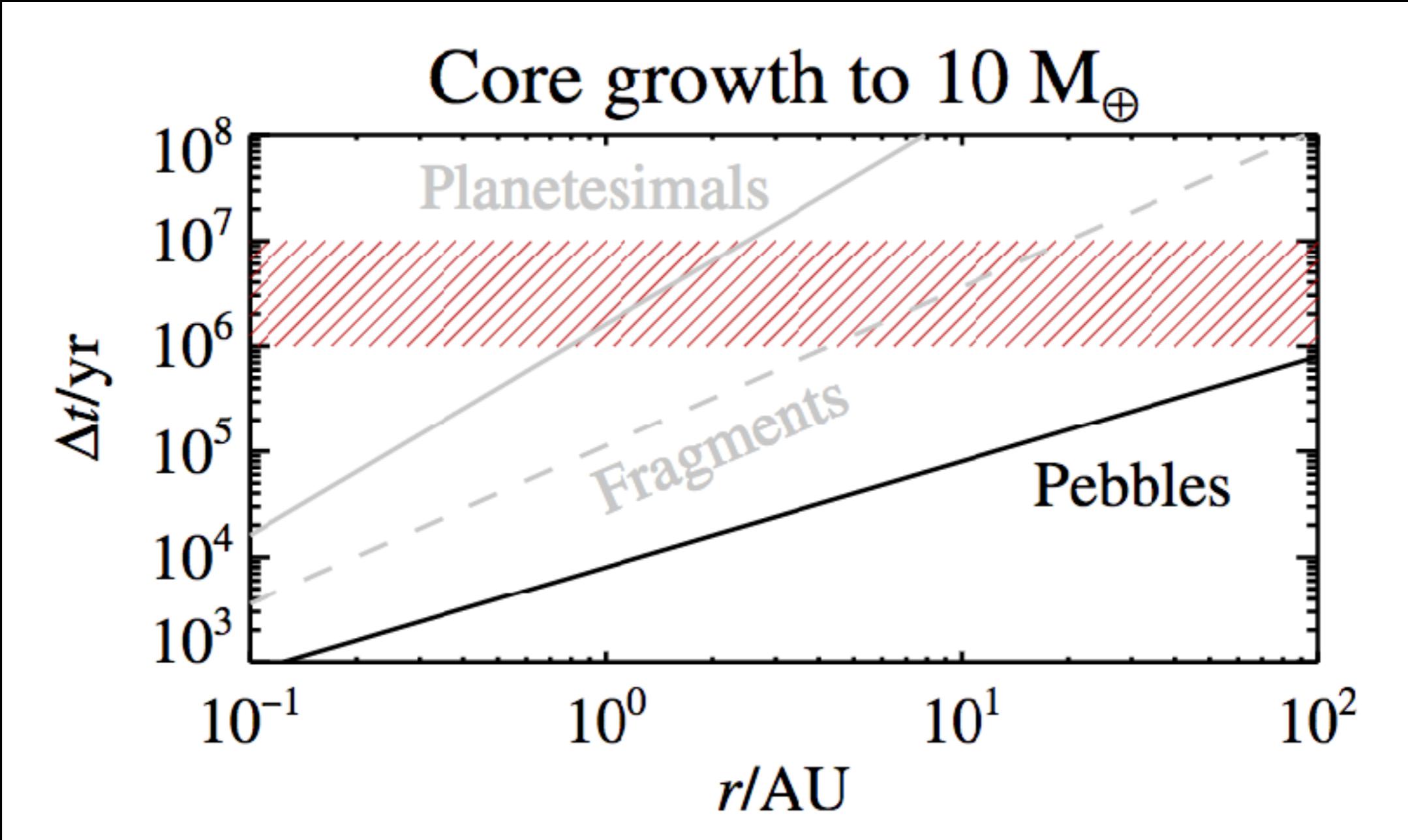


Pebble accretion

Lambrechts & Johansen, 2012



Pebble accretion is key for forming giant planet cores

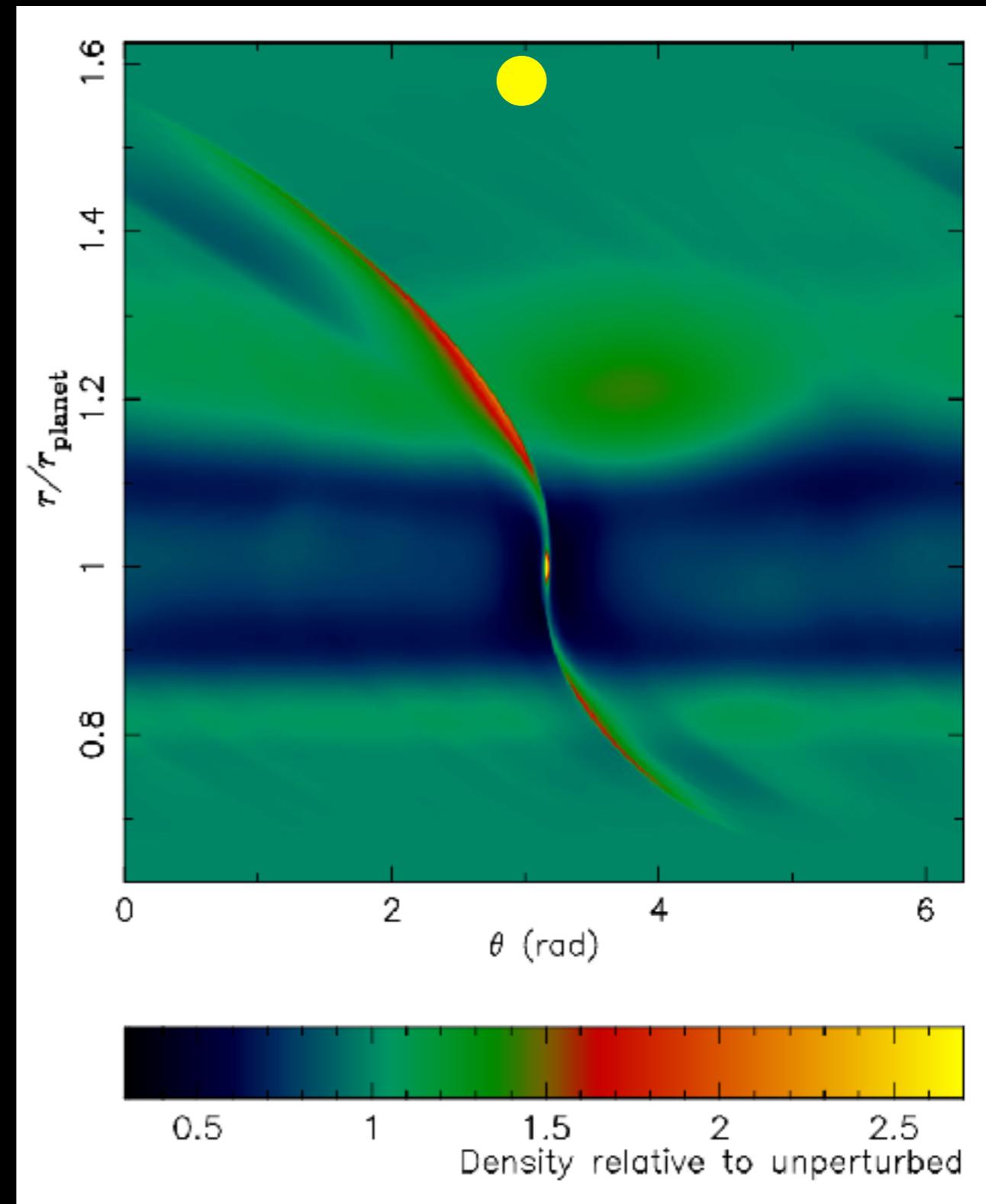


Lambrechts & Johansen (2012)

Pebble accretion is self-limiting

Above “pebble isolation mass”, a planet creates an exterior pressure bump that traps pebbles

($\sim 20 M_E$ for typical disk at Jup’s orbit)

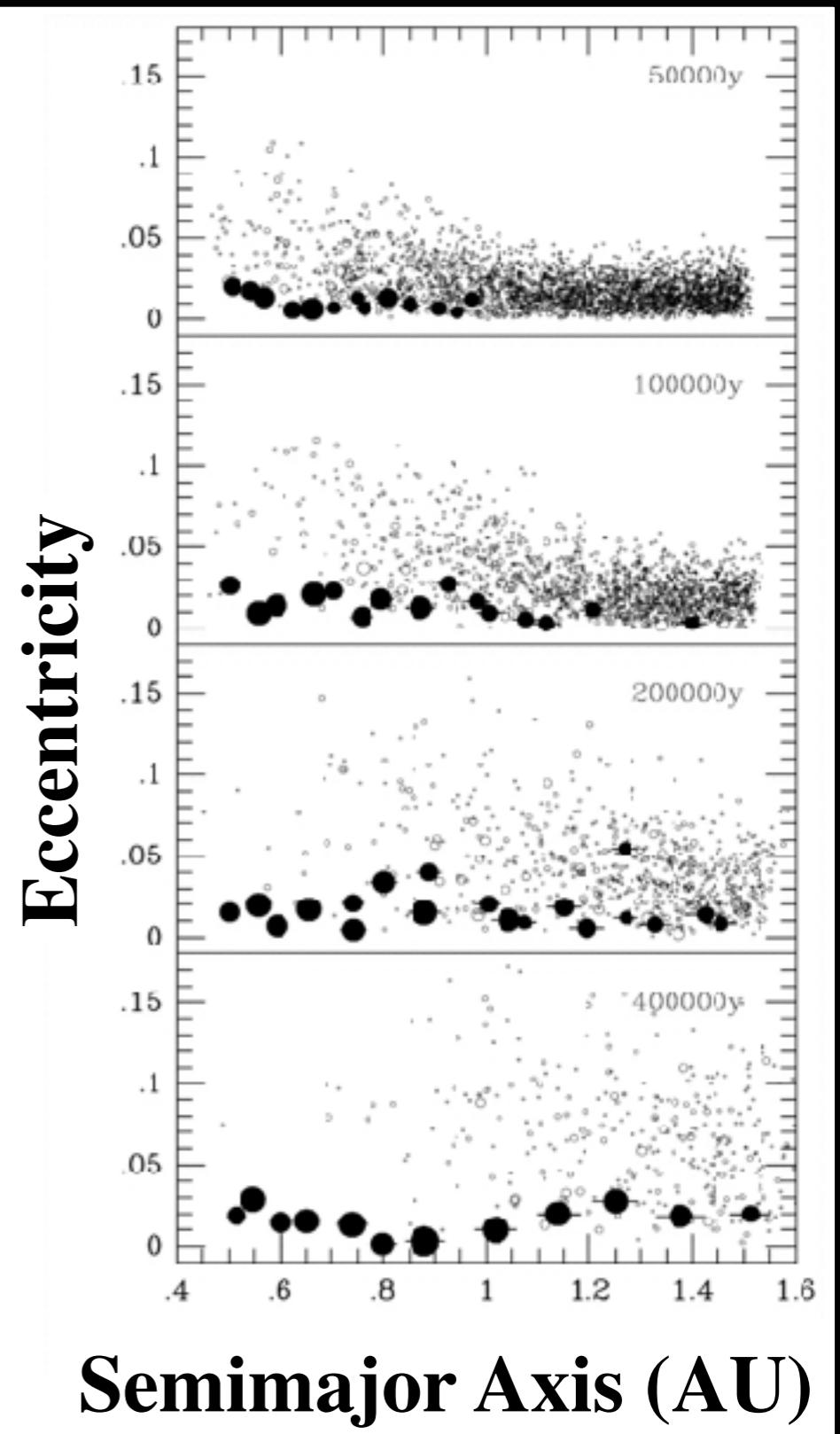


Lambrechts et al (2014); also Bitsch et al (2018)

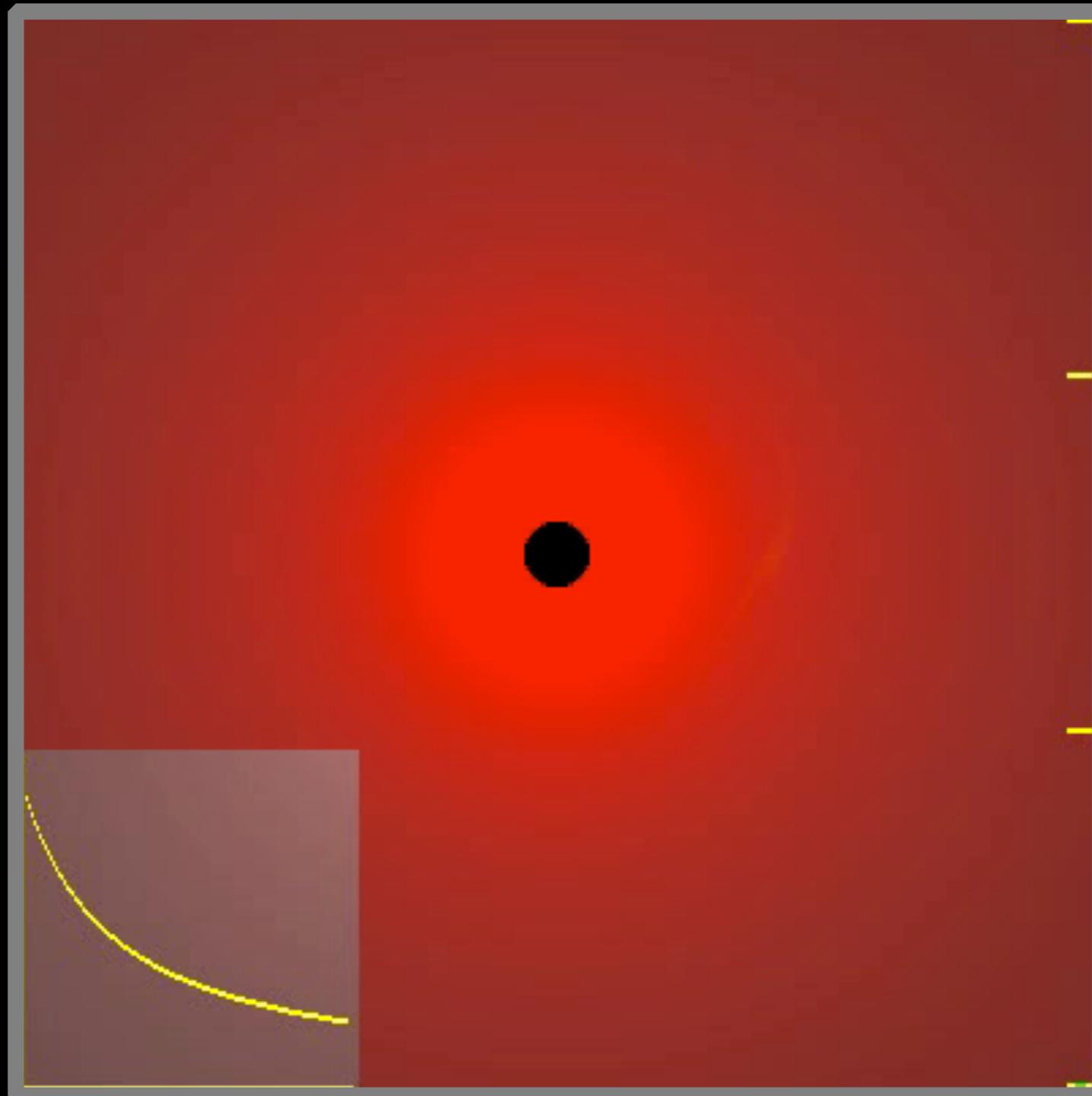
Planetesimal accretion

(dominates in terrestrial planet region)

- Runaway growth: big embryos get bigger faster by eating planetesimals



Gravitational planet-disk interaction: orbital migration

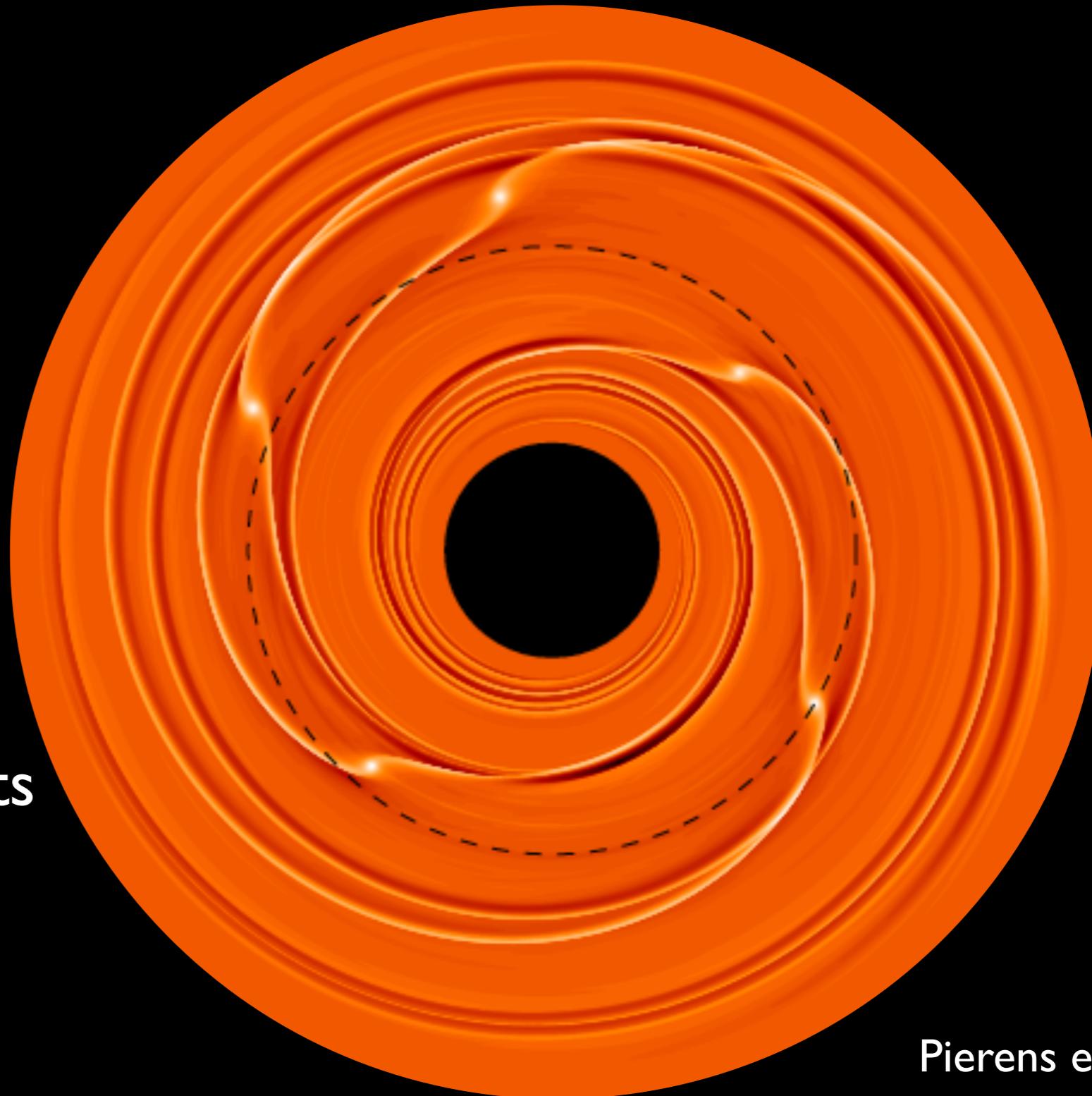


P.Armitage

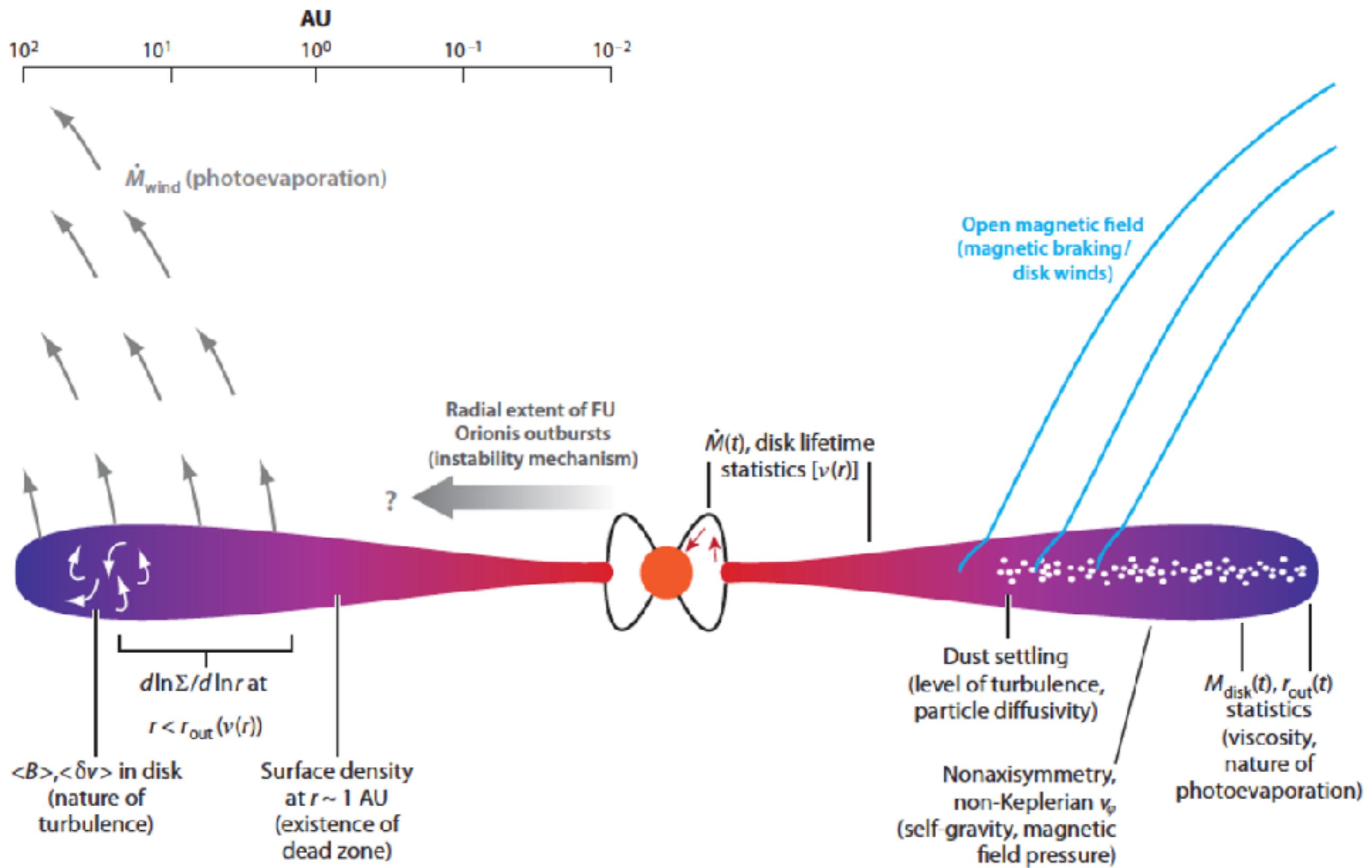
Type I migration

Matters for
 $M_p > \sim M_{\text{Earth}}$

More massive planets
migrate faster



Pierens et al (2013)



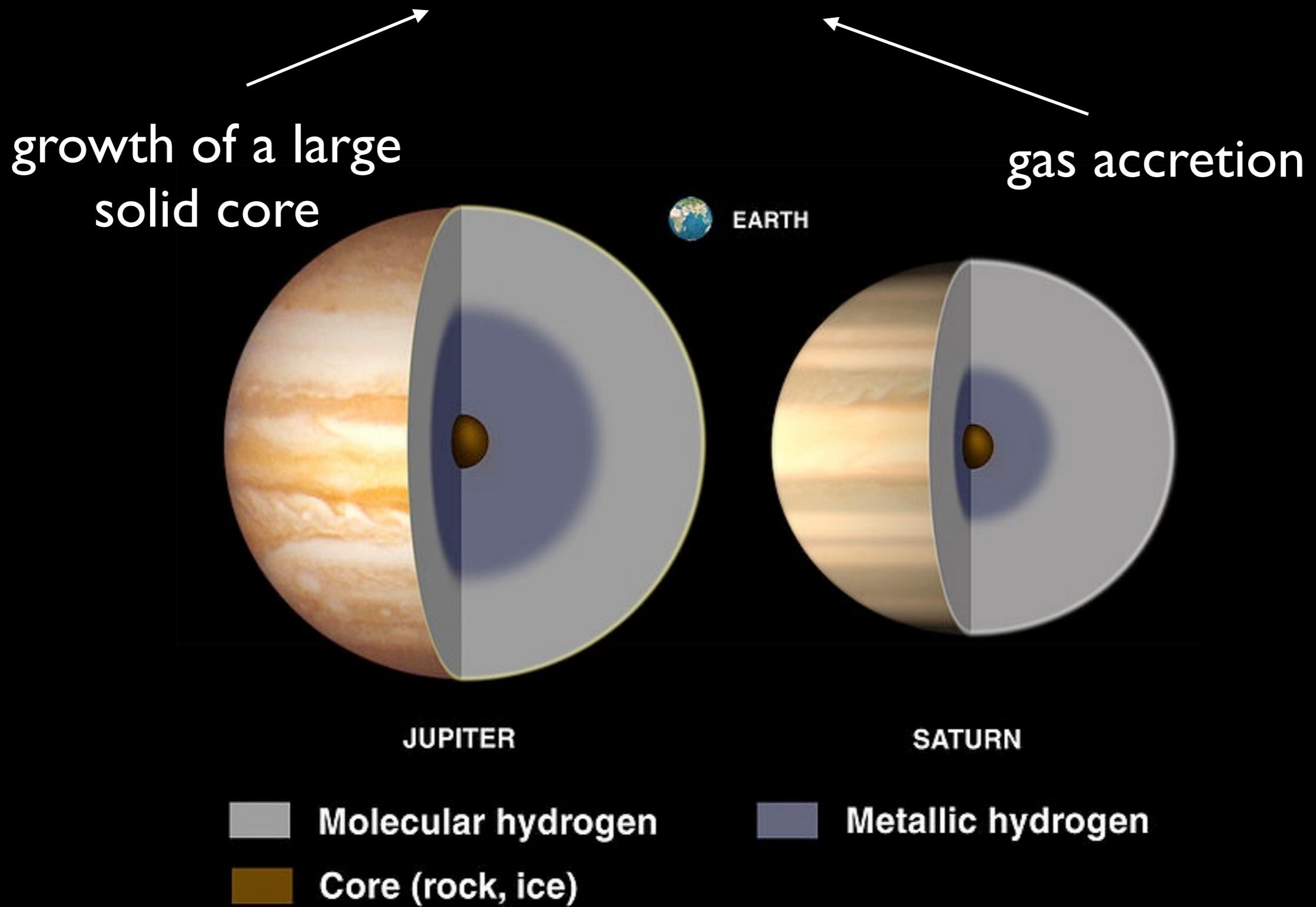
Migration stops at the inner edge of the disk



Masset et al (2006)

also Romanova & Lovelace (2006); Flock et al (2017)

Core accretion

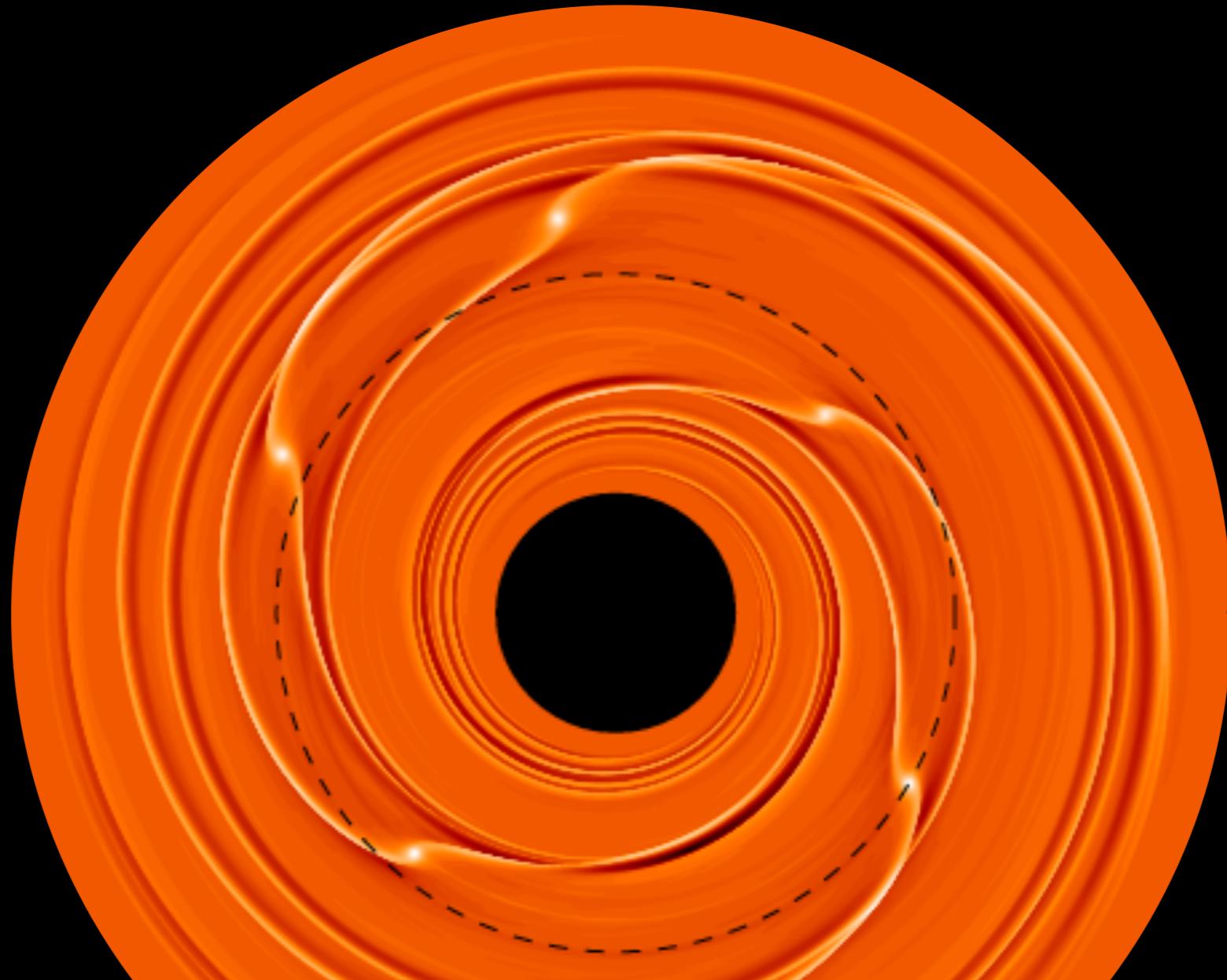


Core migration accretion

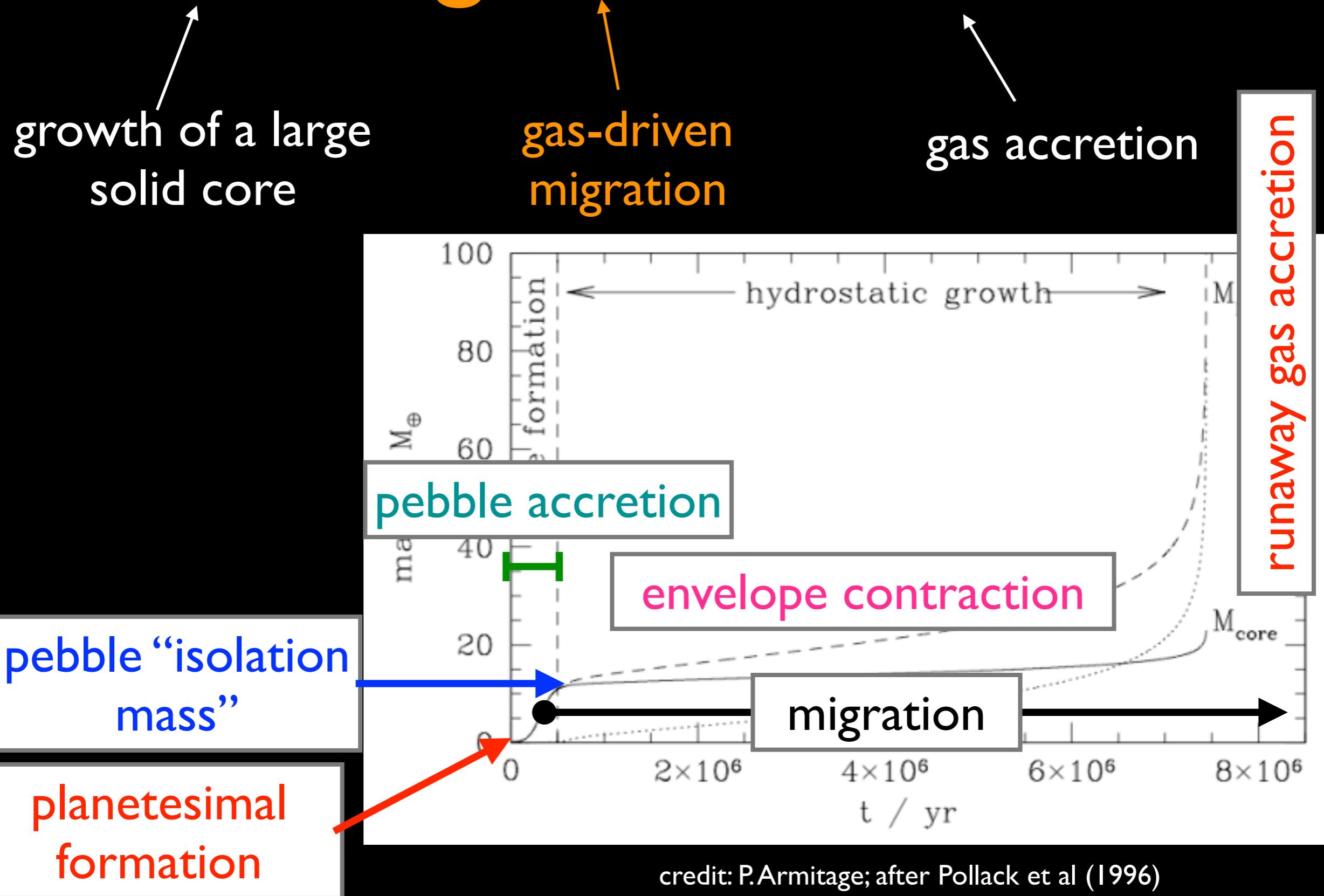
↑
growth of a large solid core

↑
gas-driven migration

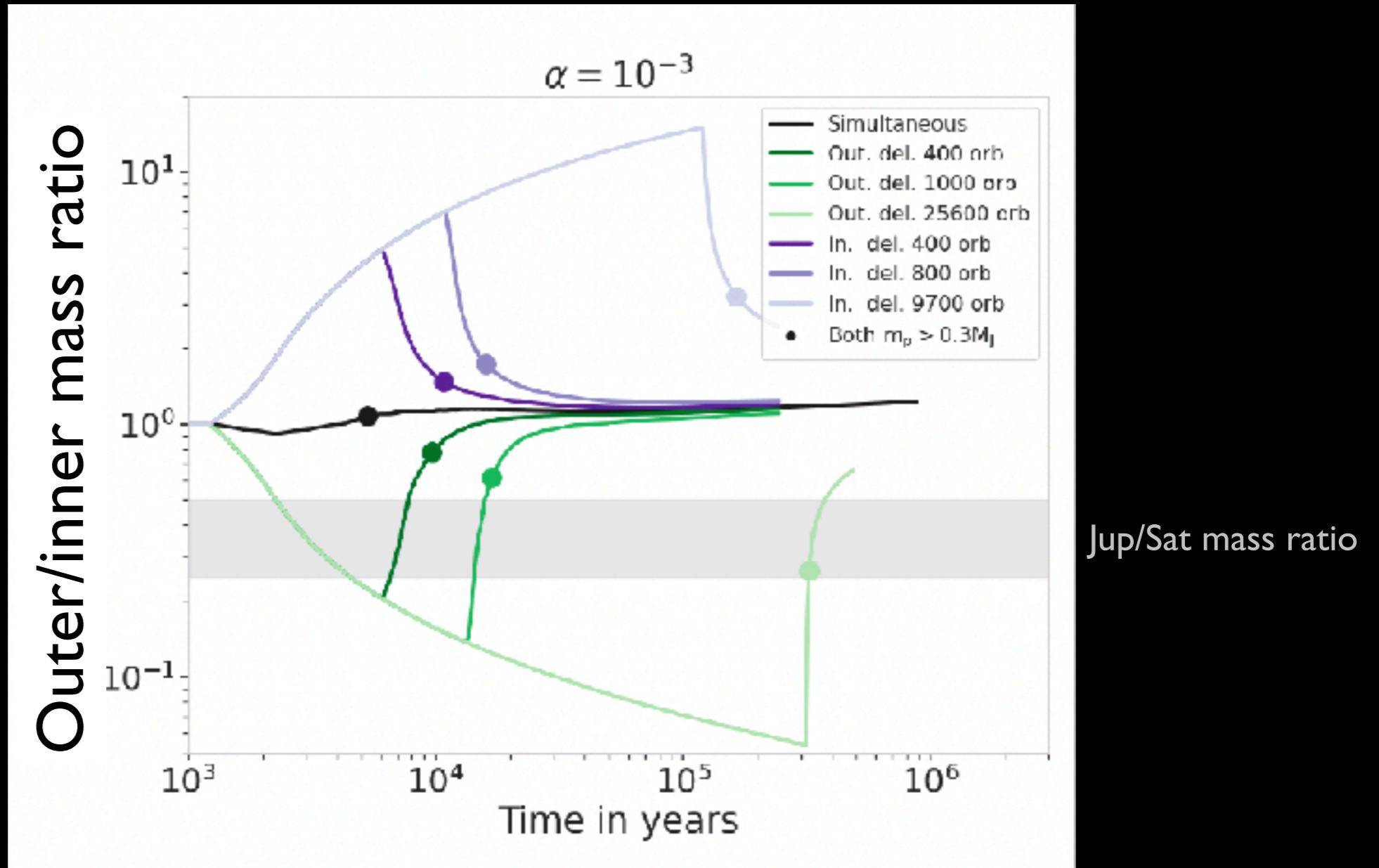
↑
gas accretion



Core migration accretion

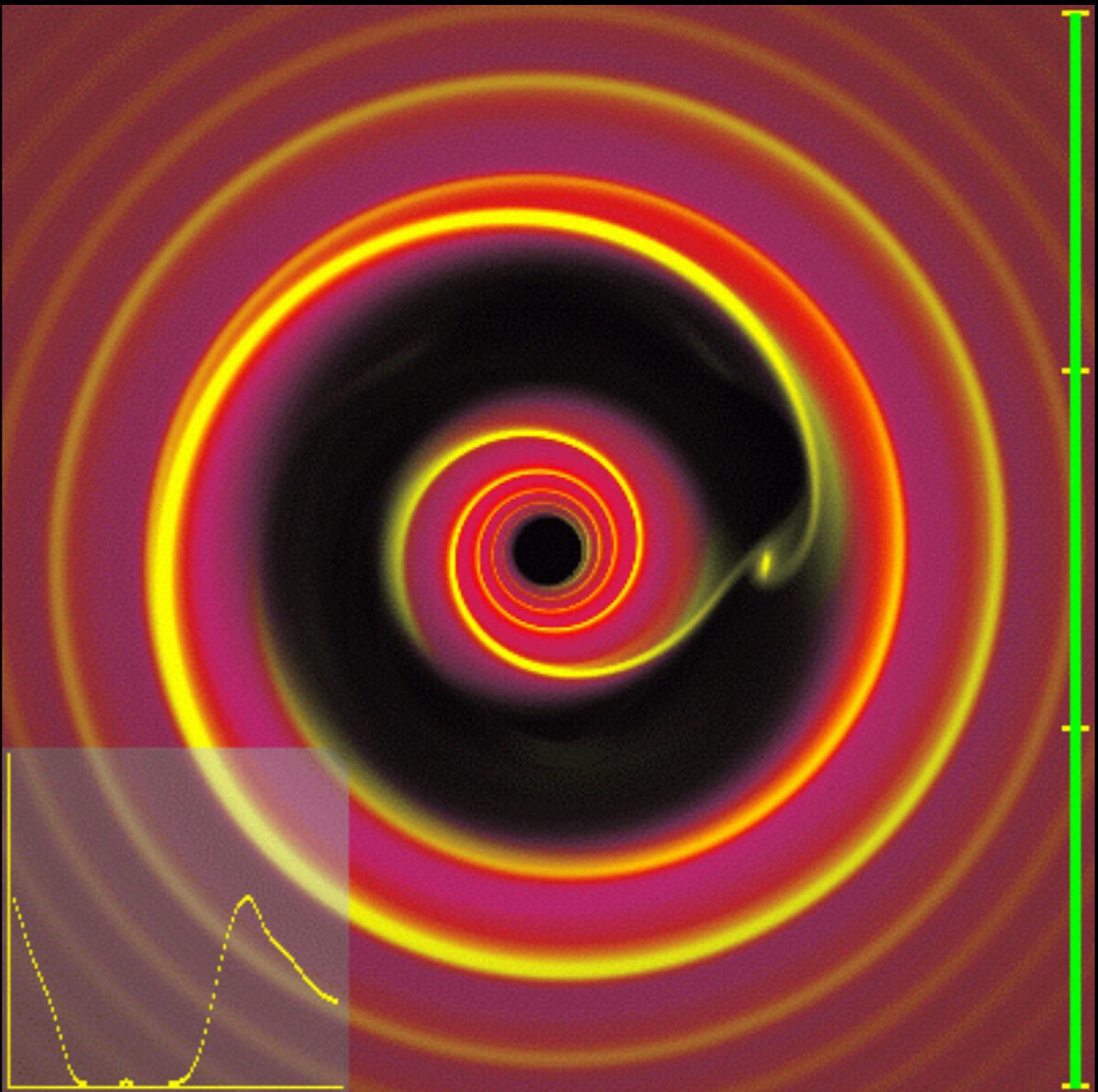


Two planets growing in the same disk tend to end up at ~the same mass

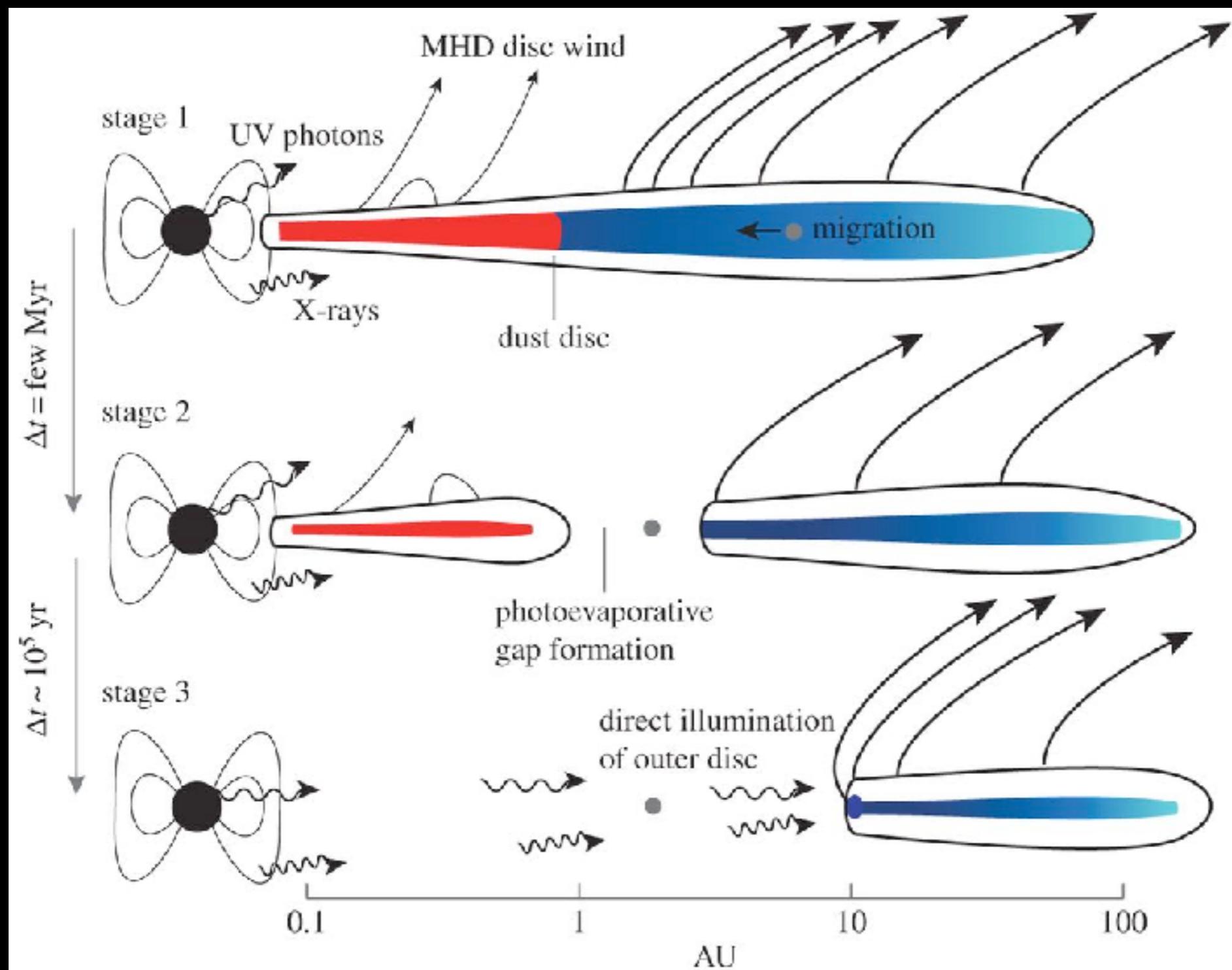


Type 2 migration

- Carve gap in disk
- Migration almost always inward
- Special cases: 2+ planets can migrate outward (e.g., Grand Tack model)

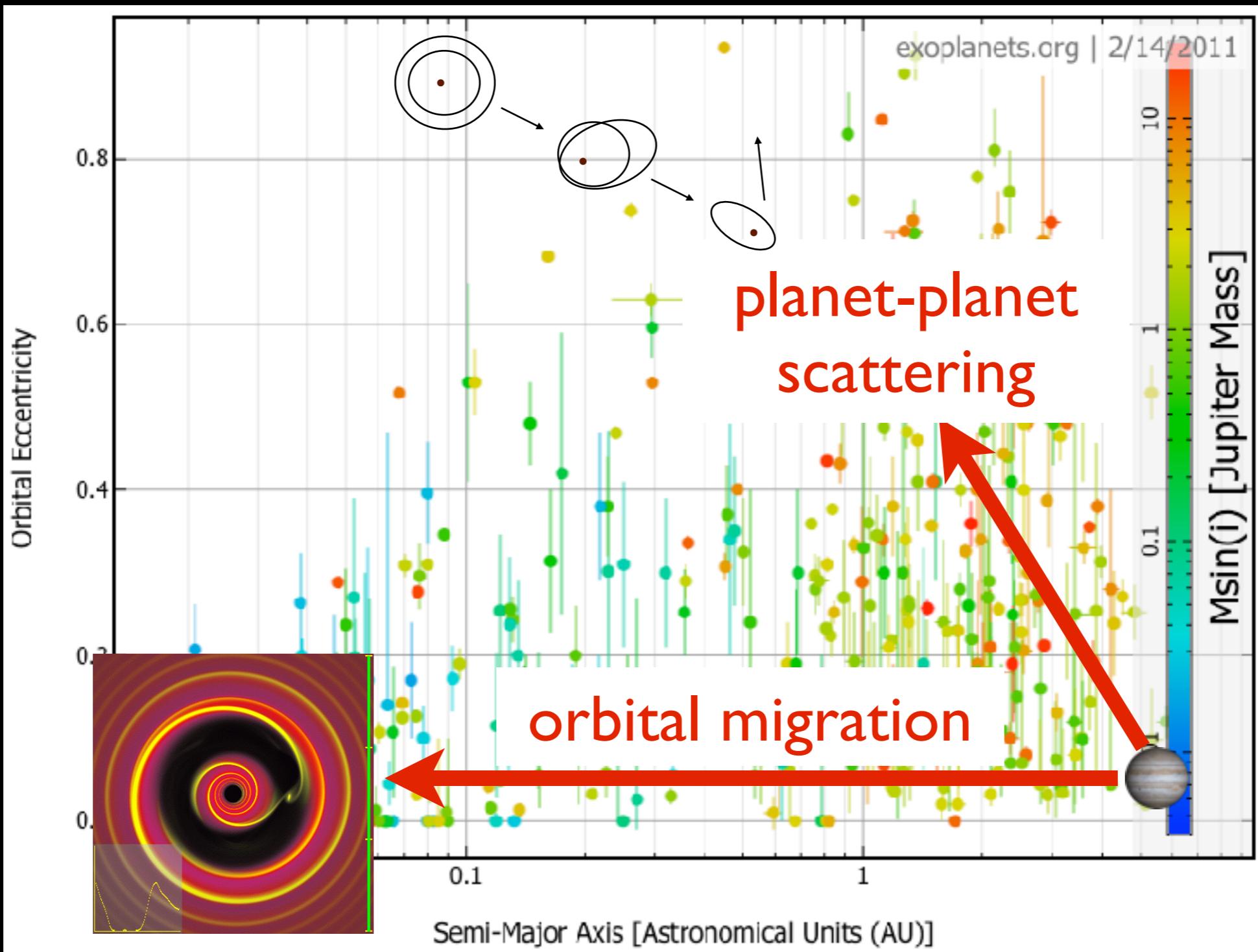


Inside-out photo-evaporation of gaseous disk



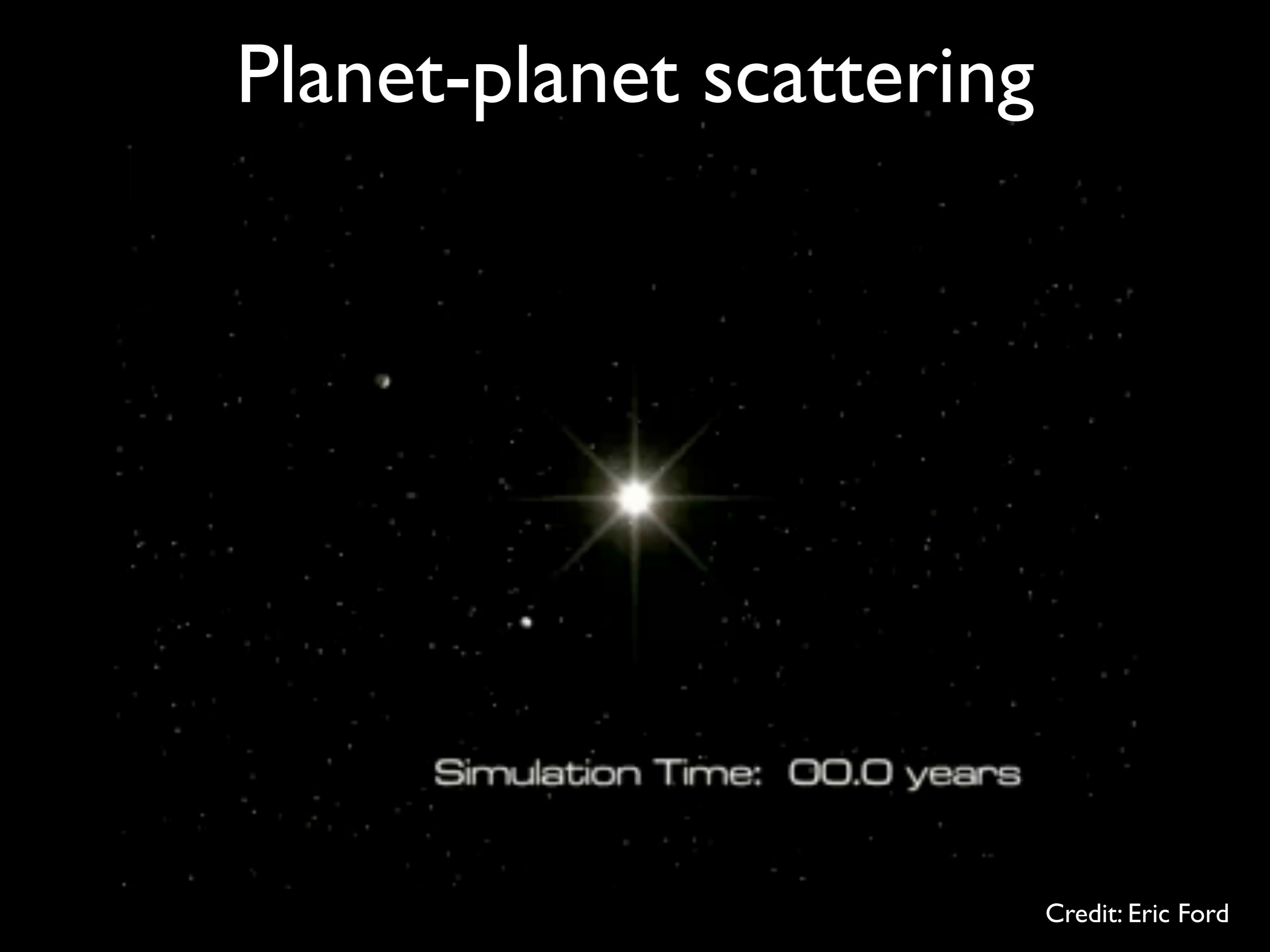
Armitage (2010)

Giant exoplanets



Wright et al
2011

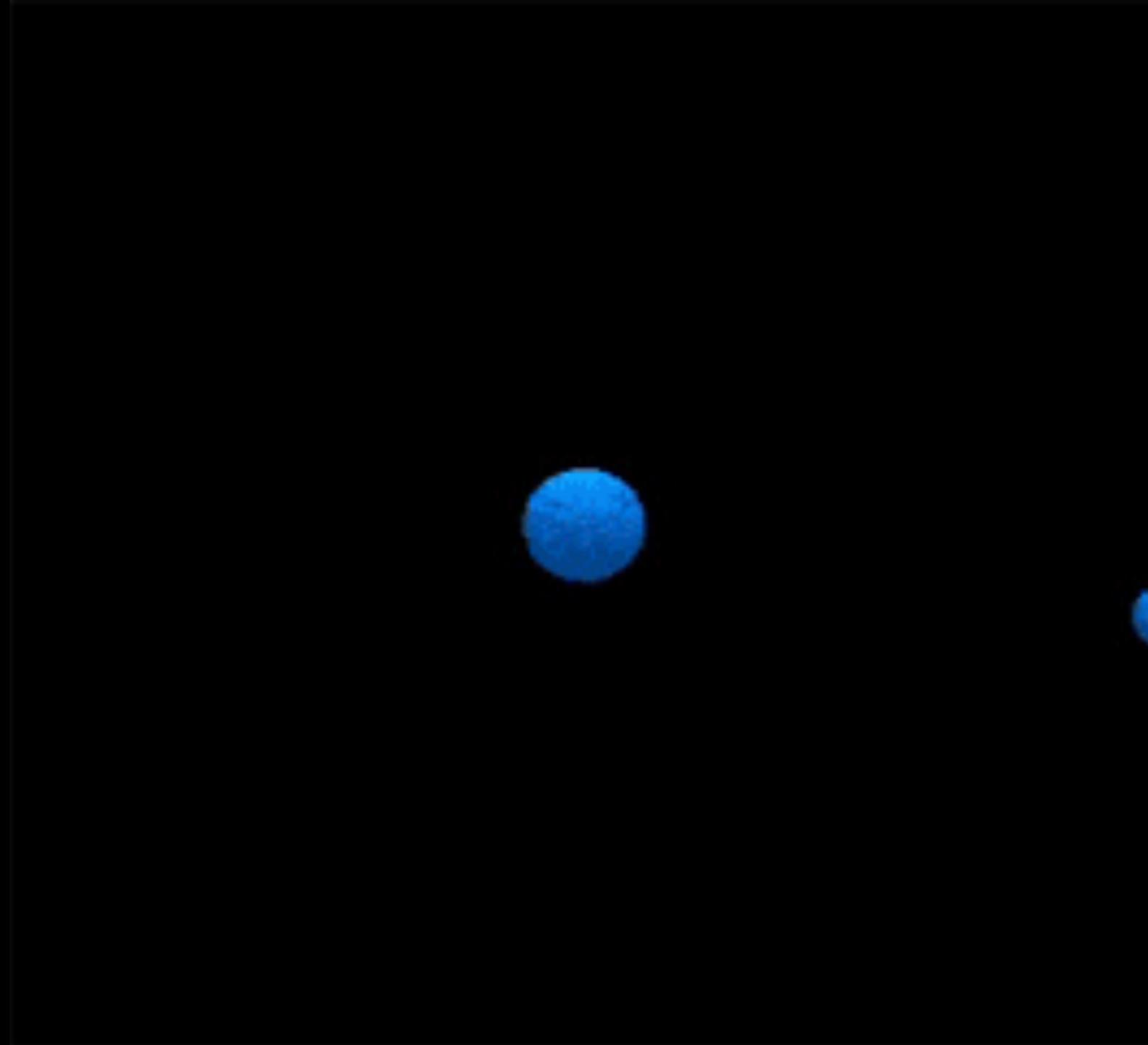
Planet-planet scattering



Simulation Time: 00.0 years

Credit: Eric Ford

Giant impacts between embryos



credit: Agnor & Asphaug

Final planetesimal impacts: “late accretion/veneer”



Estimate: ~0.5% of Earth's mass accreted from planetesimals
after Moon-forming impact
(Day et al 2007; Walker 2009)

Gas giants

~10 Earth-mass cores

$1 M_{\text{Earth}}$

Mars-mass embryos

Planets
simals
(~ 100 km)

Dust
(μm)

Migration

pebble accretion

beyond snow line: ice+rock

dust coagulation

planetary accretion

streaming instability

gas disk lasts a few Myr

gas accretion (slow, then runaway)

pebble isolation

within snow line: rocky



giant impacts

late veneer (planetesimal impacts)



Moon-forming impact

10^7 yrs

10^4 yrs

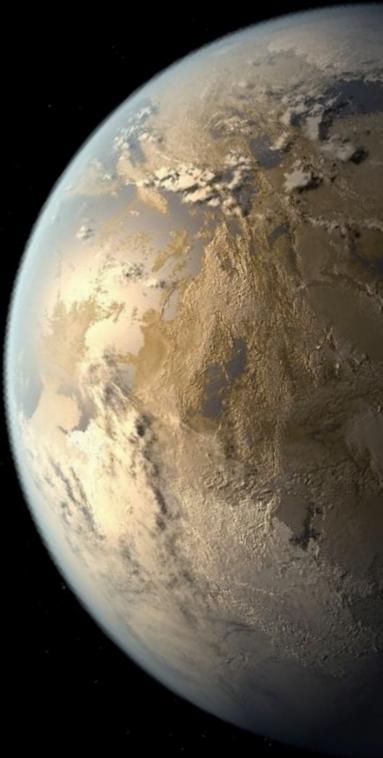
10^5 yrs

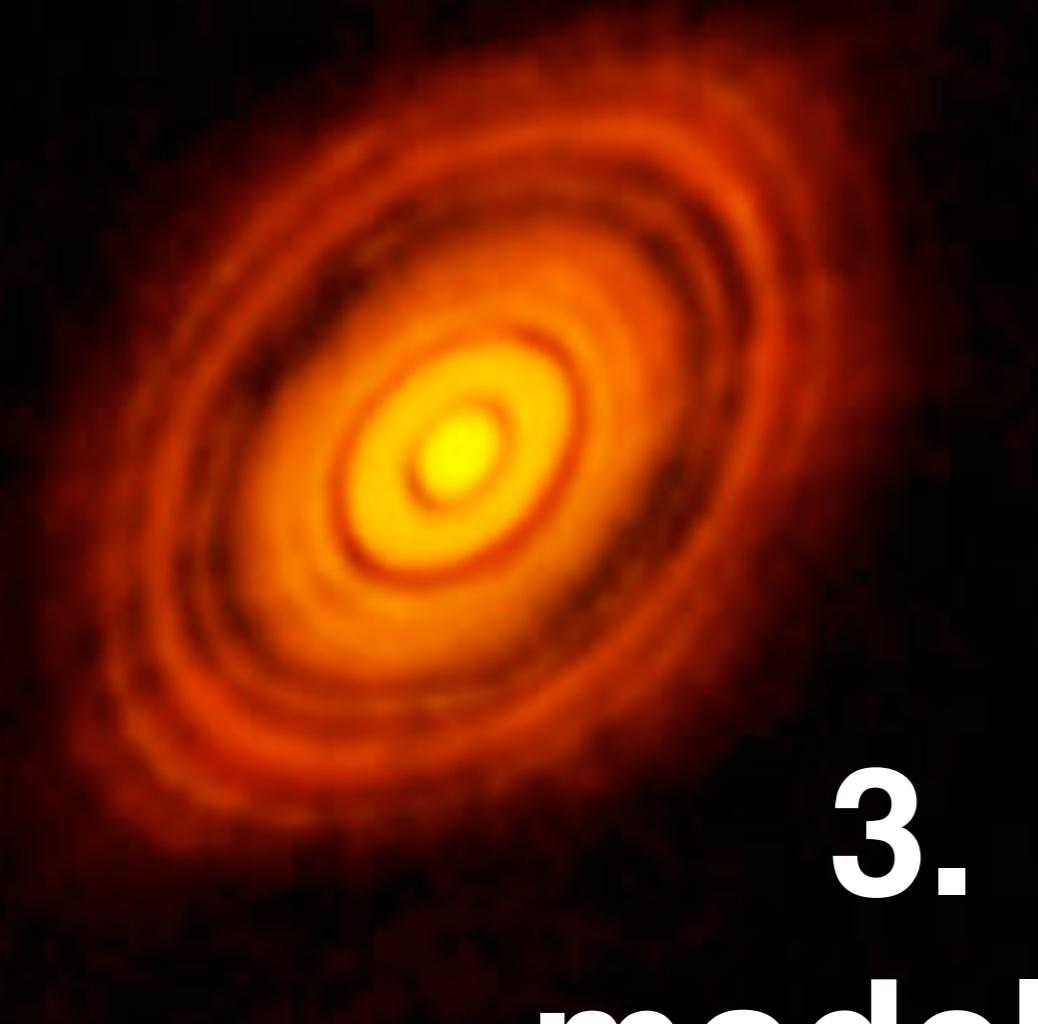
10^6 yrs

10^8 yrs

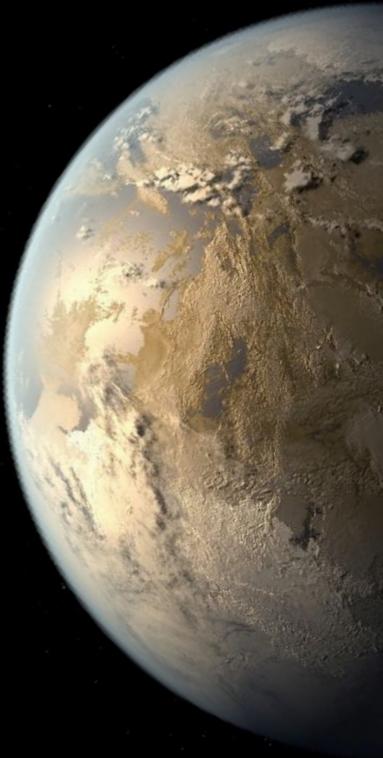


Summary: Stages of planet formation

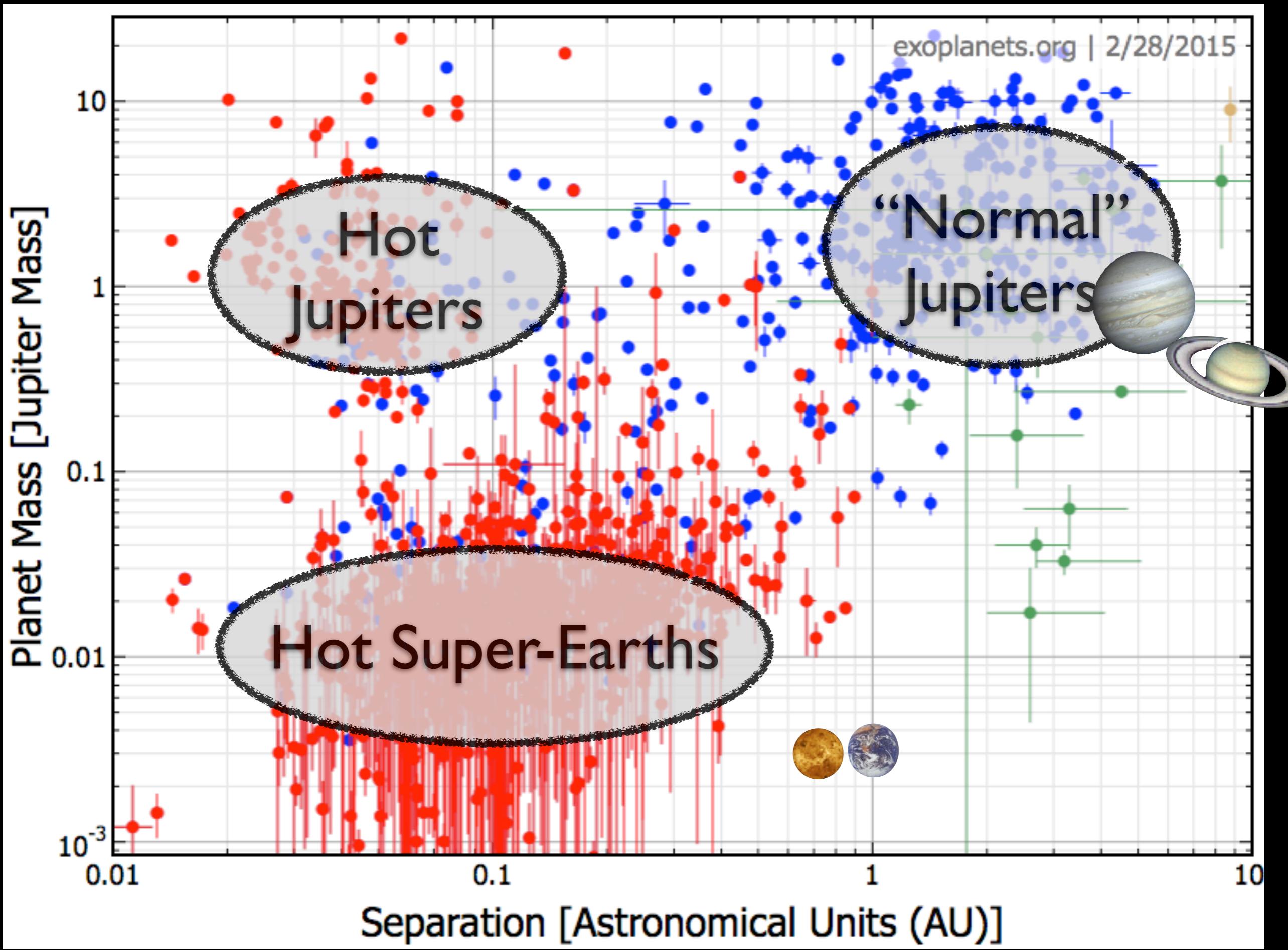
- planetesimal formation
 - pebble/planetesimal accretion
 - orbital migration
 - giant impacts
 - gas accretion
 - giant planet scattering
- 



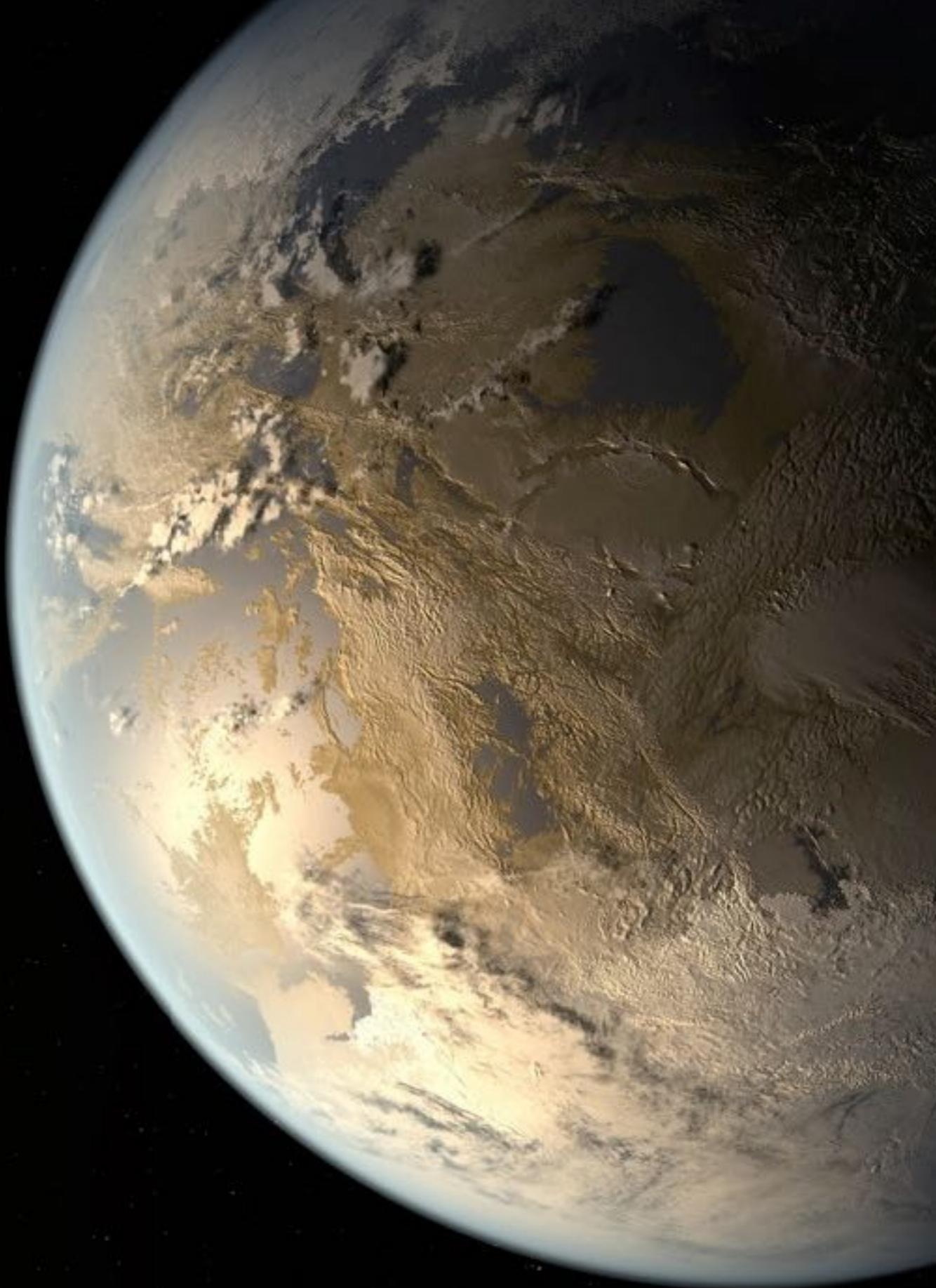
3. Formation models: exoplanets



- Close-in “super-Earths”
- Gas giants



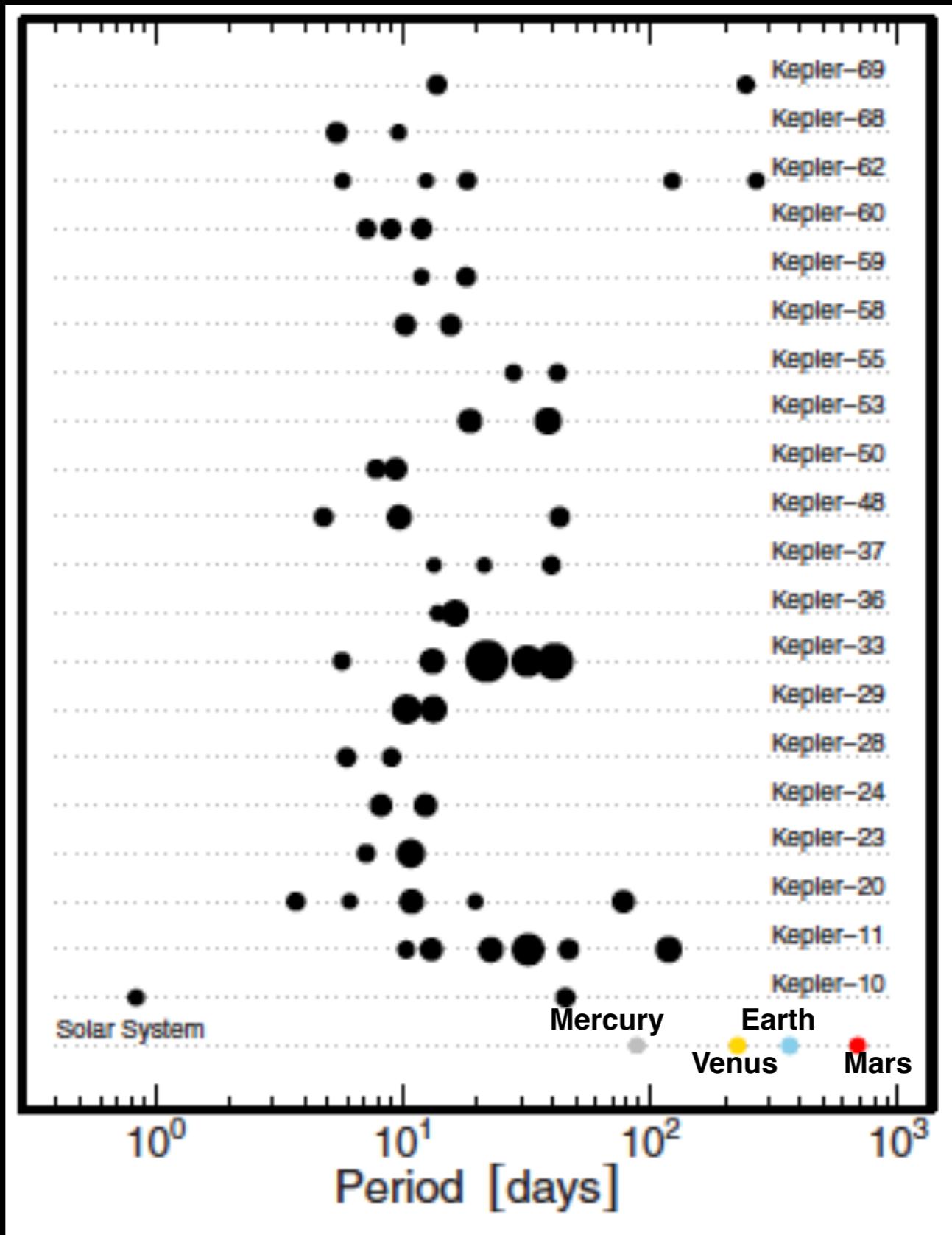
Super-Earths: formation models



Super-Earths and the Solar System

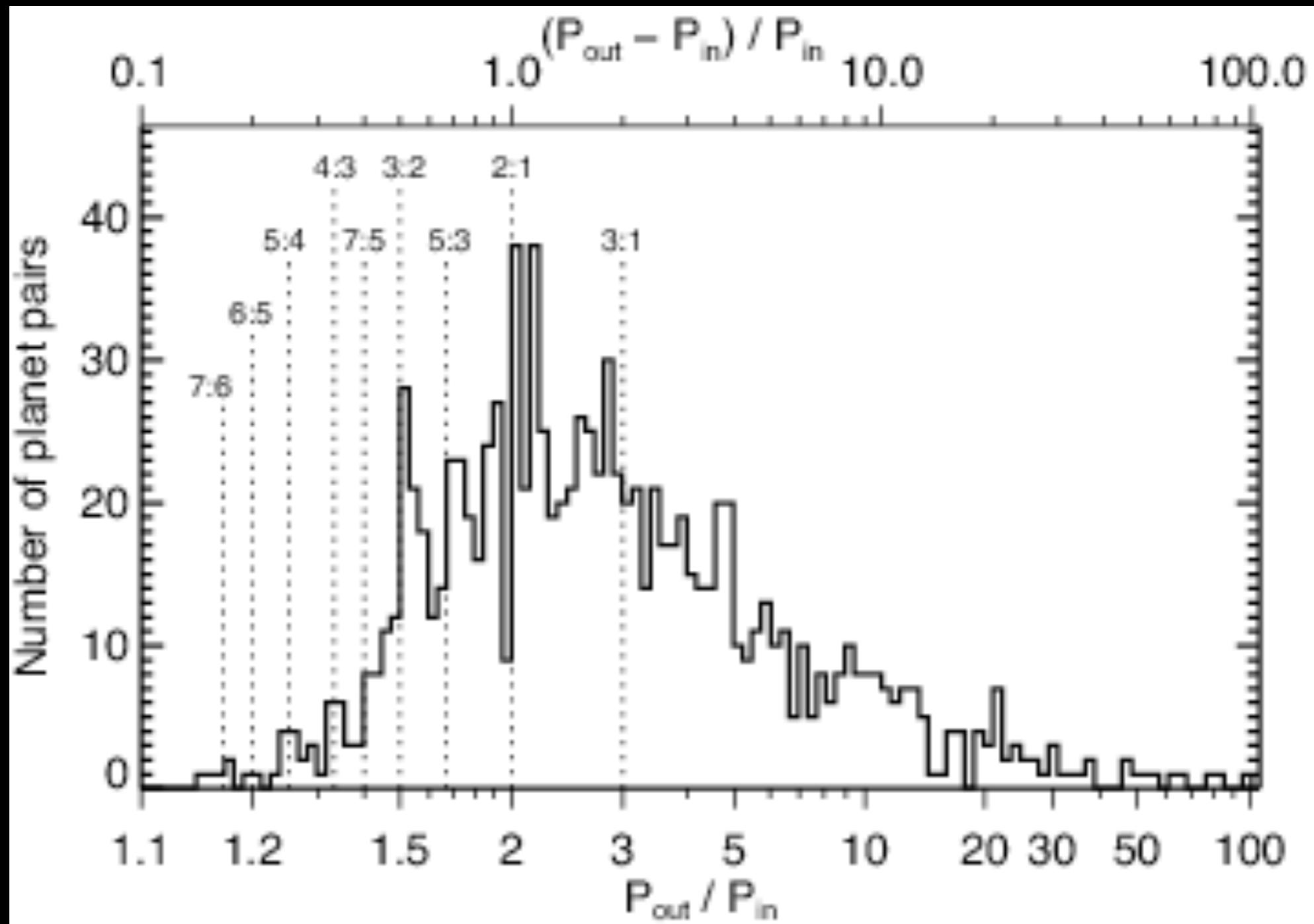
Occurrence rate:
~50%

(Mayor et al 2011; Howard et al 2012;
Fressin et al 2013, Mulders et al 2018;
many more)



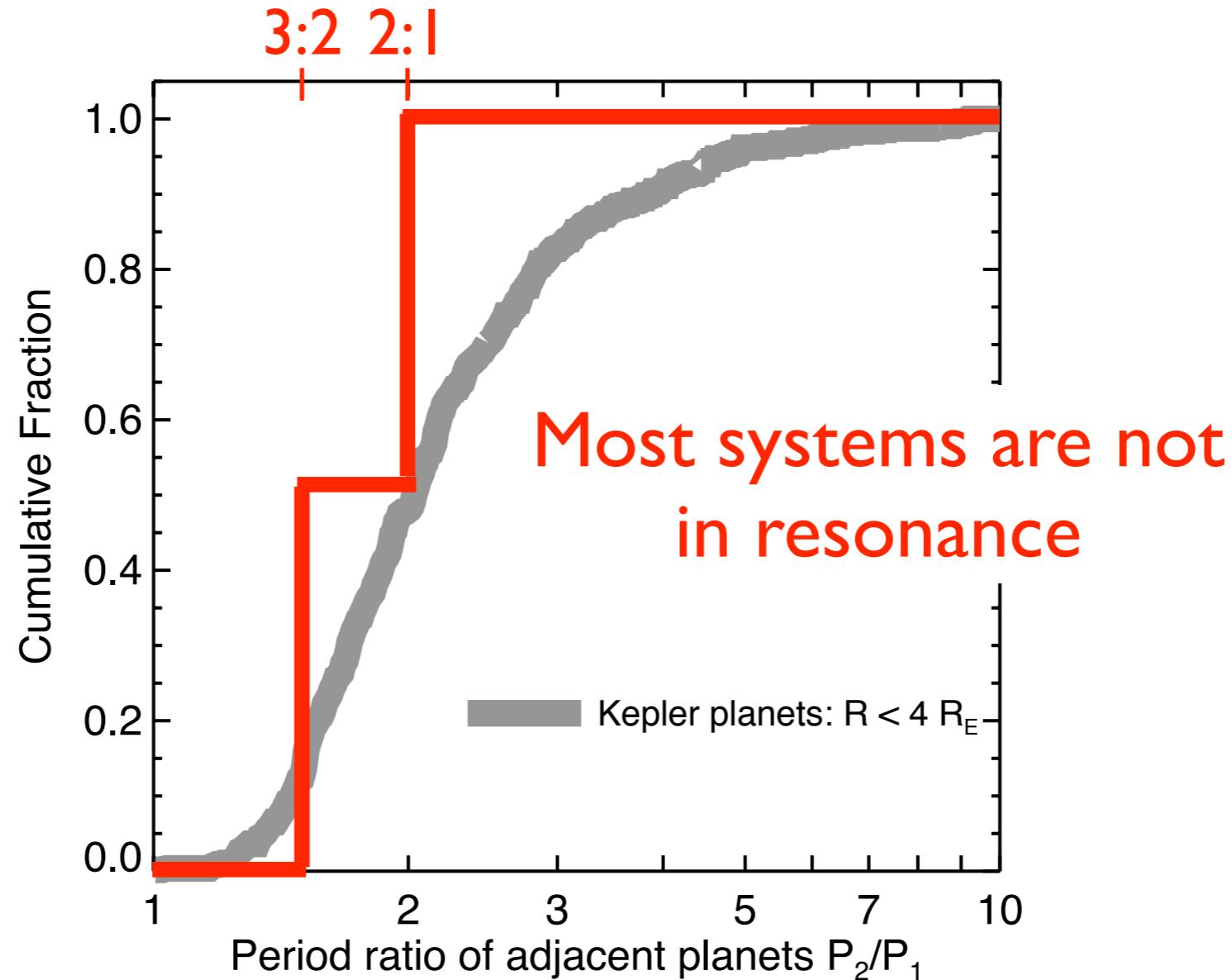
Schlaufman
(2014); Kepler data
from Batalha et al
(2013) and Rowe et al
(2014)

Period Ratio distribution

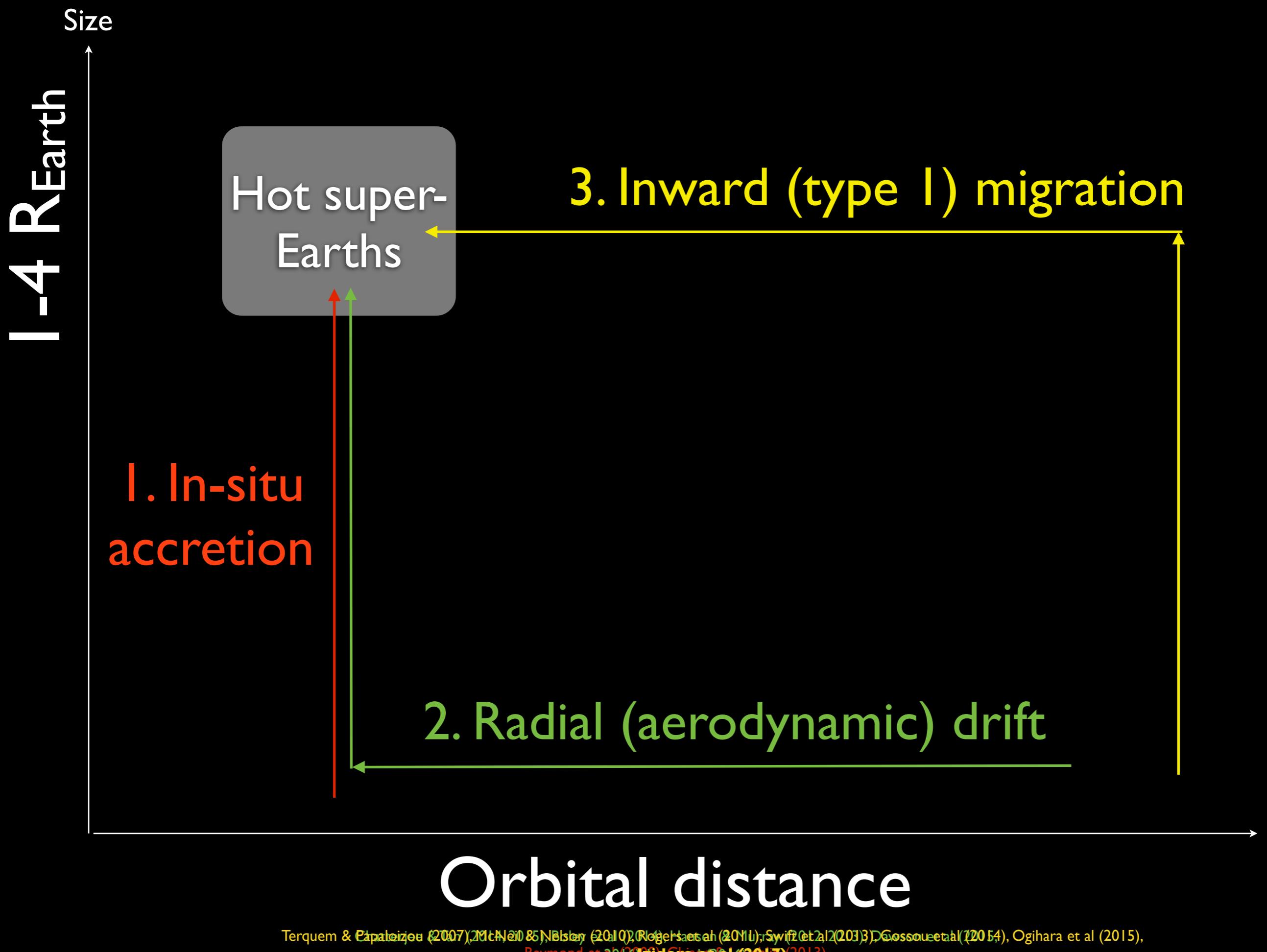


Winn & Fabrycky 2015

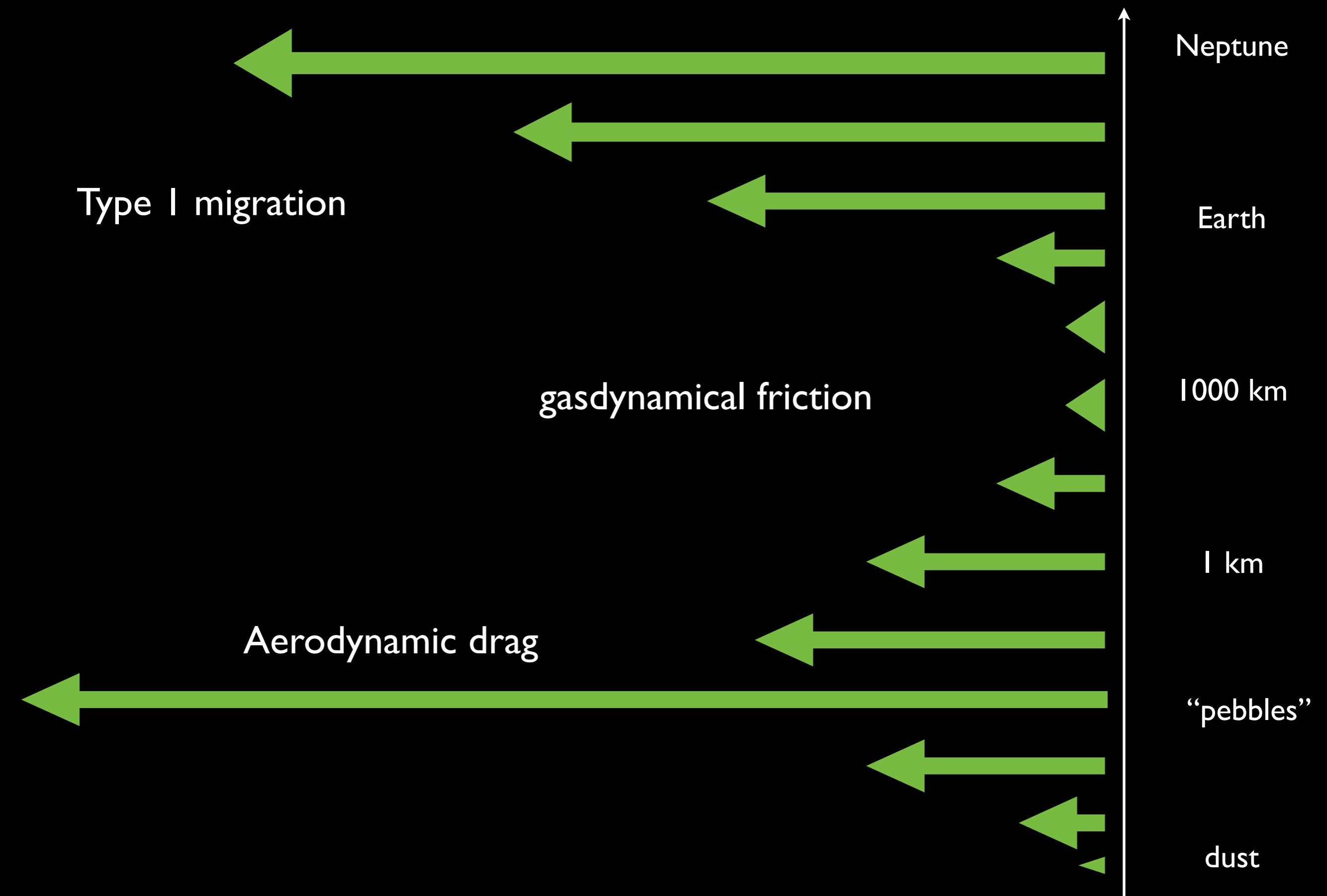
Period ratio distribution



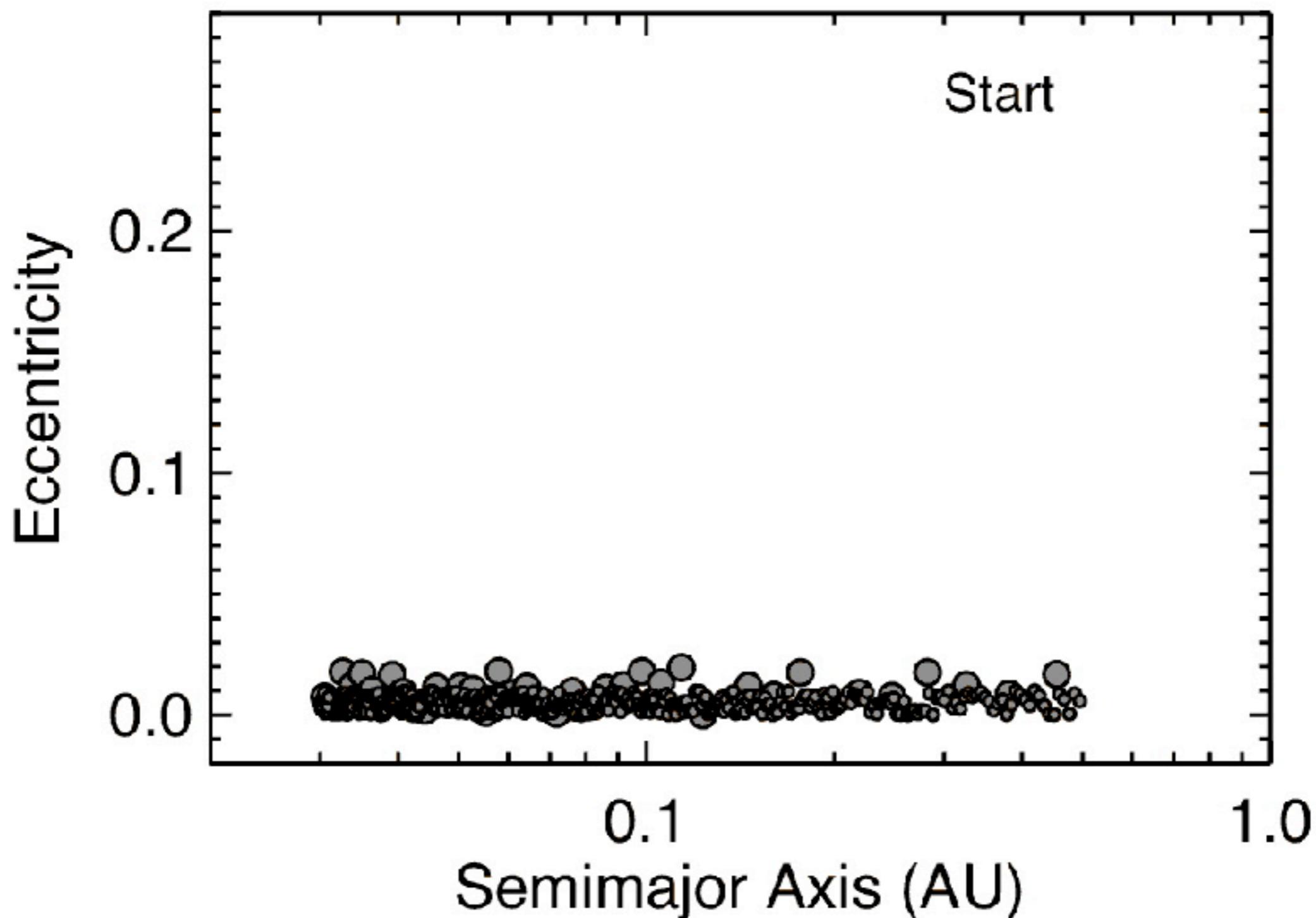
Lissauer et al (2011); Fabrycky et al (2014)



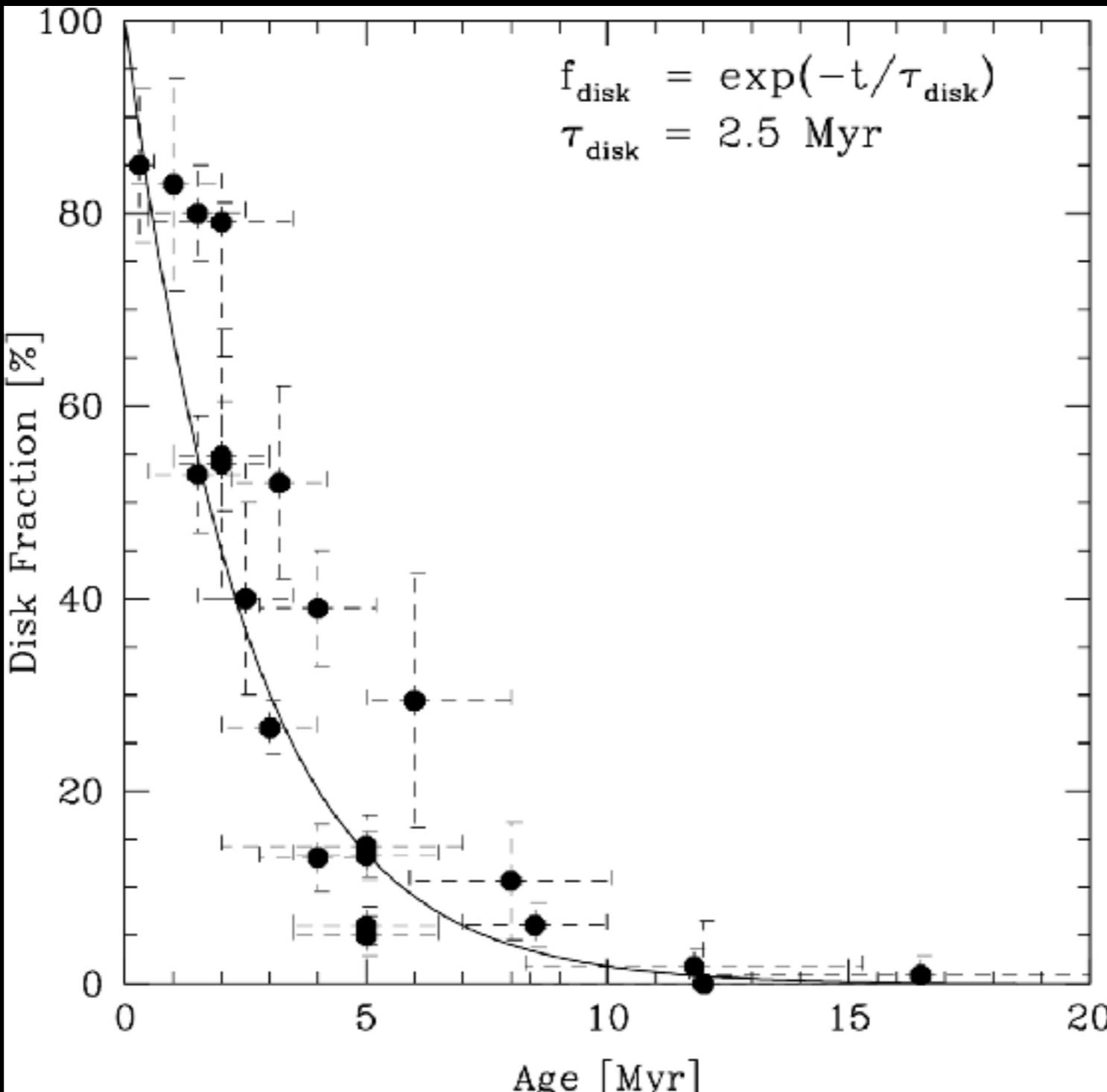
Gaseous disk causes orbital decay



Growth timescales are very short

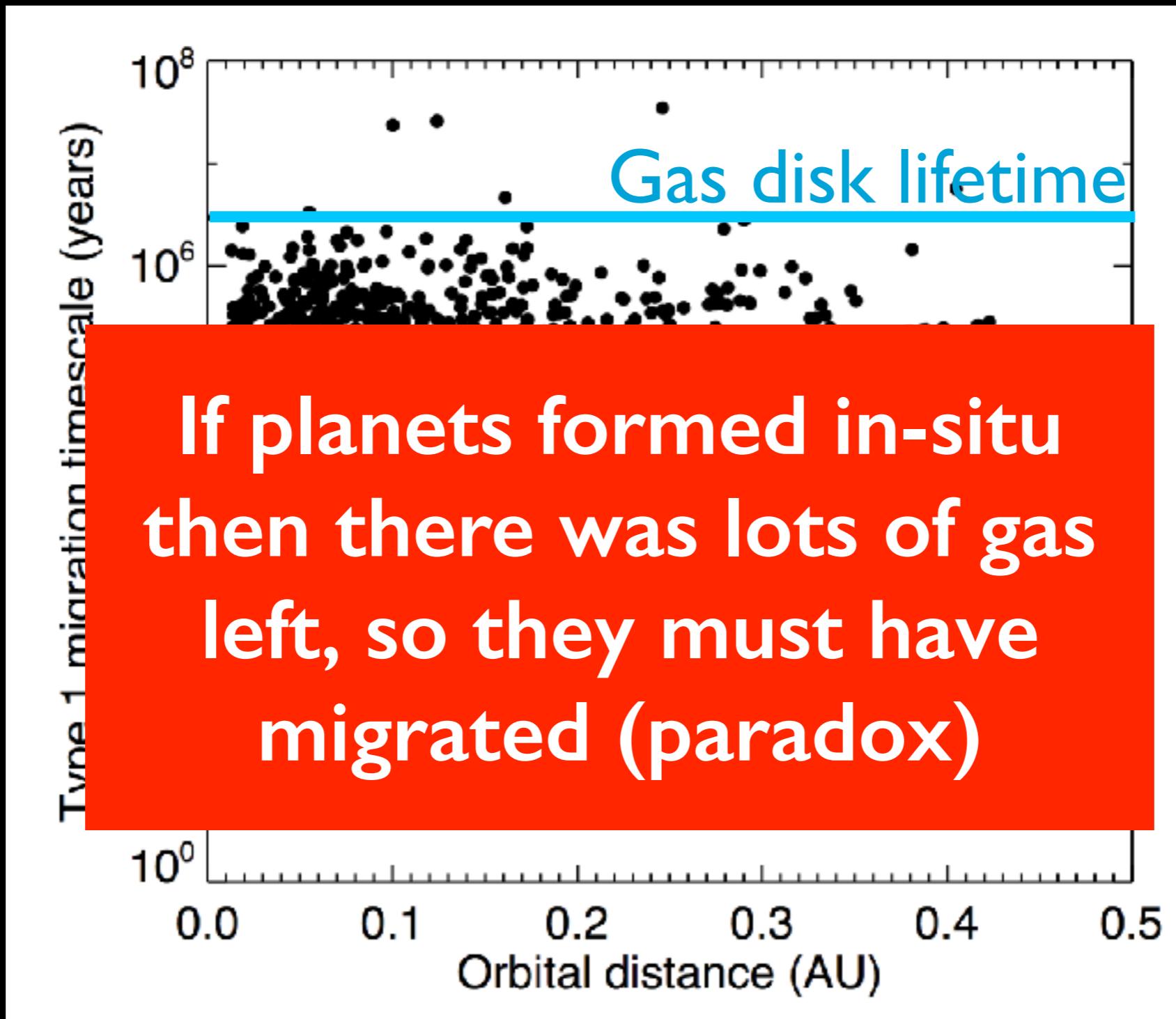


Gas disks (inferred from hot dust) dissipate on a few Myr timescale

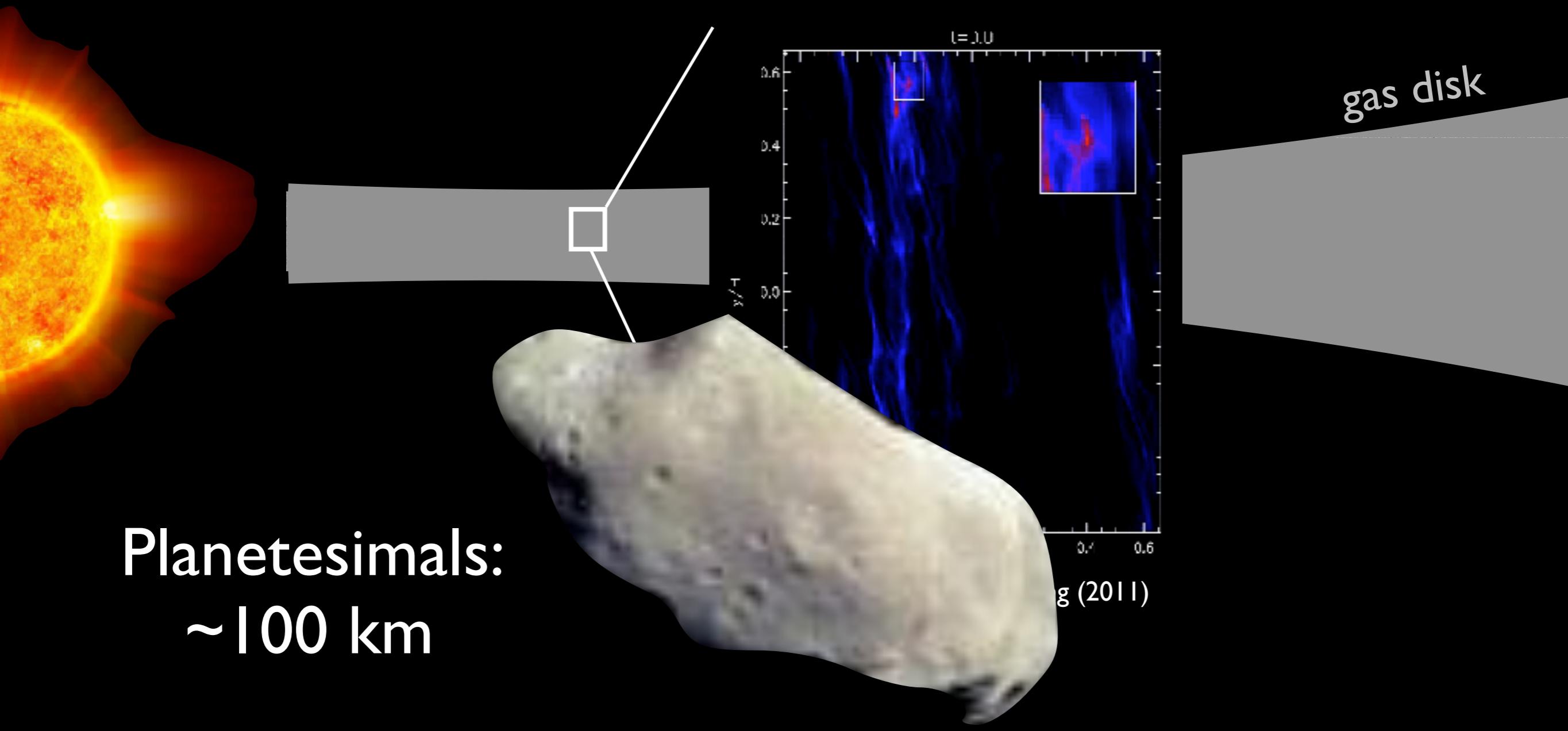


Mamajek 2009

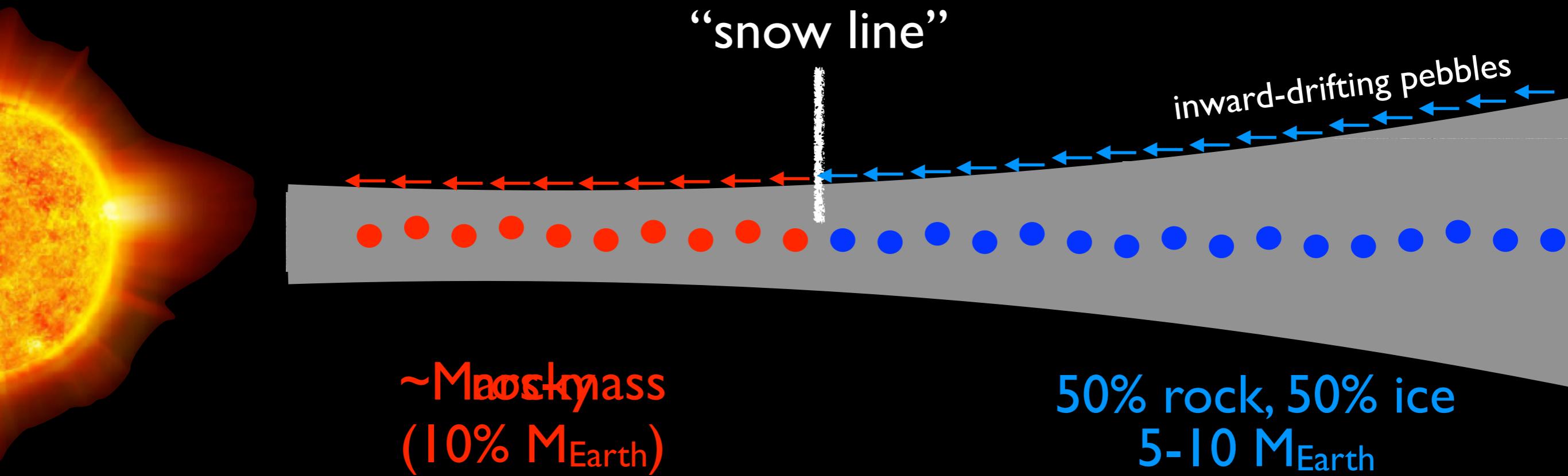
Migration timescales are very short: “in-situ” accretion is impossible



See Inamdar & Schlichting 2015, Schlichting 2014; Ogiwara et al 2015; Grishin & Perets 2015



Planetary embryos



Pebble accretion is far more efficient past the snowline
(Lambrechts et al 2014; Morbidelli et al 2015; Ormel 2017)

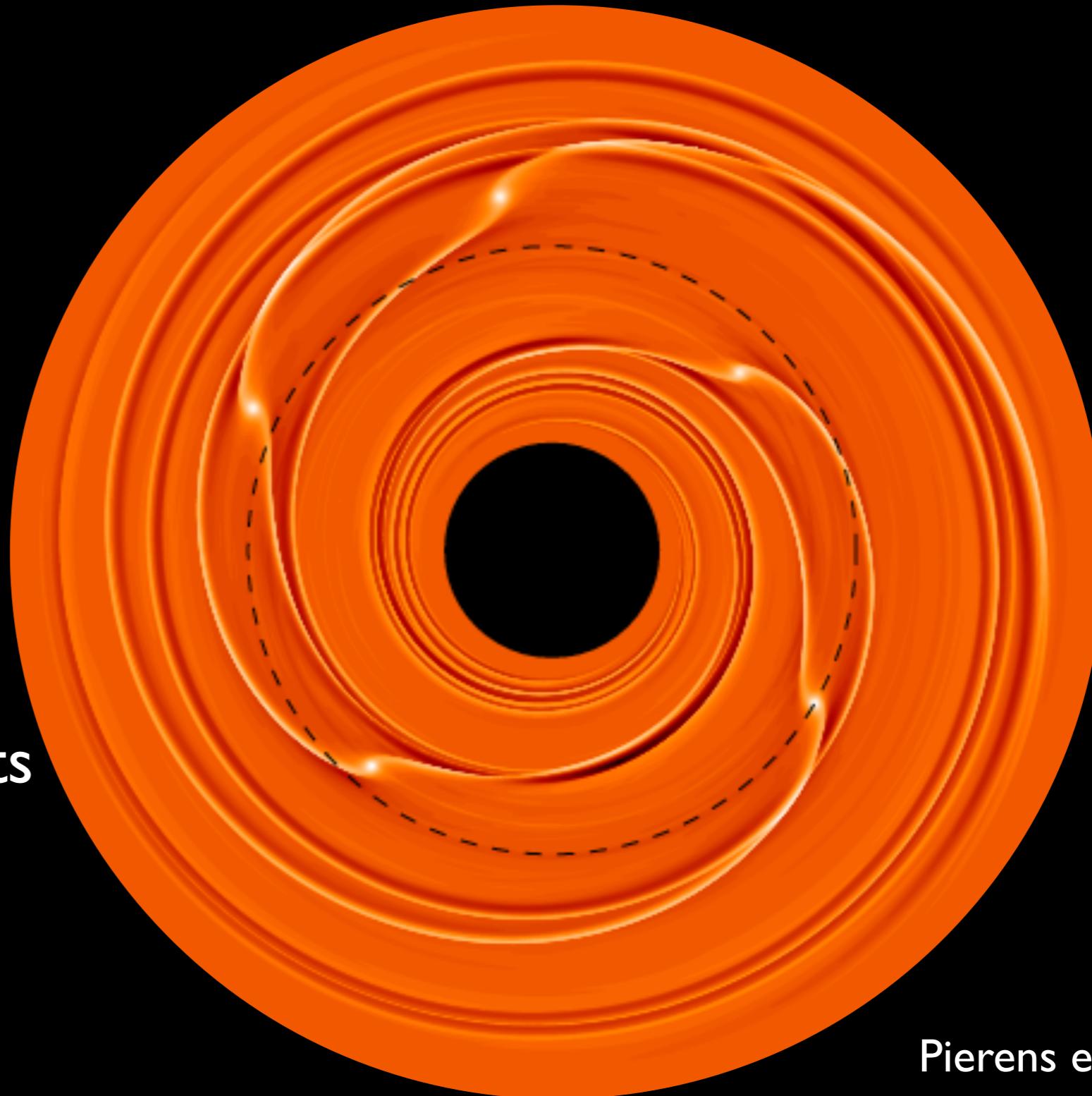
All roads lead to migration...



Orbital migration

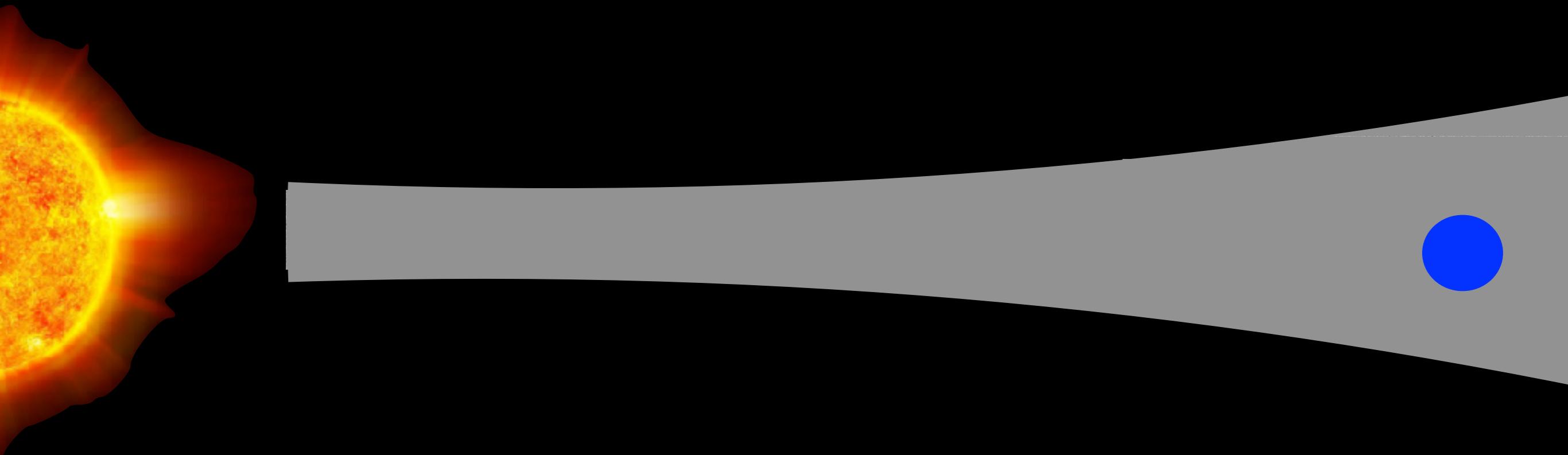
Matters for
 $M_p > \sim M_{\text{Earth}}$

More massive planets
migrate faster



Pierens et al (2013)

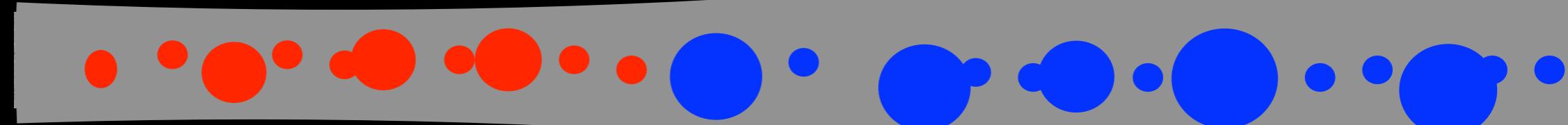
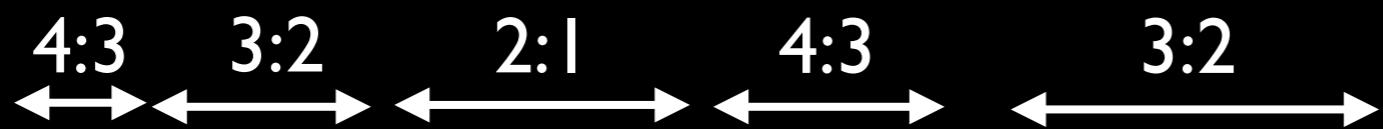
Migrating planets are trapped at the inner edge of the disk



Masset et al (2006); Romanova & Lovelace (2006)

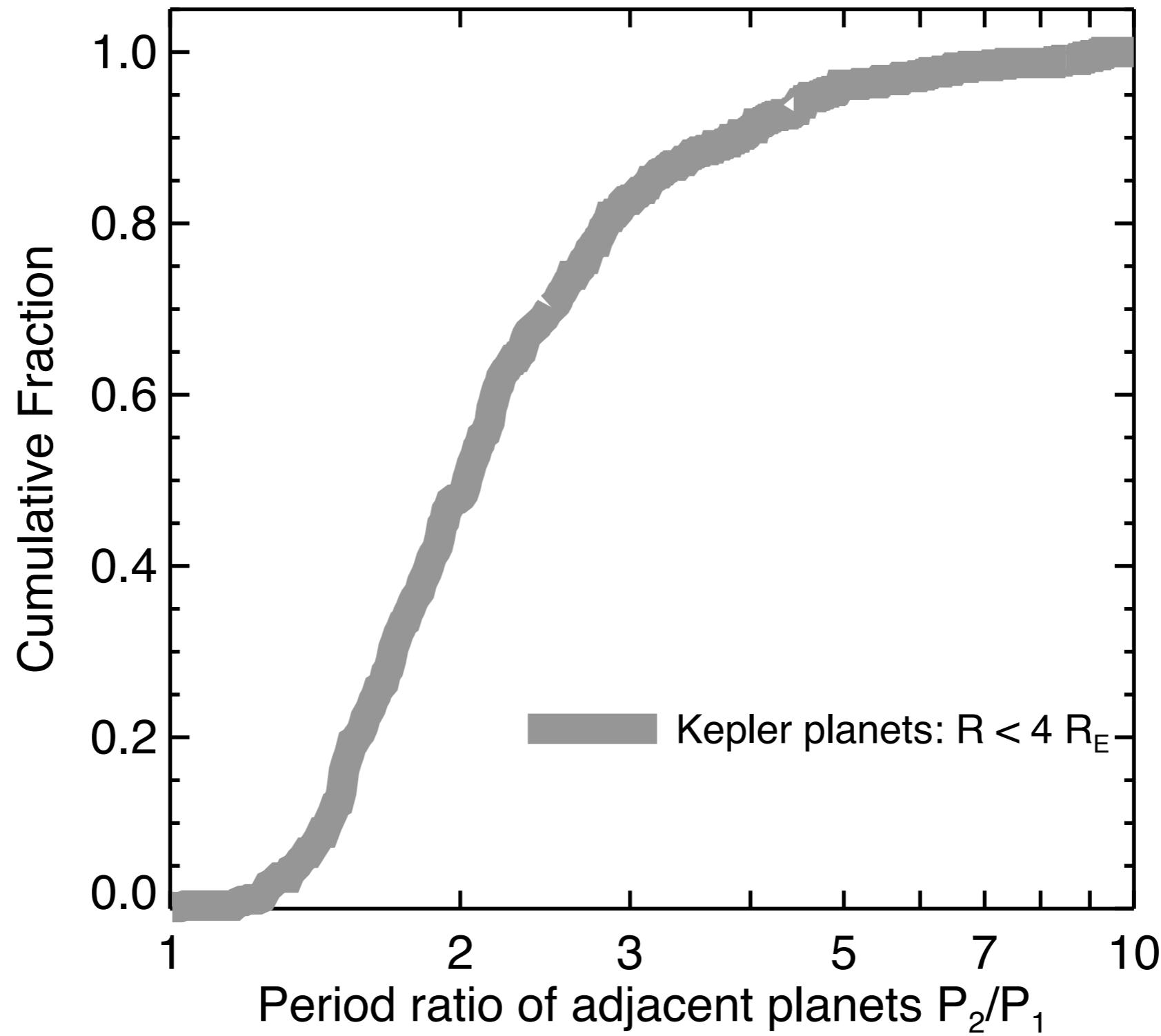
Planetary embryos

Instability spreads planets out and
destroys resonances
(e.g., Pichierri et al 2019)

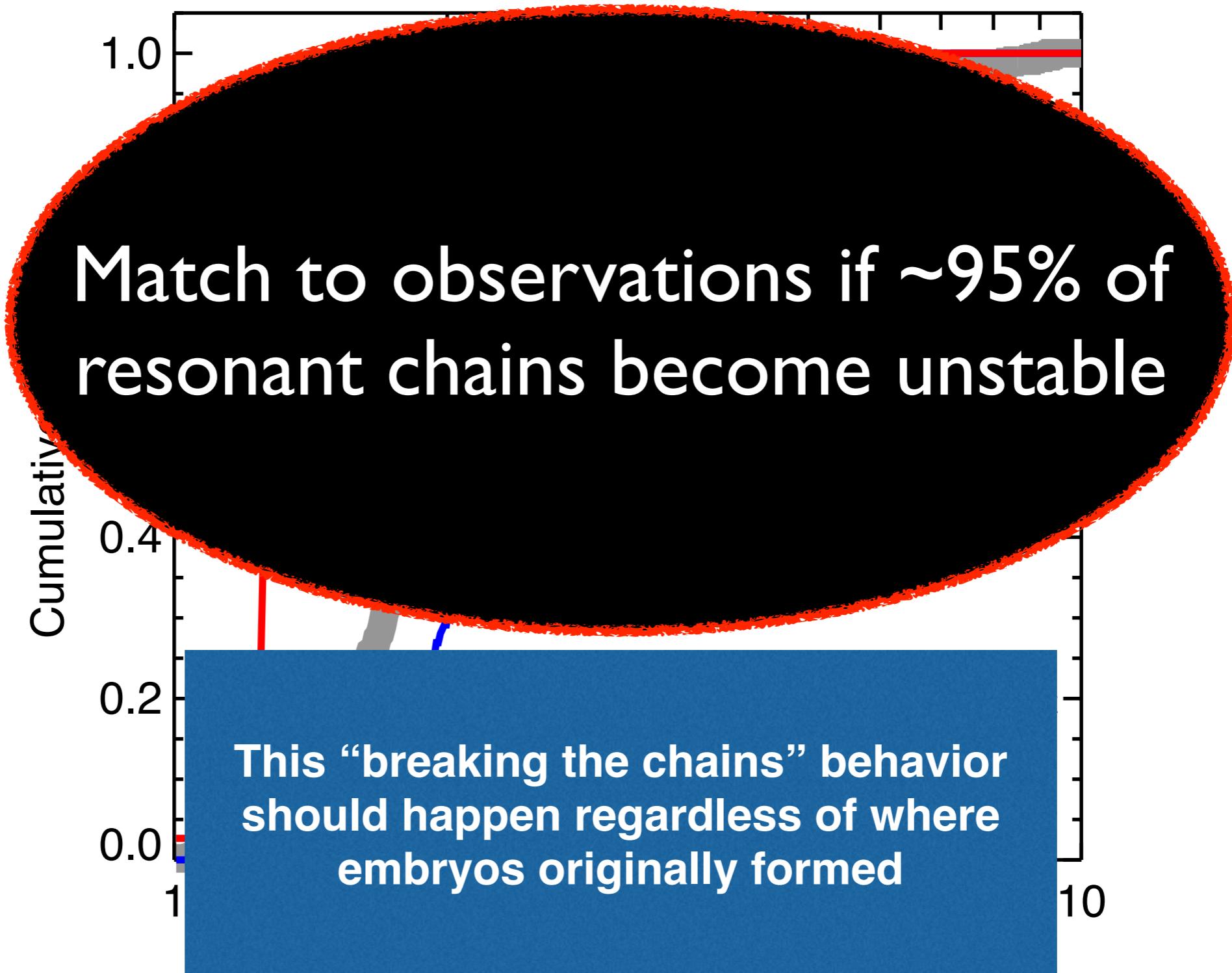


~Mars-mass
(10% M_{Earth}) 5-10 M_{Earth}
Gaseous disk dissipates after a few
million years

The period ratio distribution

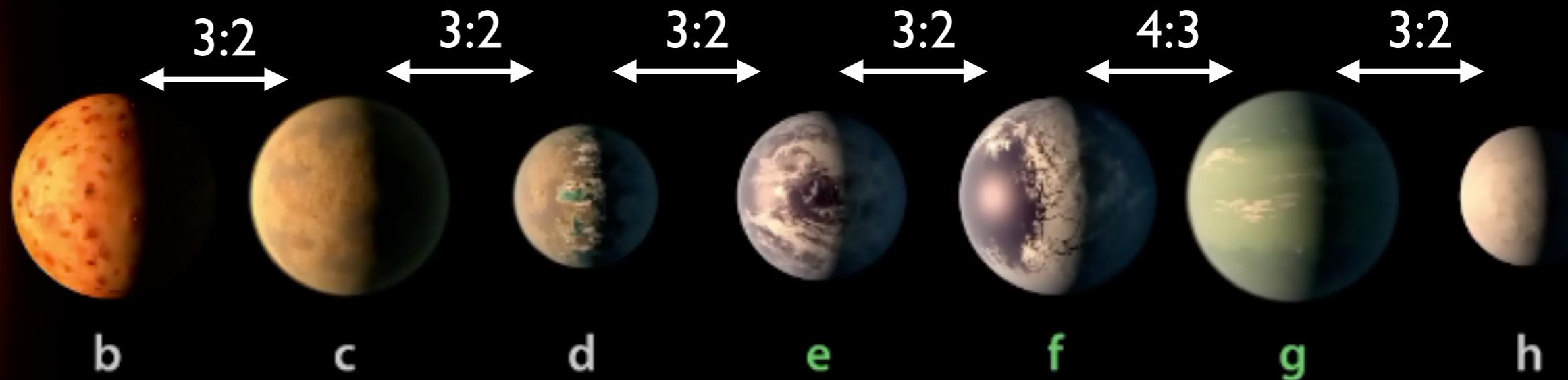


The period ratio distribution





TRAPPIST-1 System



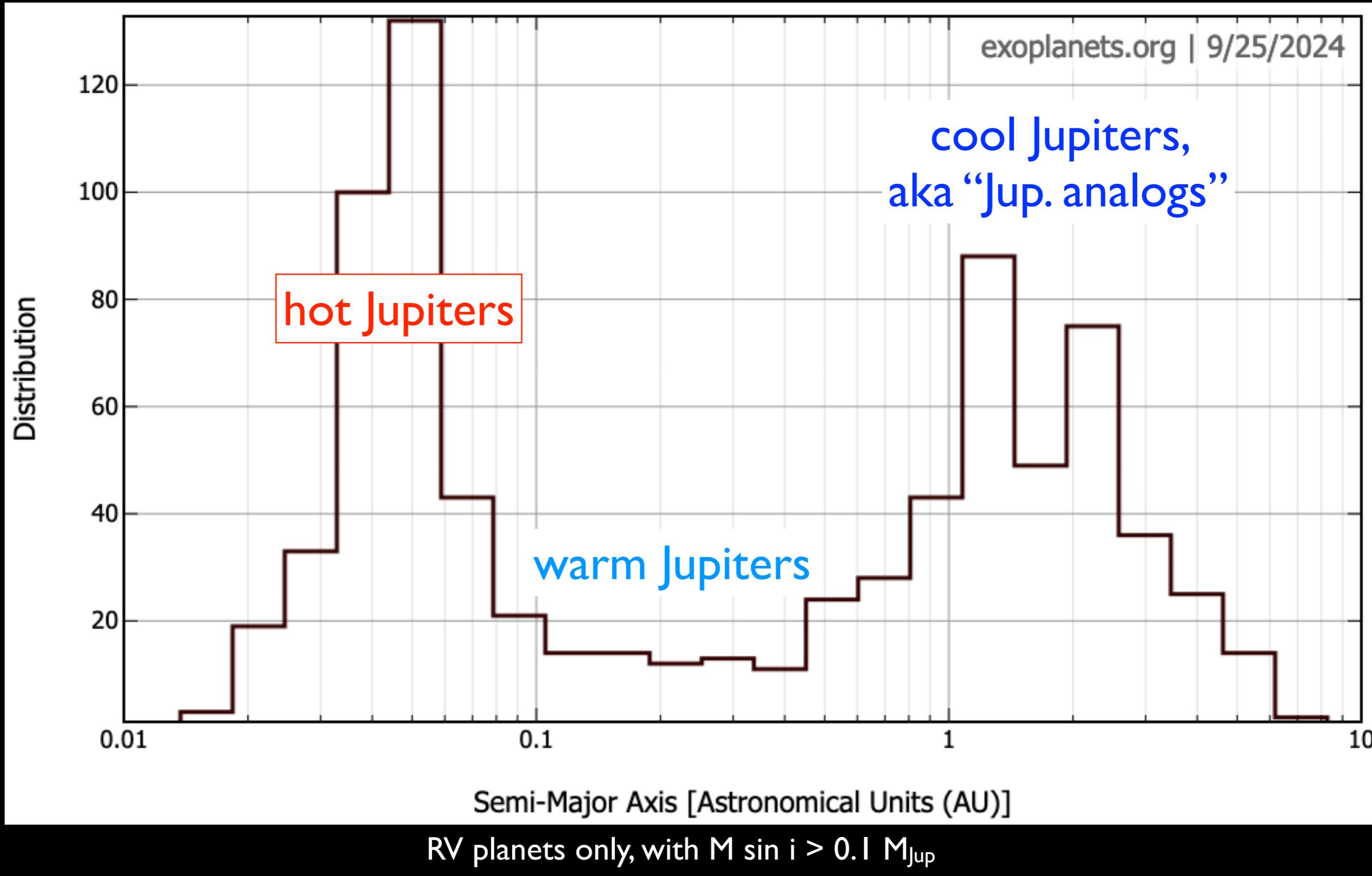
Illustration

(Gillon et al 2017, Luger et al 2017)

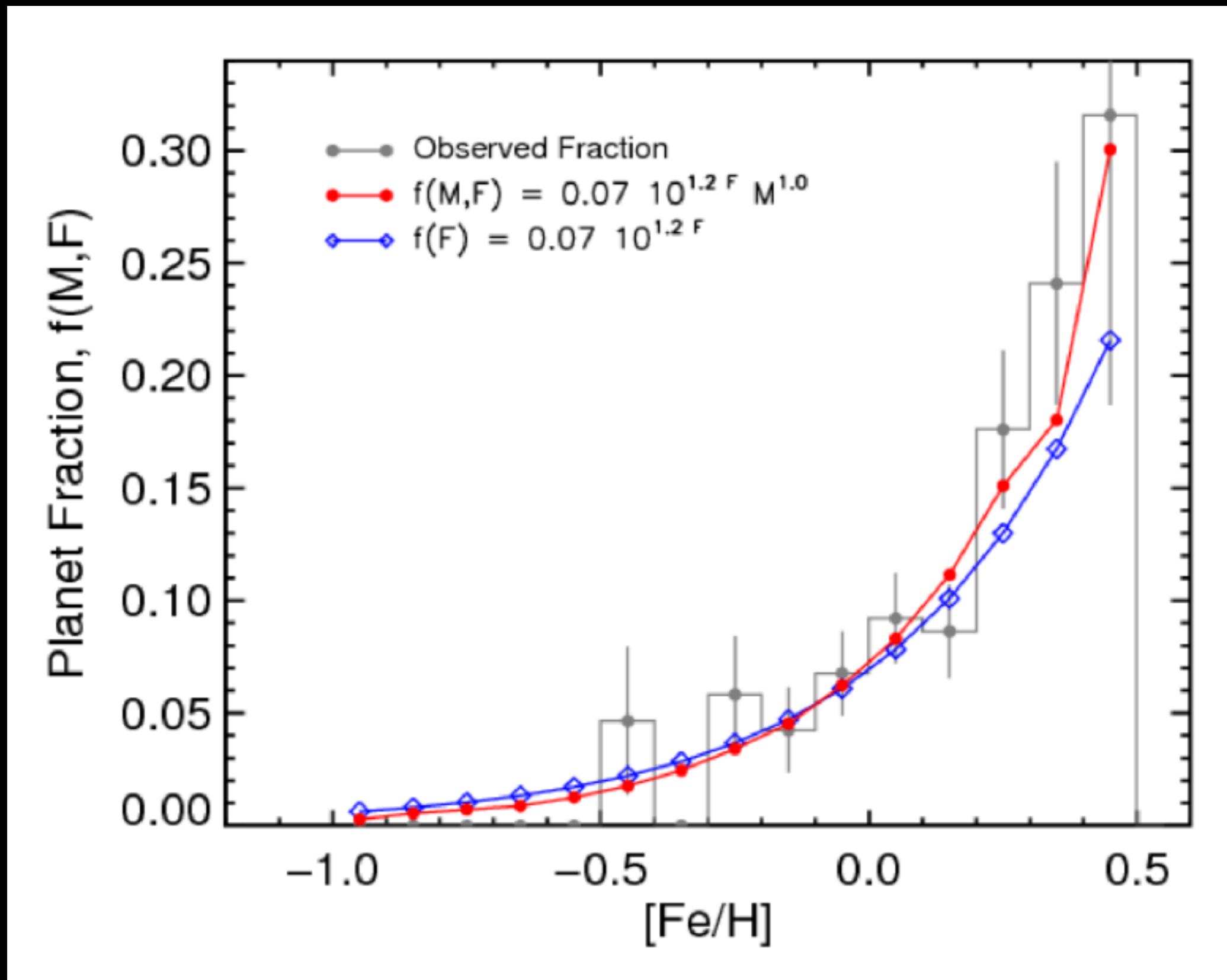
Giant (exo)planets



Radial distribution of gas giants



Giant planet-metallicity correlation



Johnson et al (2010); also Gonzalez (1997); Santos et al (2003); Fischer & Valenti (2005)

Formation models for giant planets

- Disk instability
- Core accretion



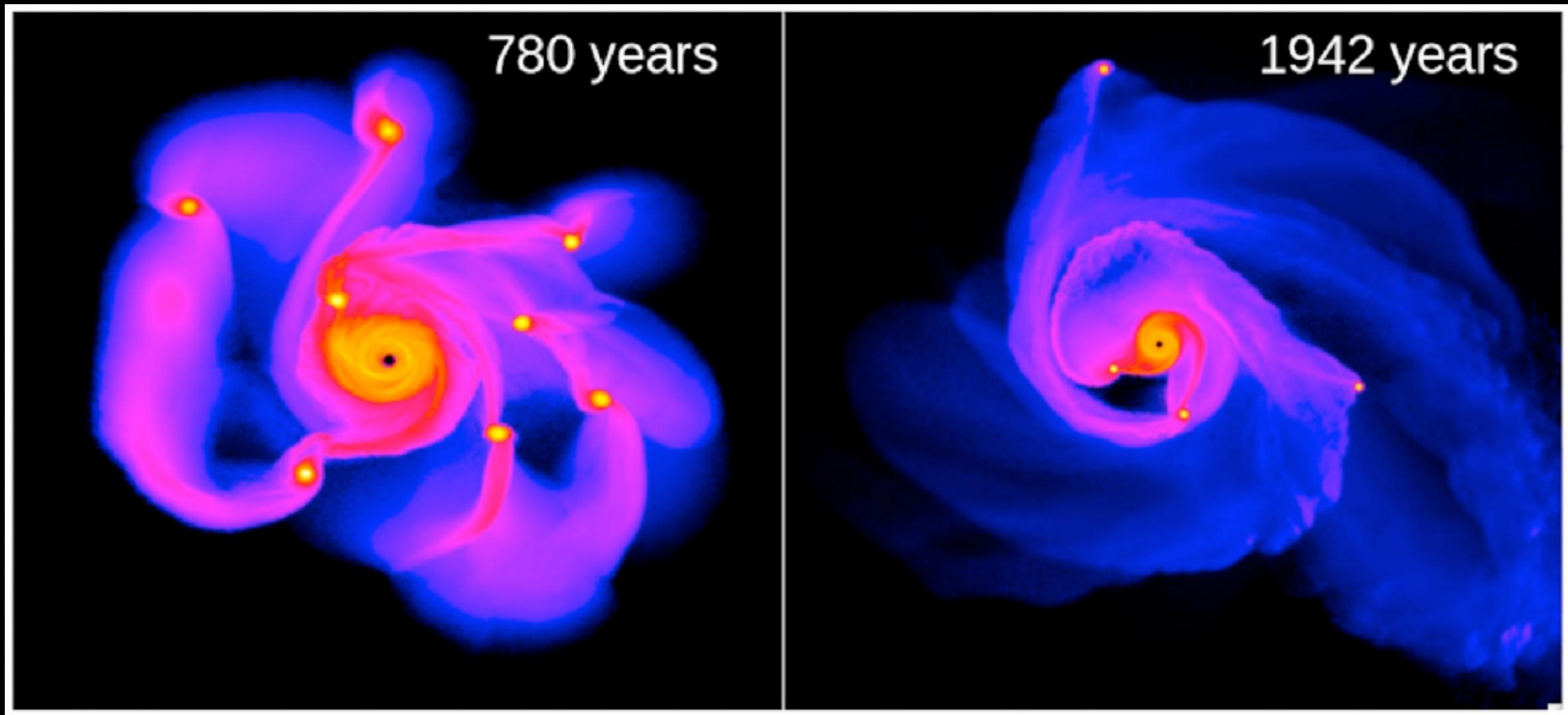
Disk instability

- Requires a region in the disk to be Toomre unstable

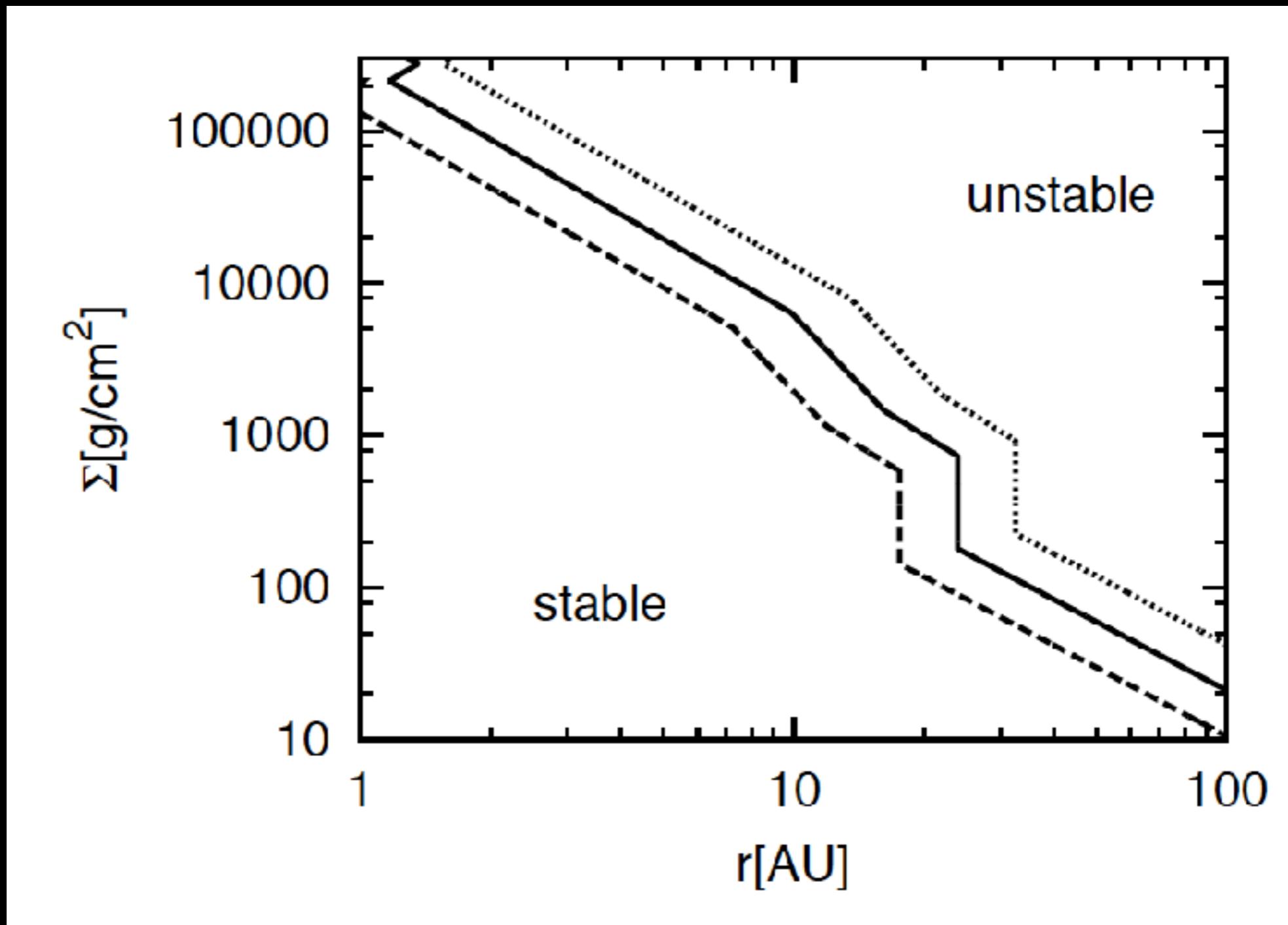
$$Q \equiv \frac{c_s \Omega}{\pi G \Sigma} < Q_{\text{crit}} \simeq 1$$

The diagram shows the Toomre Q factor formula: $Q \equiv \frac{c_s \Omega}{\pi G \Sigma} < Q_{\text{crit}} \simeq 1$. Three arrows point from labels to the formula: "sound speed" points to c_s , "orbital frequency" points to Ω , and "surface density" points to Σ .

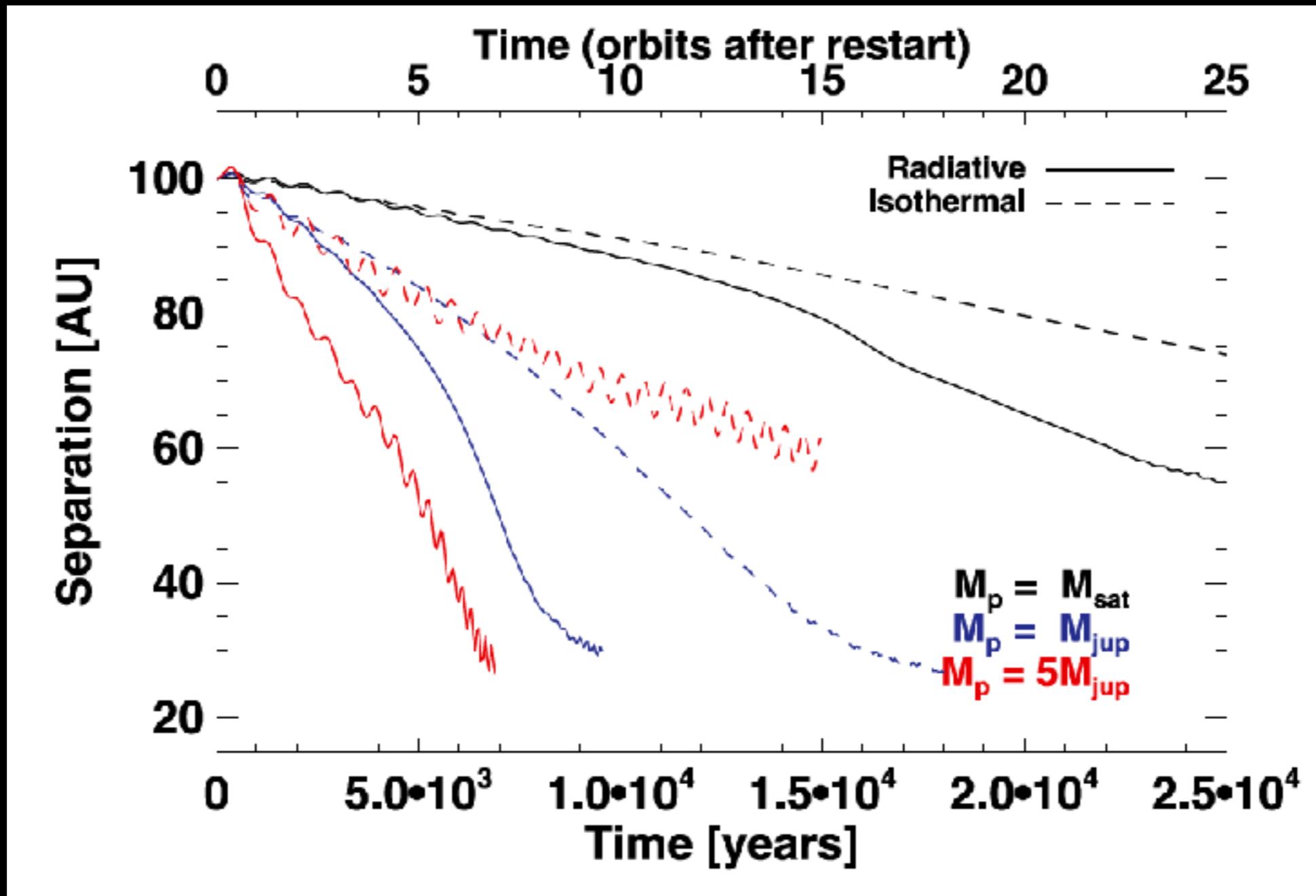
Disk instability



Gravitational instability: only important for massive wide-orbit planets

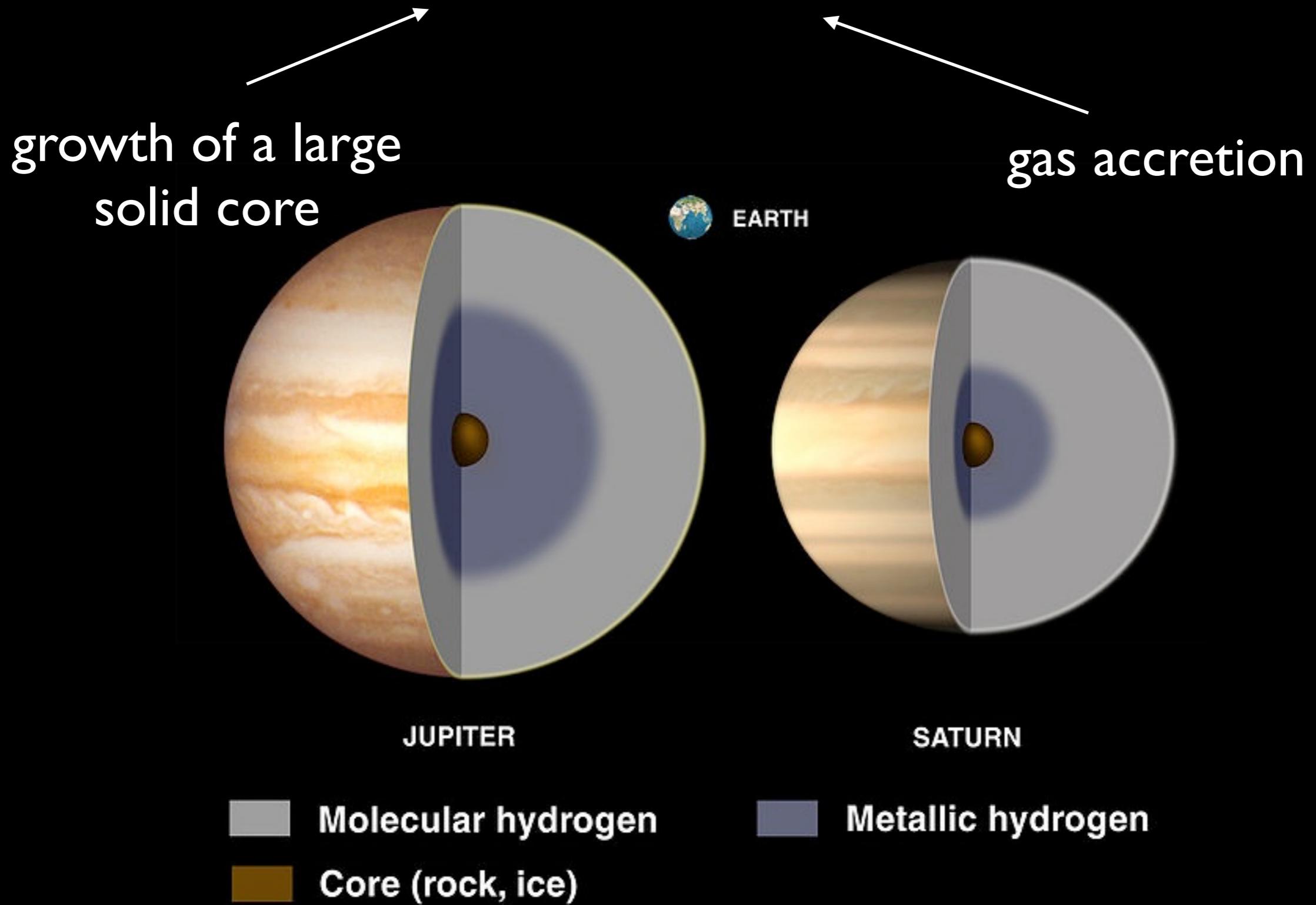


Clumps formed by disk instability migrate inward rapidly



Baruteau et al (2012);
“tidal downsizing hypothesis” by Nayakshin (2010)

Core accretion

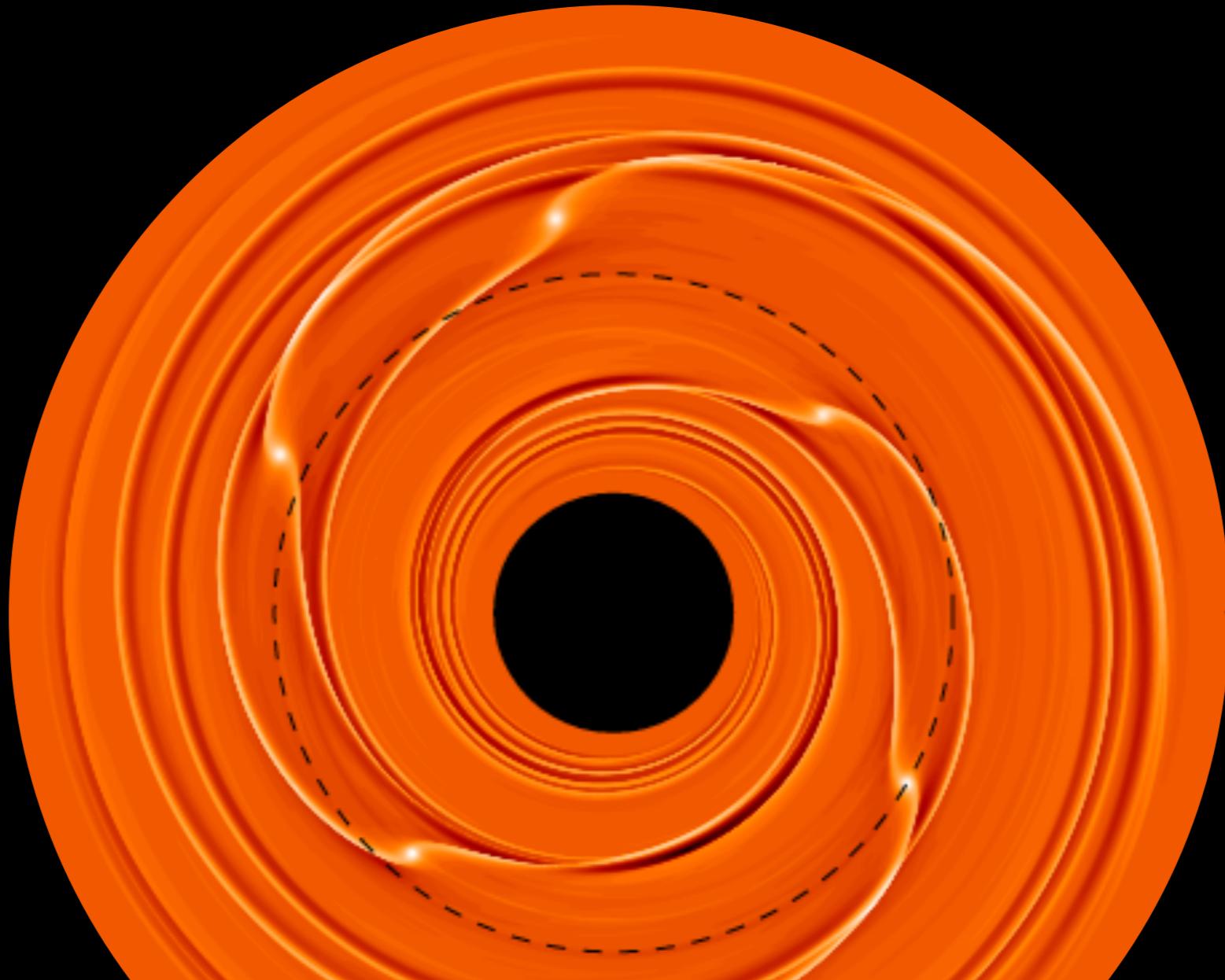


Core migration accretion

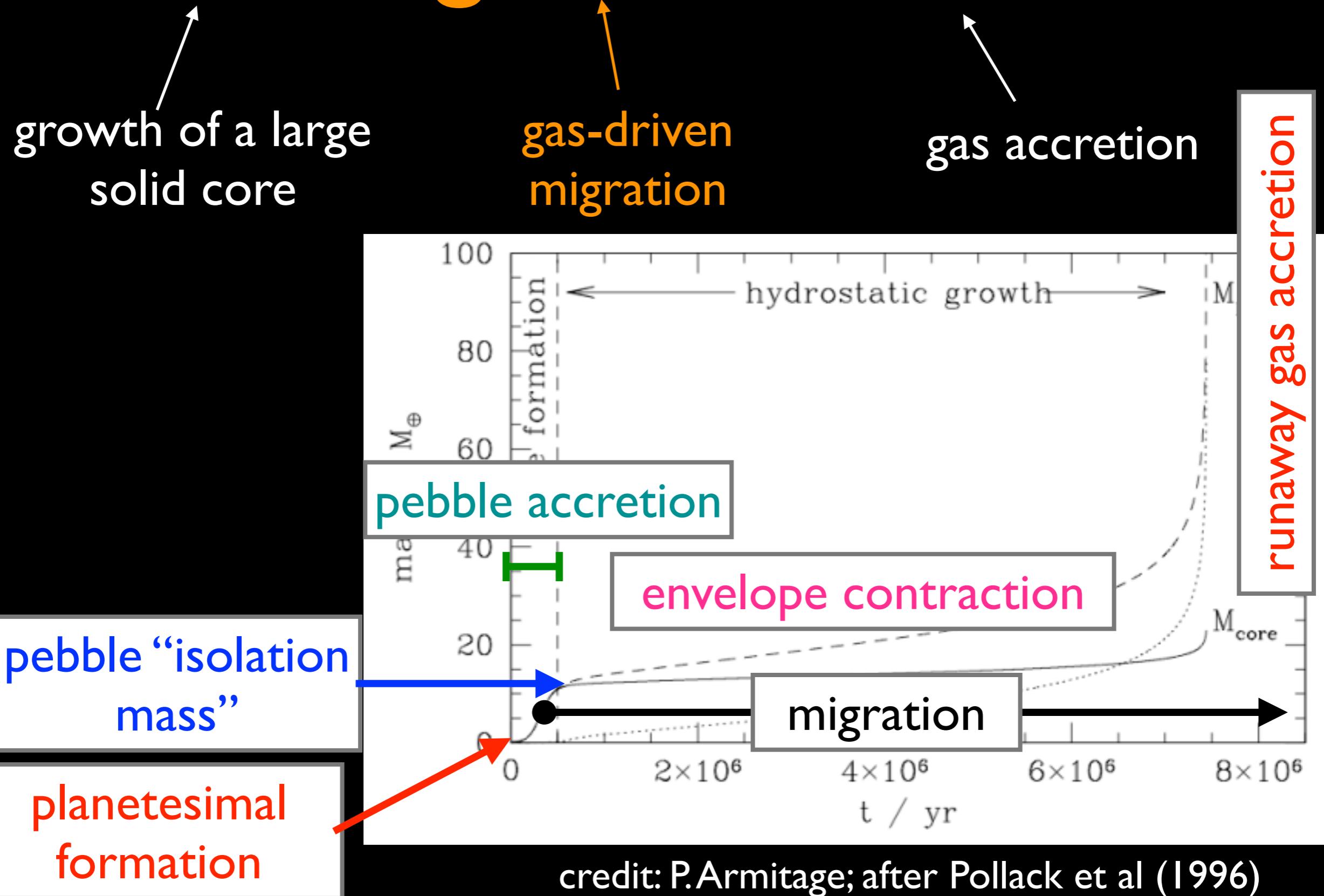
↑
growth of a large solid core

↑
gas-driven migration

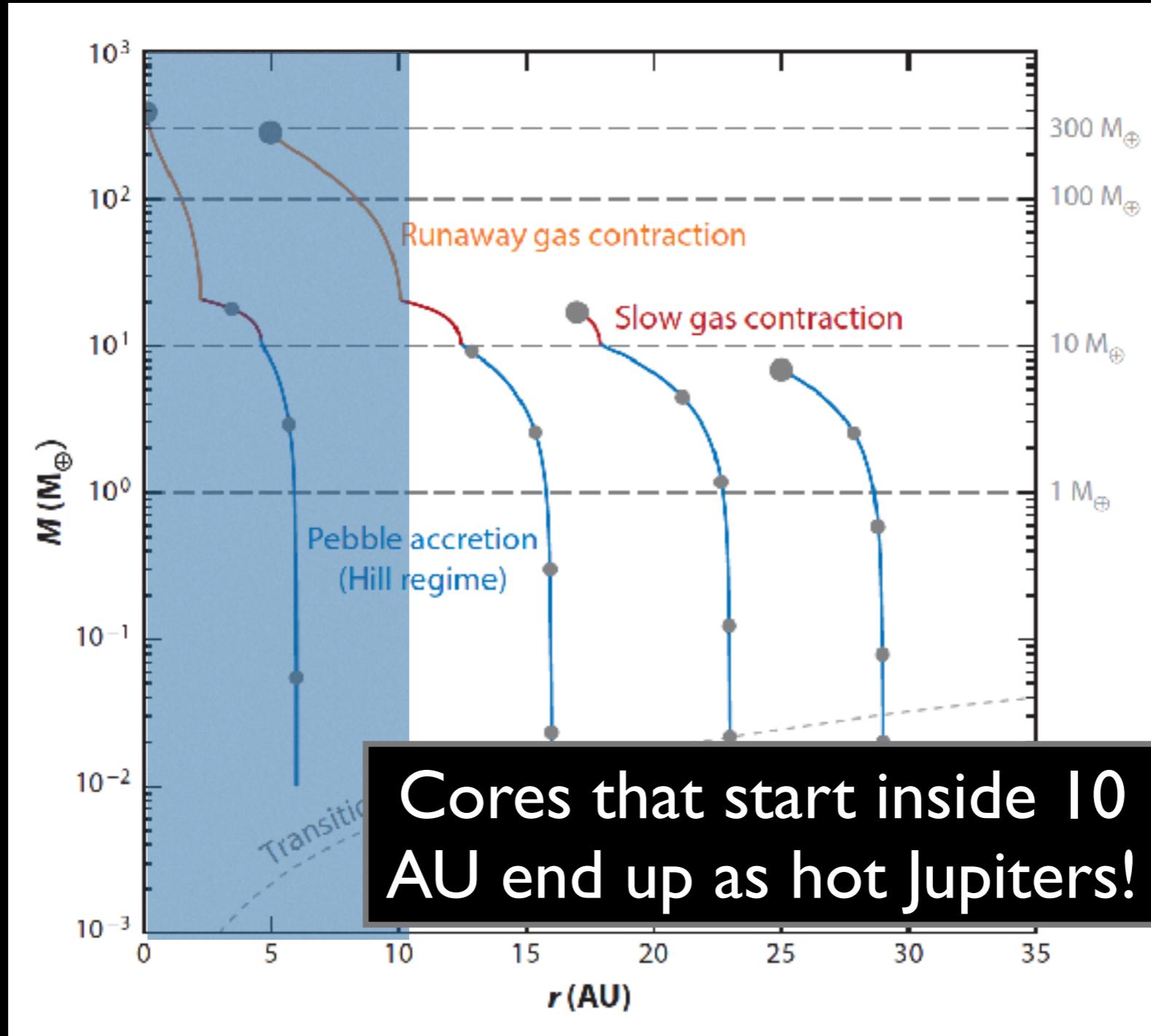
↑
gas accretion



Core migration accretion



Growth/migration tracks with pebble accretion



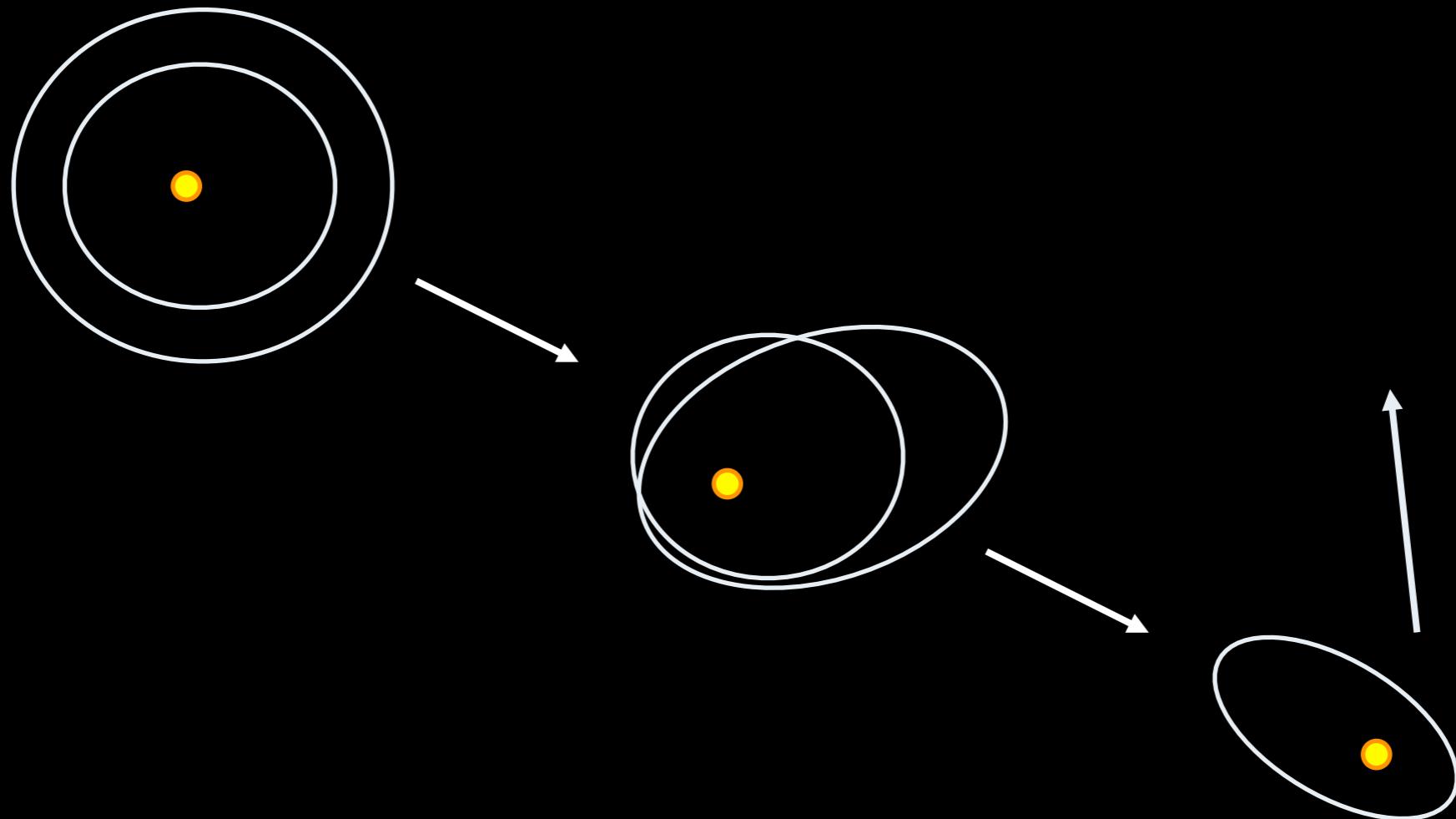
Johansen & Lambrechts (2017); after Bitsch et al (2015)

How did Jupiter end up at 5 AU?

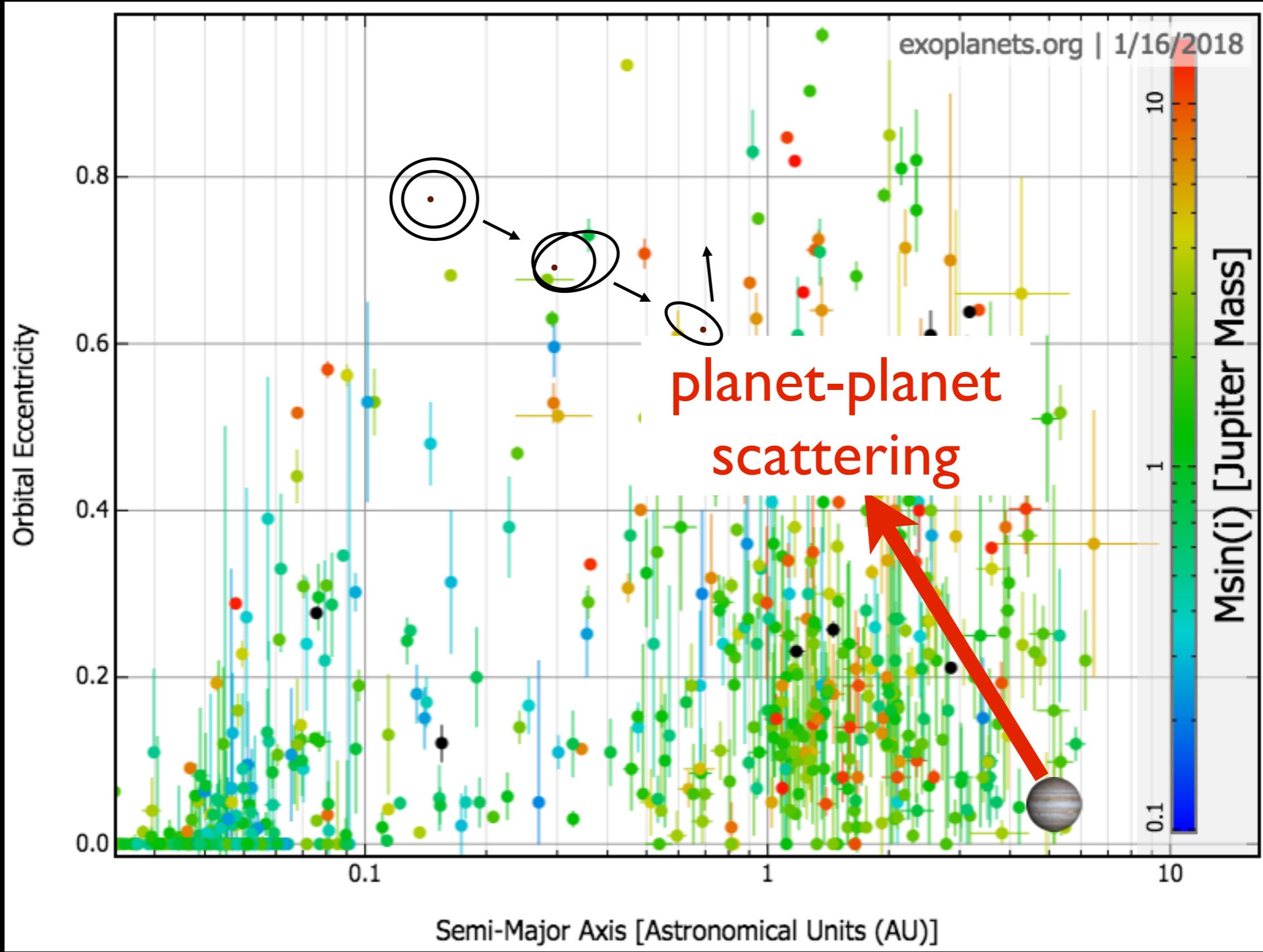
- Jupiter's core formed at 15-20 AU (Bitsch et al 2015)
- Very low viscosity disks: very slow type 2 migration (e.g., Bitsch et al 2019; Griveaud et al 2024)
- Inner disk evaporated away, planets couldn't migrate closer than \sim 1 AU (Alexander & Pascucci 2012)
- Saturn stopped or reversed Jupiter's migration (Masset & Snellgrove 2001; Grand Tack model)



The giant exoplanet eccentricity distribution: planet-planet scattering

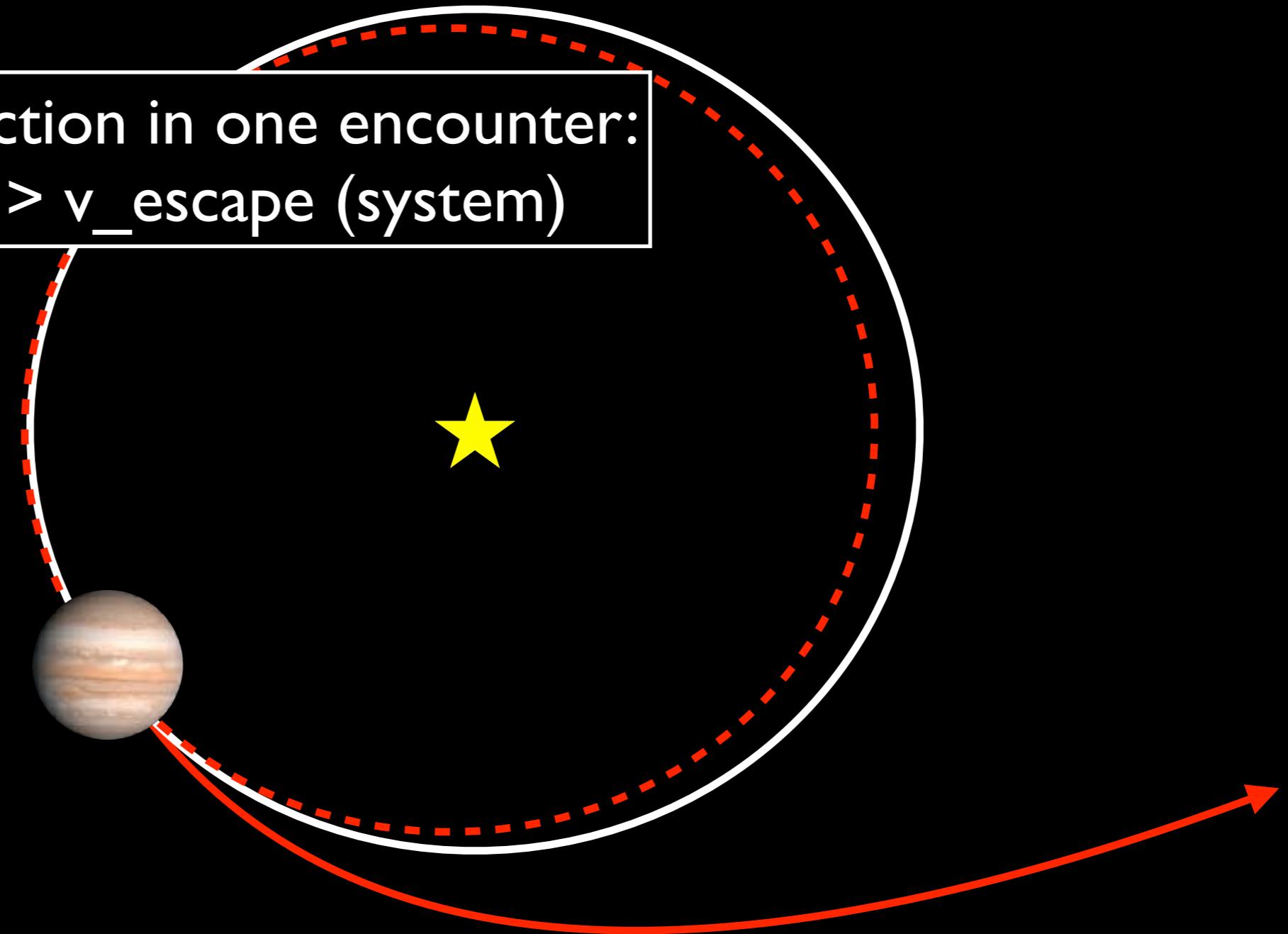


Giant exoplanets



Scattering vs accretion

Requirement for ejection in one encounter:
 $v_{\text{escape}}(\text{planet}) > v_{\text{escape}}(\text{system})$



The “Safronov number”: scattering vs accretion

- Ratio of escape speed from planet’s surface to escape speed from system at planet’s orbital radius

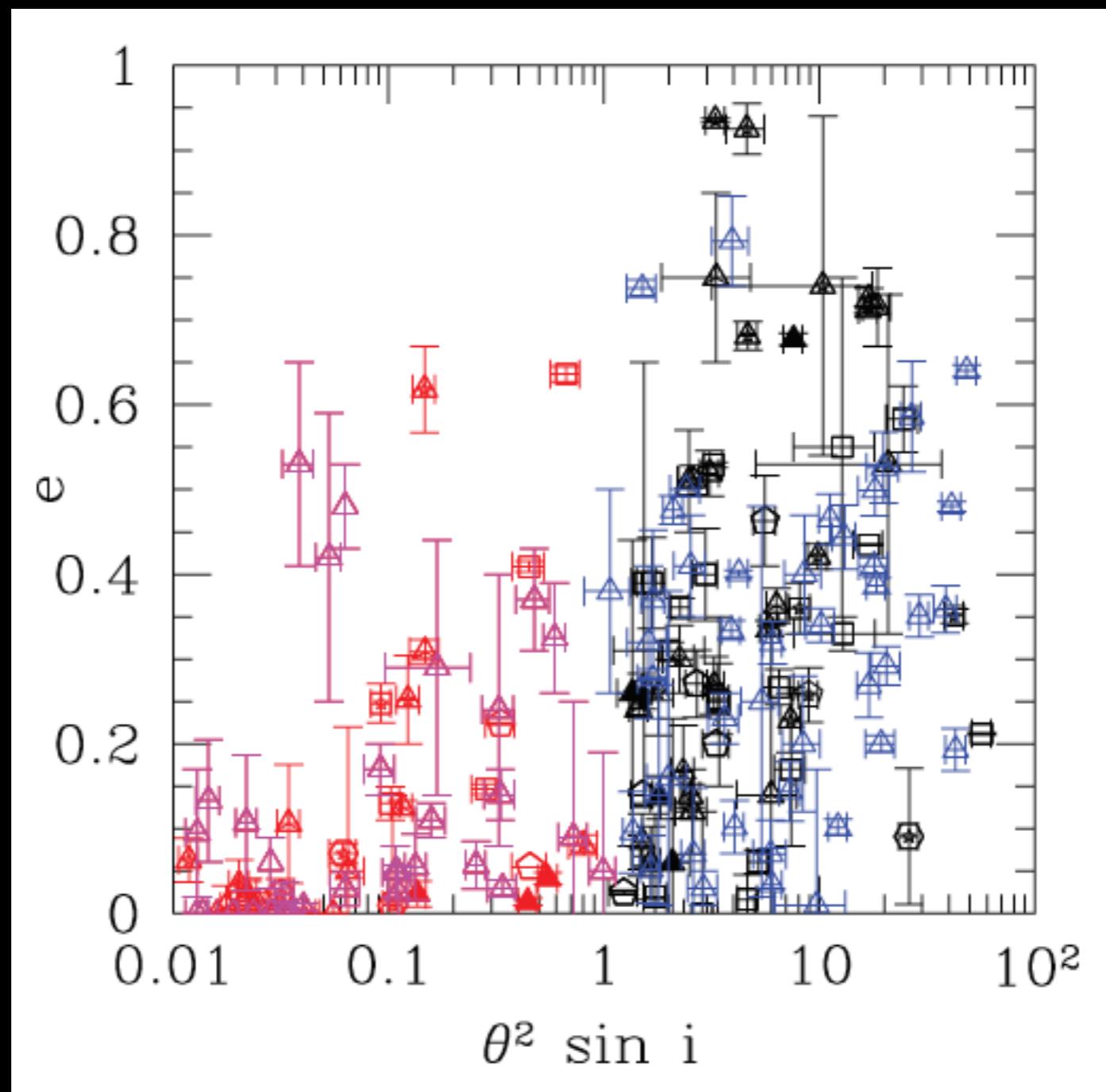
$$\begin{aligned}\theta^2 &\equiv \left(\frac{Gm}{R_p}\right) \left(\frac{r}{GM_*}\right) \\ &= 10 \left(\frac{m}{M_J}\right) \left(\frac{M_\odot}{M_*}\right) \left(\frac{R_J}{R_p}\right) \left(\frac{r}{5 \text{ AU}}\right).\end{aligned}$$

The “Safronov number”: scattering vs accretion

- $\text{Saf} > 1$: high-mass or distant planets — **scattering**
- $\text{Saf} < 1$: low-mass or close-in planets — **accretion**

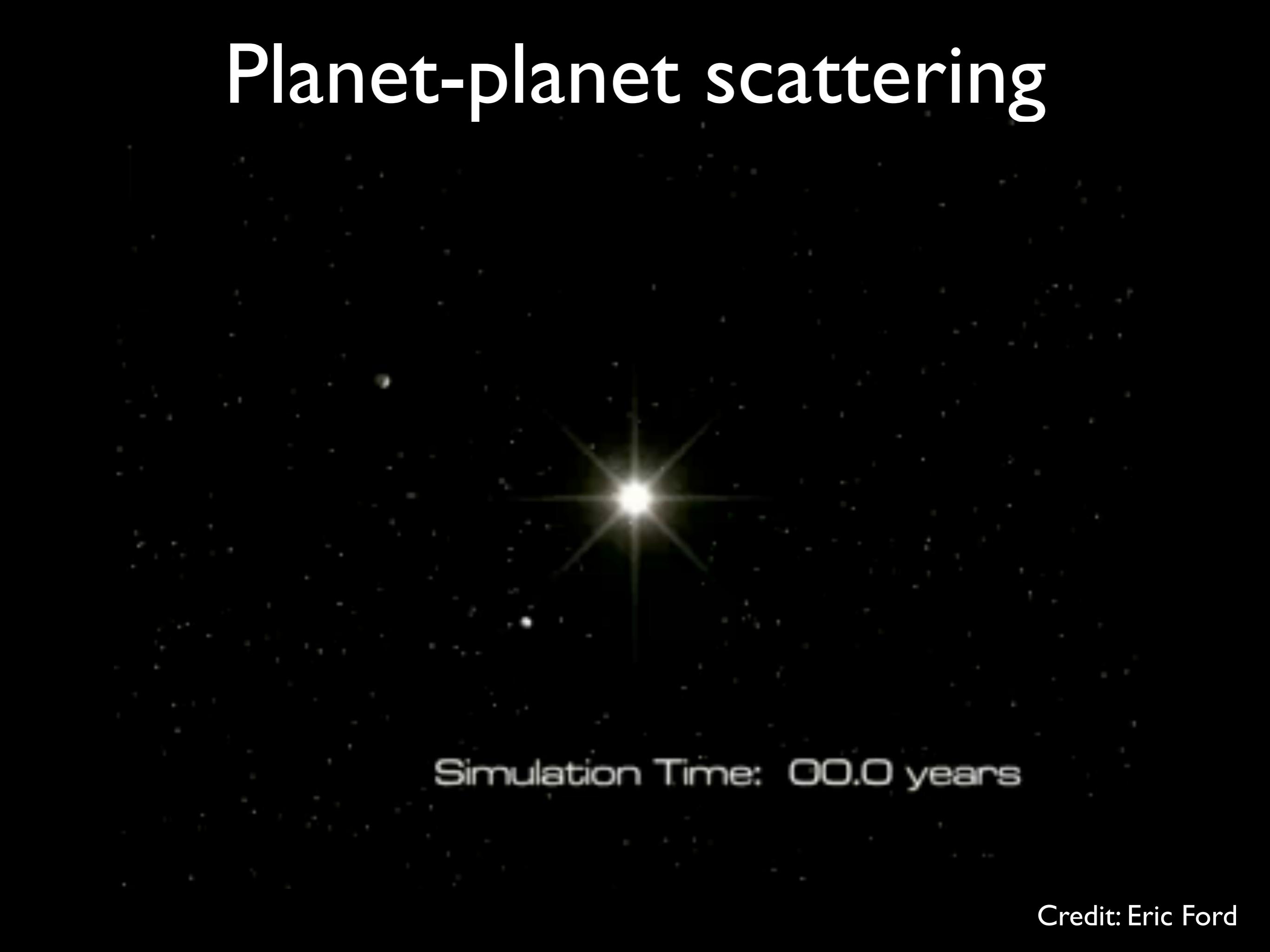
$$\begin{aligned}\theta^2 &\equiv \left(\frac{Gm}{R_p}\right) \left(\frac{r}{GM_\star}\right) \\ &= 10 \left(\frac{m}{M_J}\right) \left(\frac{M_\odot}{M_\star}\right) \left(\frac{R_J}{R_p}\right) \left(\frac{r}{5 \text{ AU}}\right).\end{aligned}$$

Giant planet eccentricities correlate with Safronov#



Ford & Rasio (2008)

Planet-planet scattering



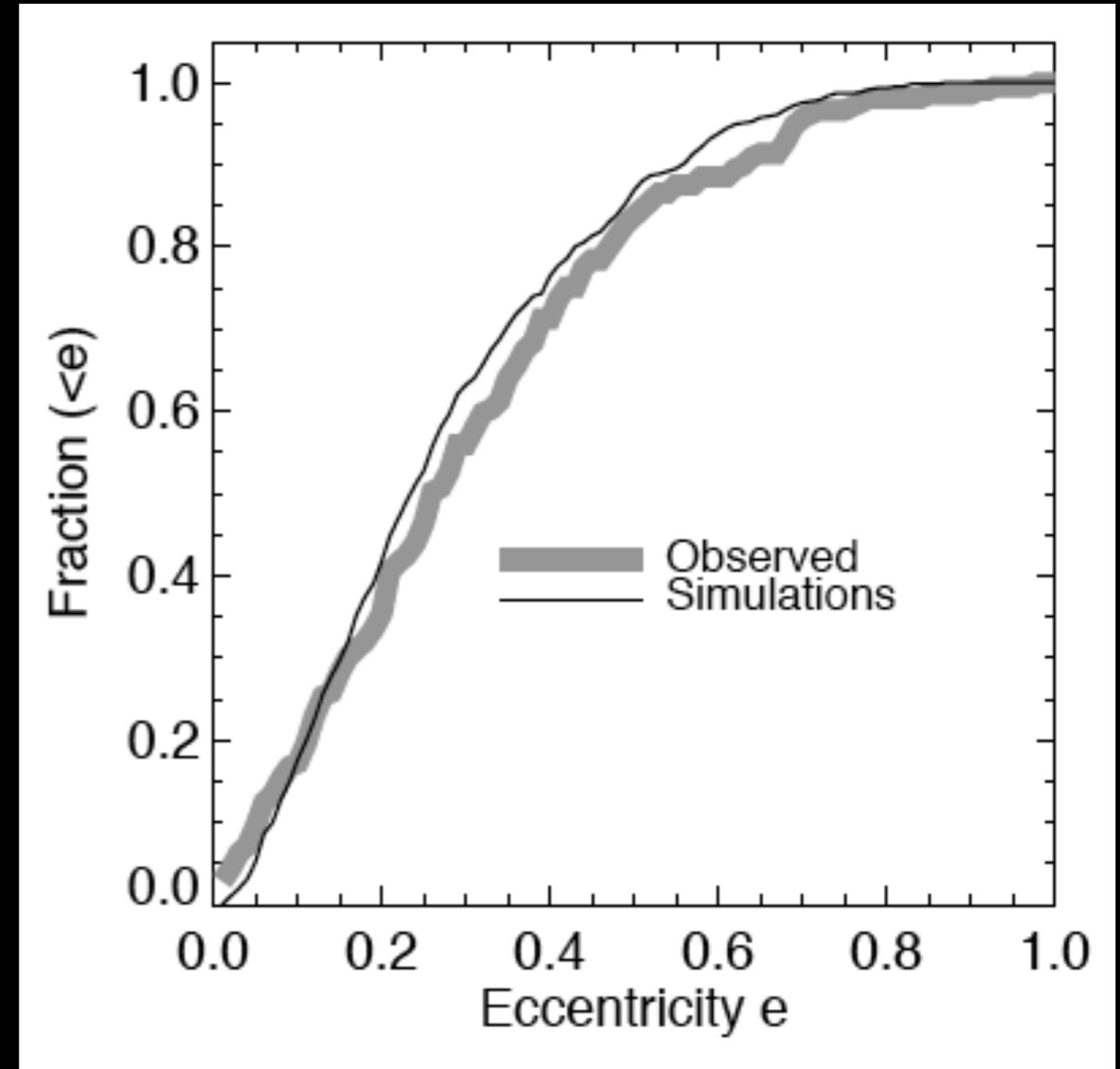
Simulation Time: 00.0 years

Credit: Eric Ford

Survivors of planet-planet scattering match the eccentricity distribution

To fit eccentricity distribution, 75-95% of giant exoplanet systems must be survivors of instability

(Juric & Tremaine 2008; Chatterjee et al 2008; Raymond et al 2010)

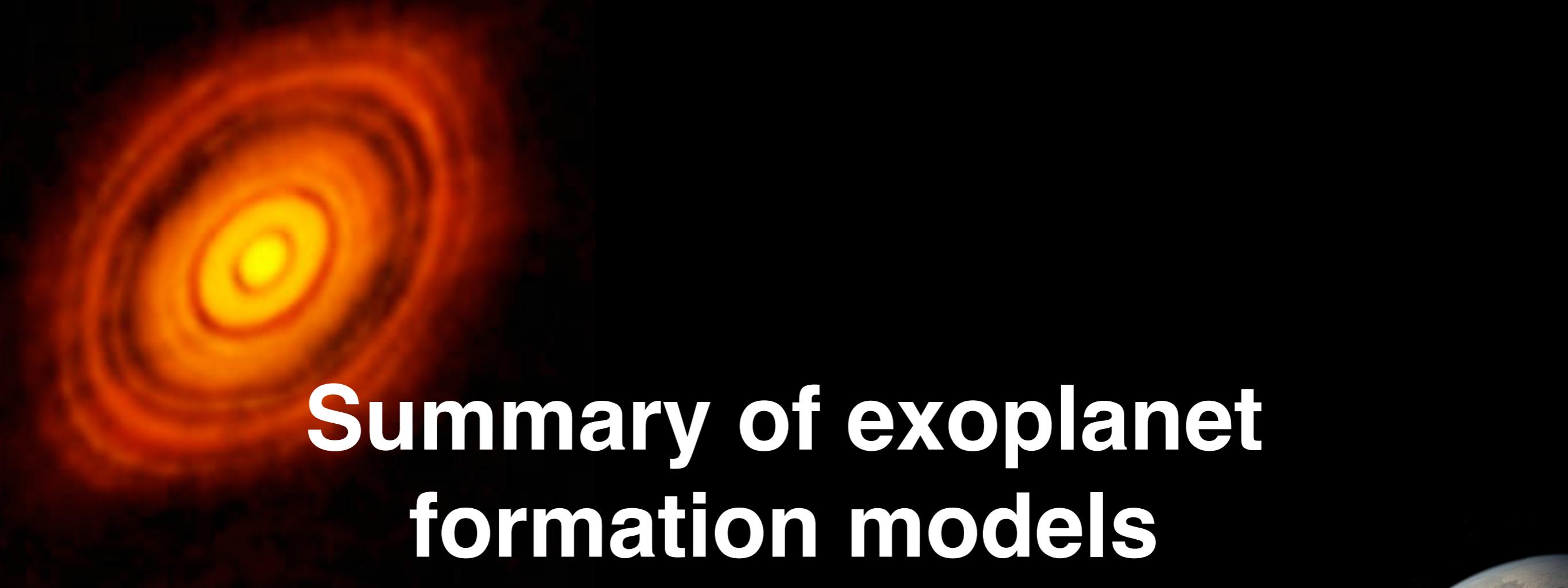


Raymond et al (2009)

Planet-planet scattering generates free-floating planets



Several hundred FFPs known to date (typically Jupiters)
[e.g., Mroz et al 2017, Kirkpatrick et al 2019, Miret-Roig et al 2022, Sumi et al 2023]



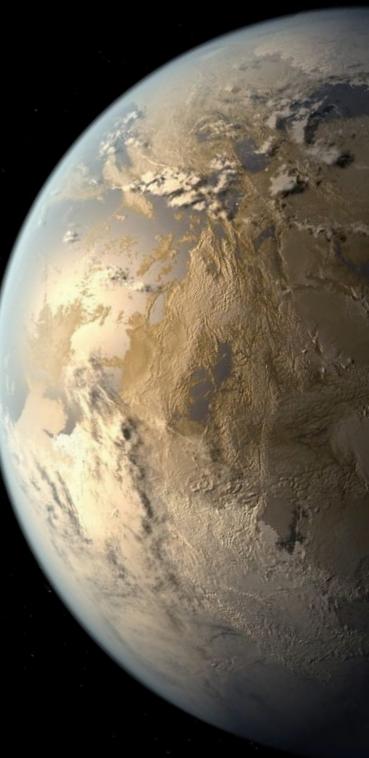
Summary of exoplanet formation models

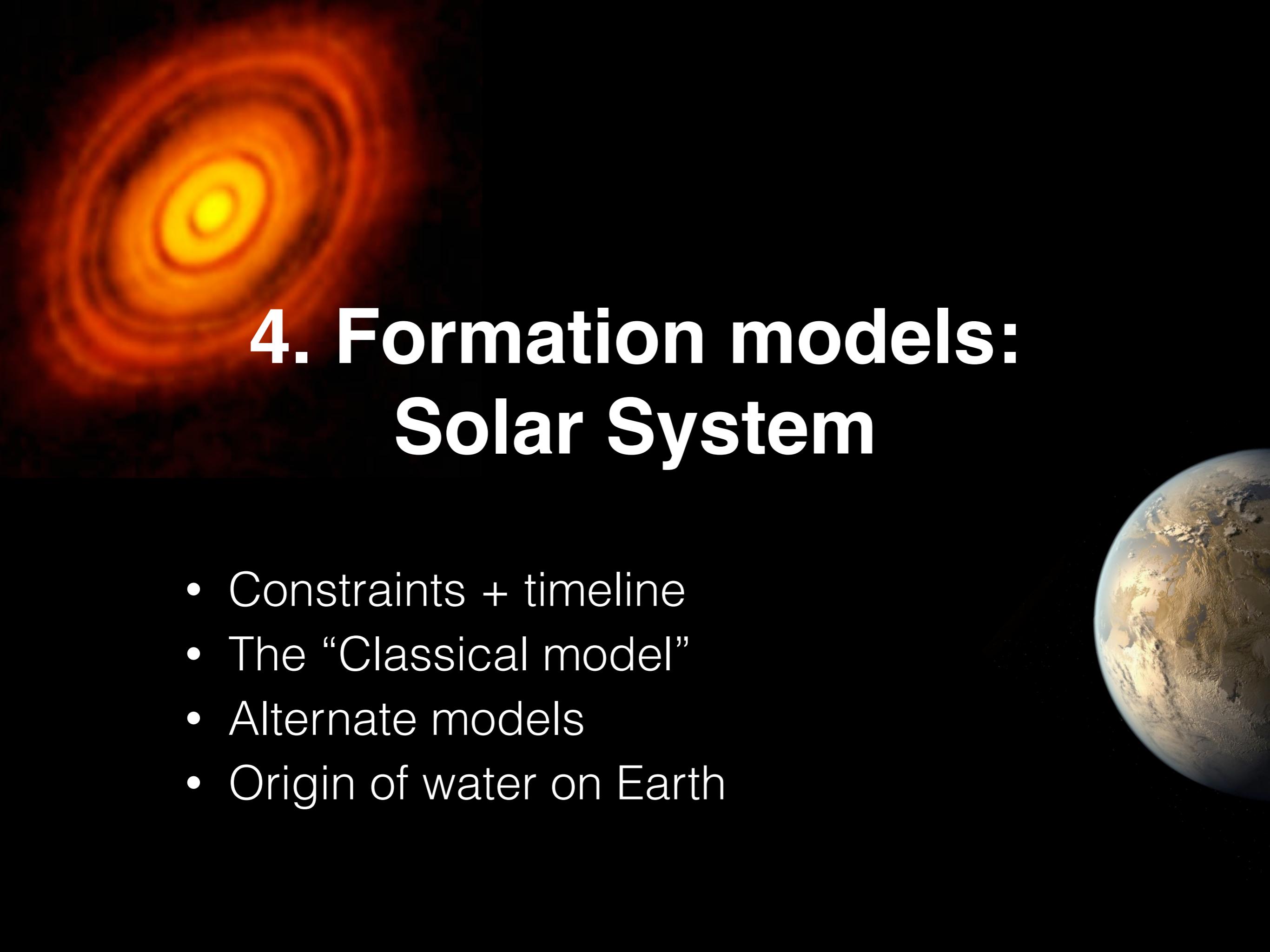
Close-in “super-Earths”

- In-situ growth impossible
- Migration then instability (“breaking the chains”)

Gas giants

- Disk instability only for outer high-mass planets
- Core-migration-accretion
- Planet-planet scattering





4. Formation models: Solar System

- Constraints + timeline
- The “Classical model”
- Alternate models
- Origin of water on Earth

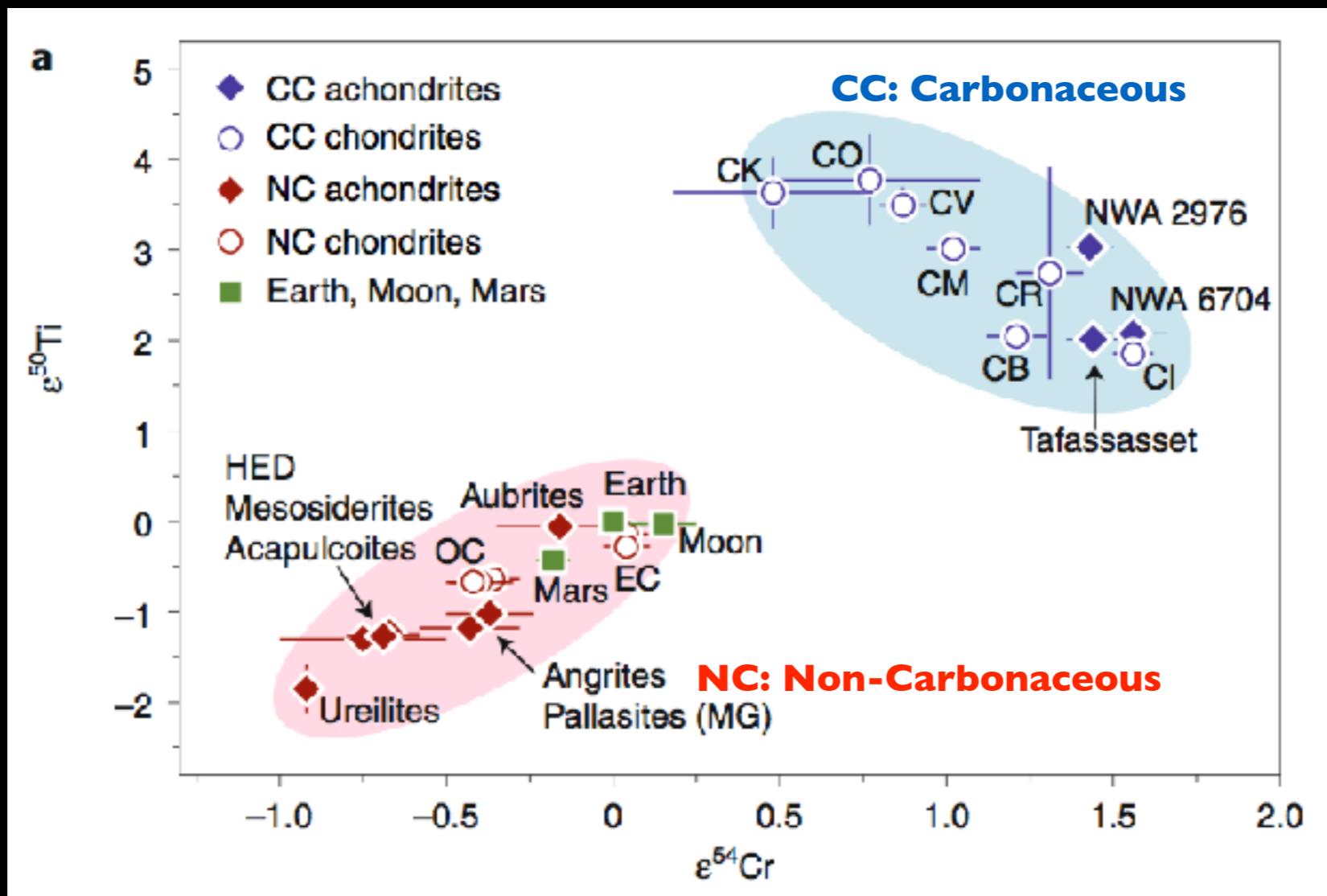
A few key events in Solar System history that (almost) everyone agrees upon...

rough time order

1. Planetesimals formed
2. Planetary embryos formed
3. Gas giants formed (and migrated)
4. Giant planet instability
5. Moon-forming impact

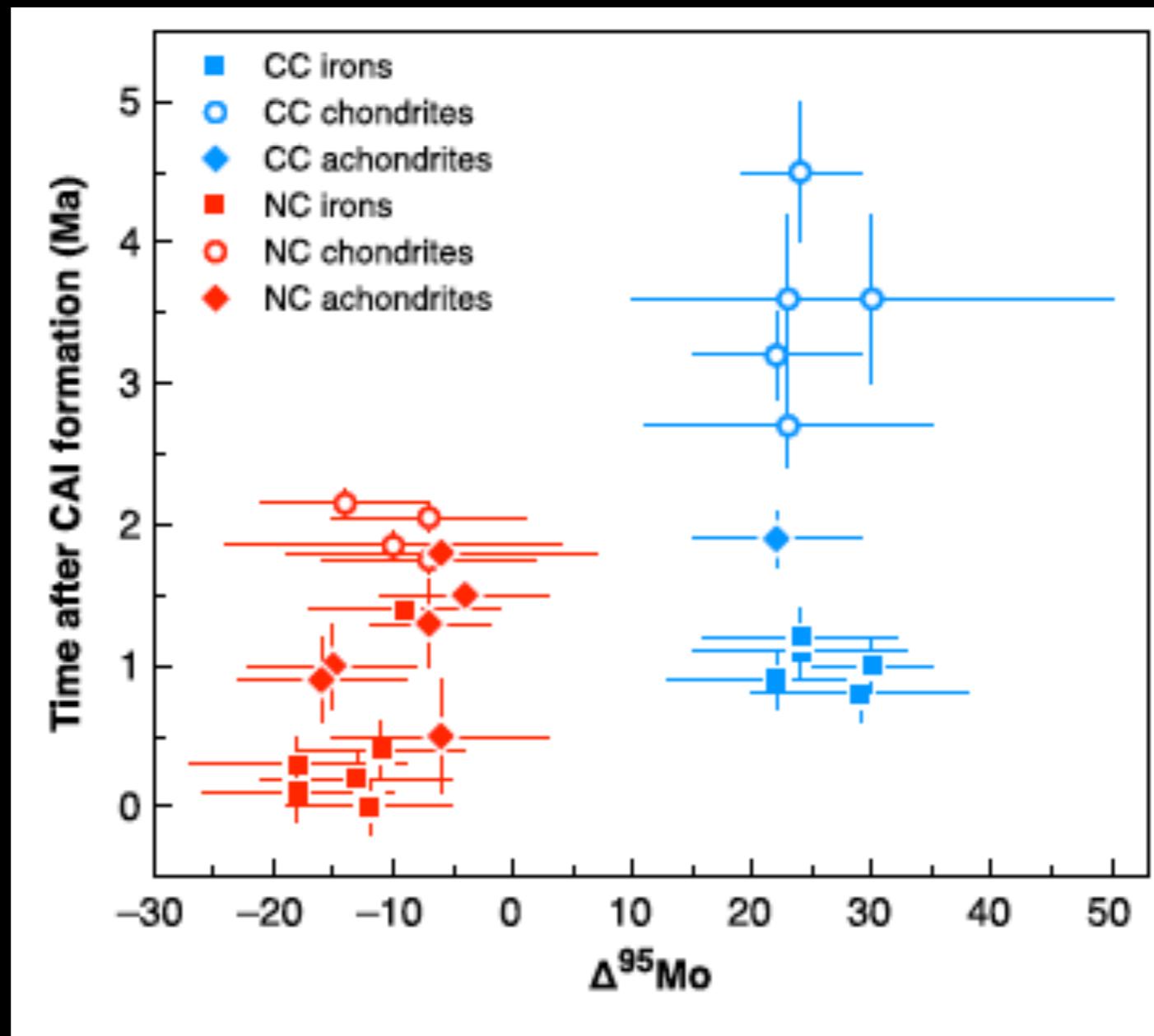


Key event I: formation of two classes of planetesimals



Did they form at different times or in different places?

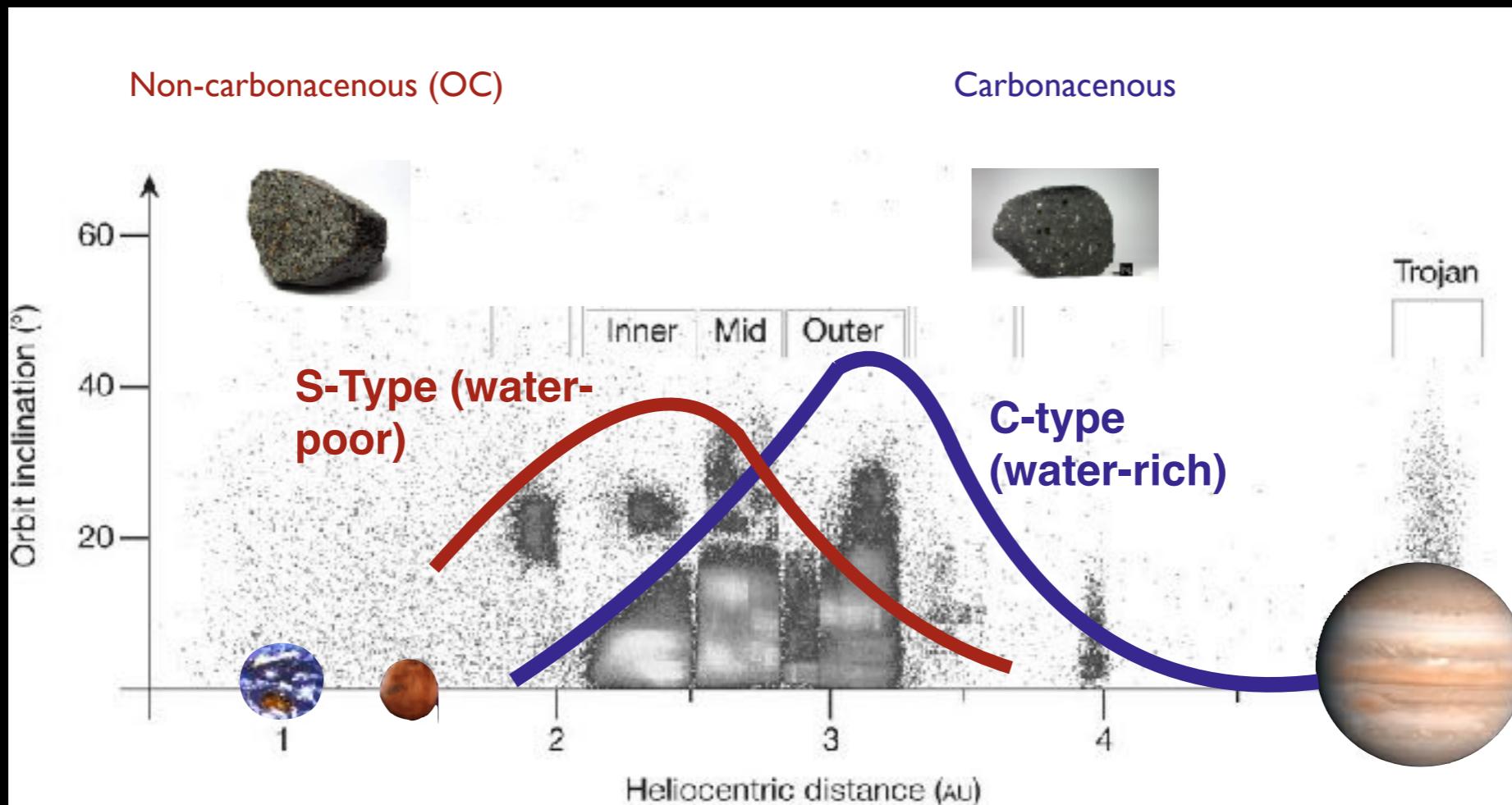
NC and CC planetesimals were forming at the same time



Kleine et al (2020)

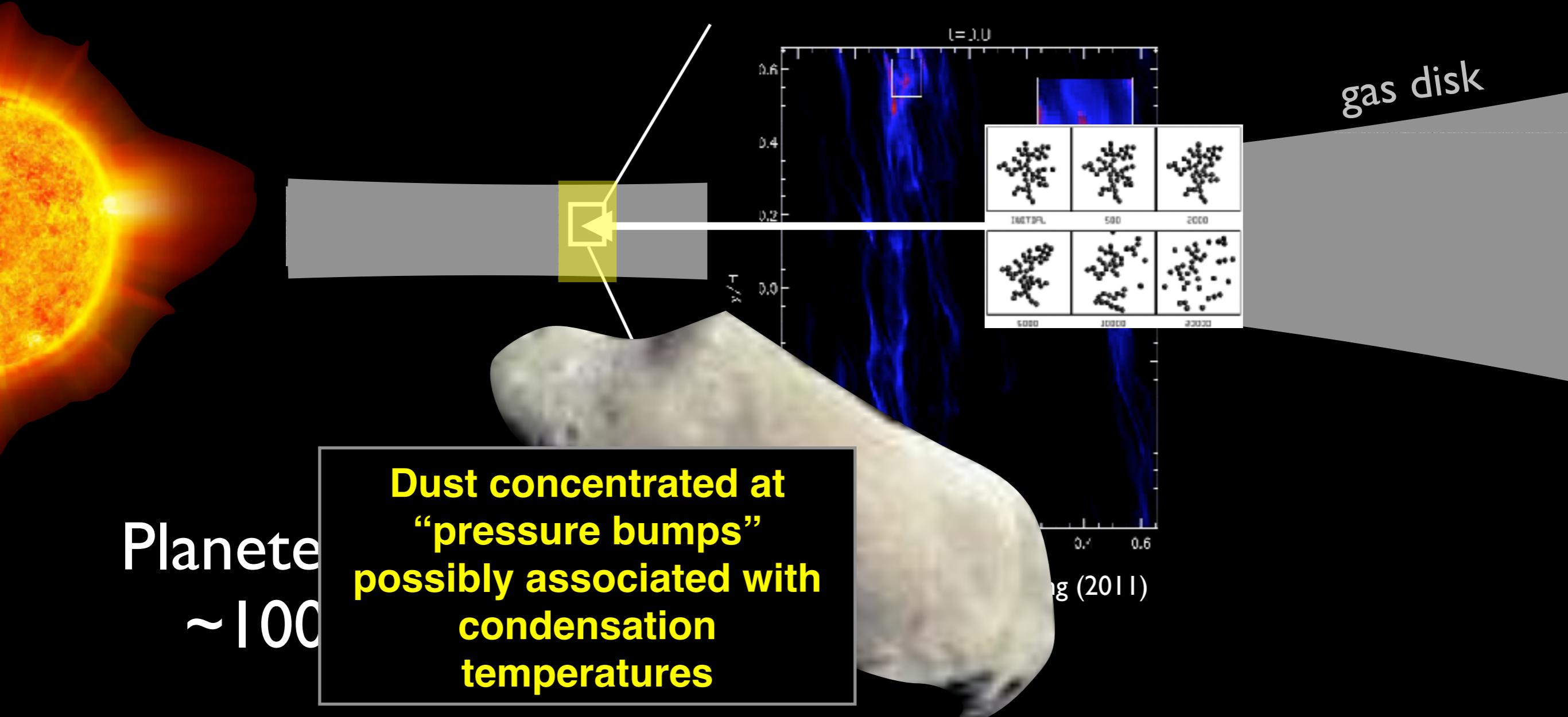
They formed in different places!

Surviving NC and CC planetesimals have overlapping orbits

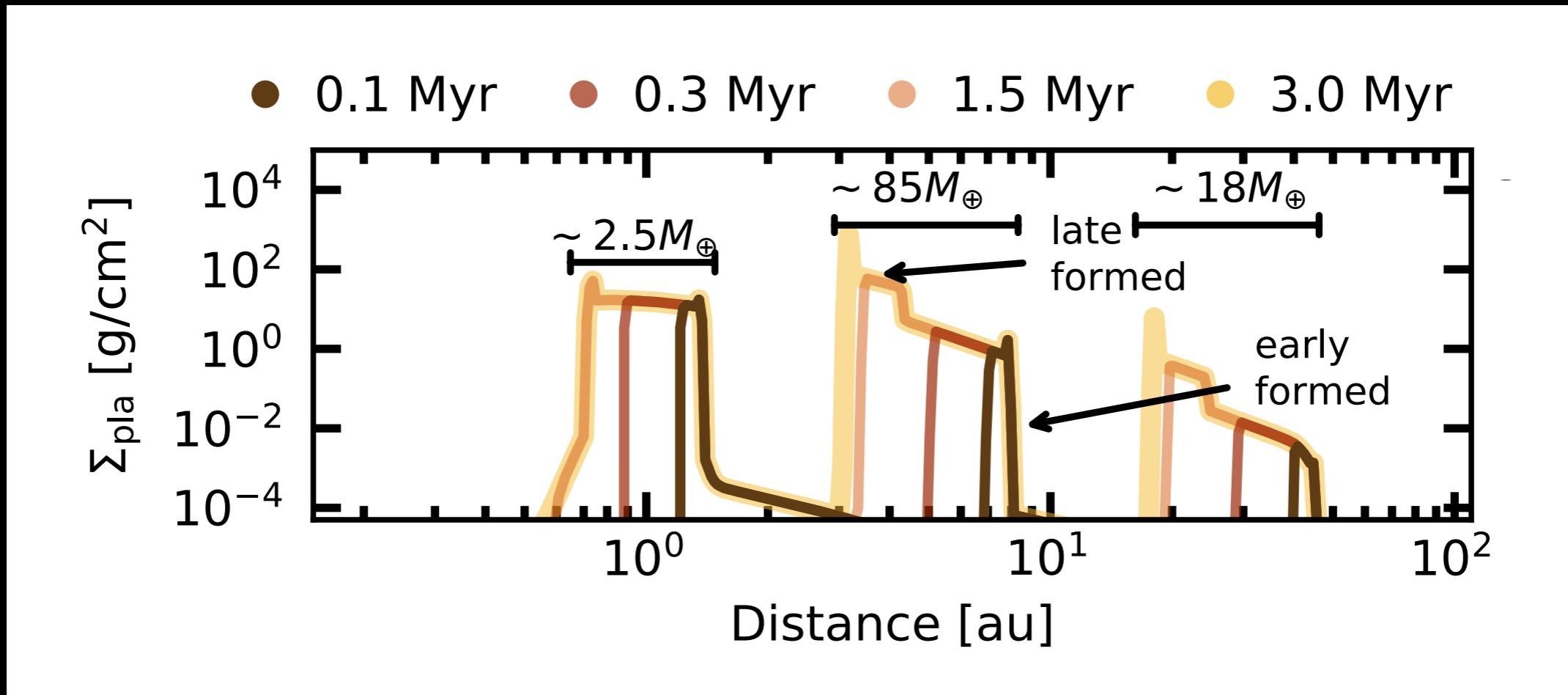


Gradie & Tedesco 1982; Demeo & Carry 2014

Planetesimal formation models: dust growth/drift with disk evolution

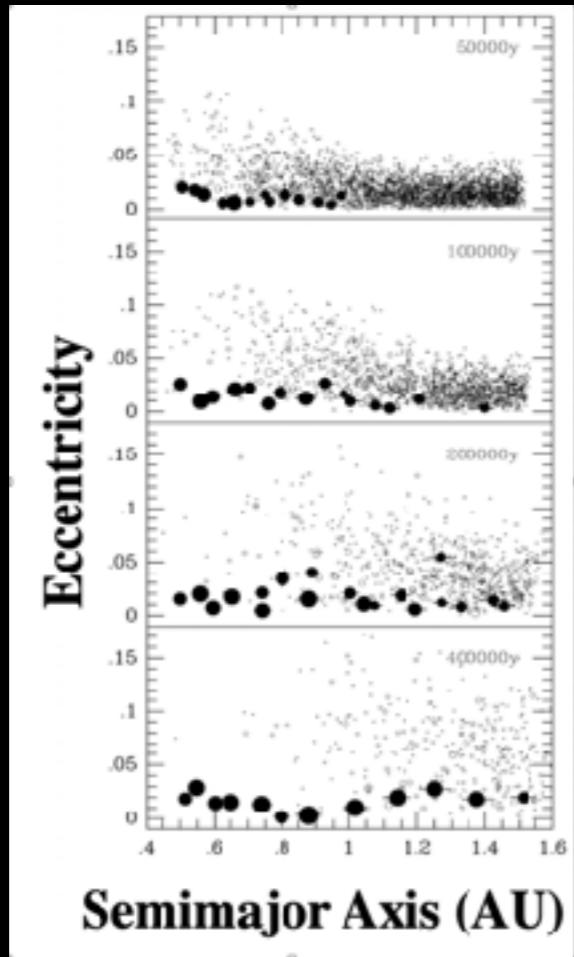


Three rings of planetesimals

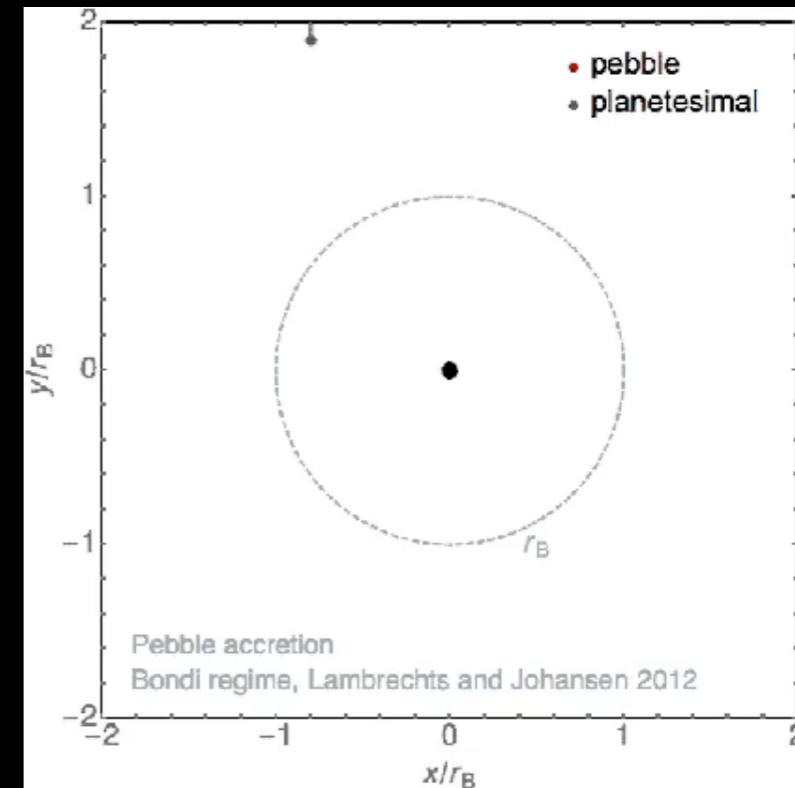


Key event 2: growth of *planetary embryos* and giant planet cores

inside snow line:
planetesimal accretion



beyond snow line:
pebble accretion

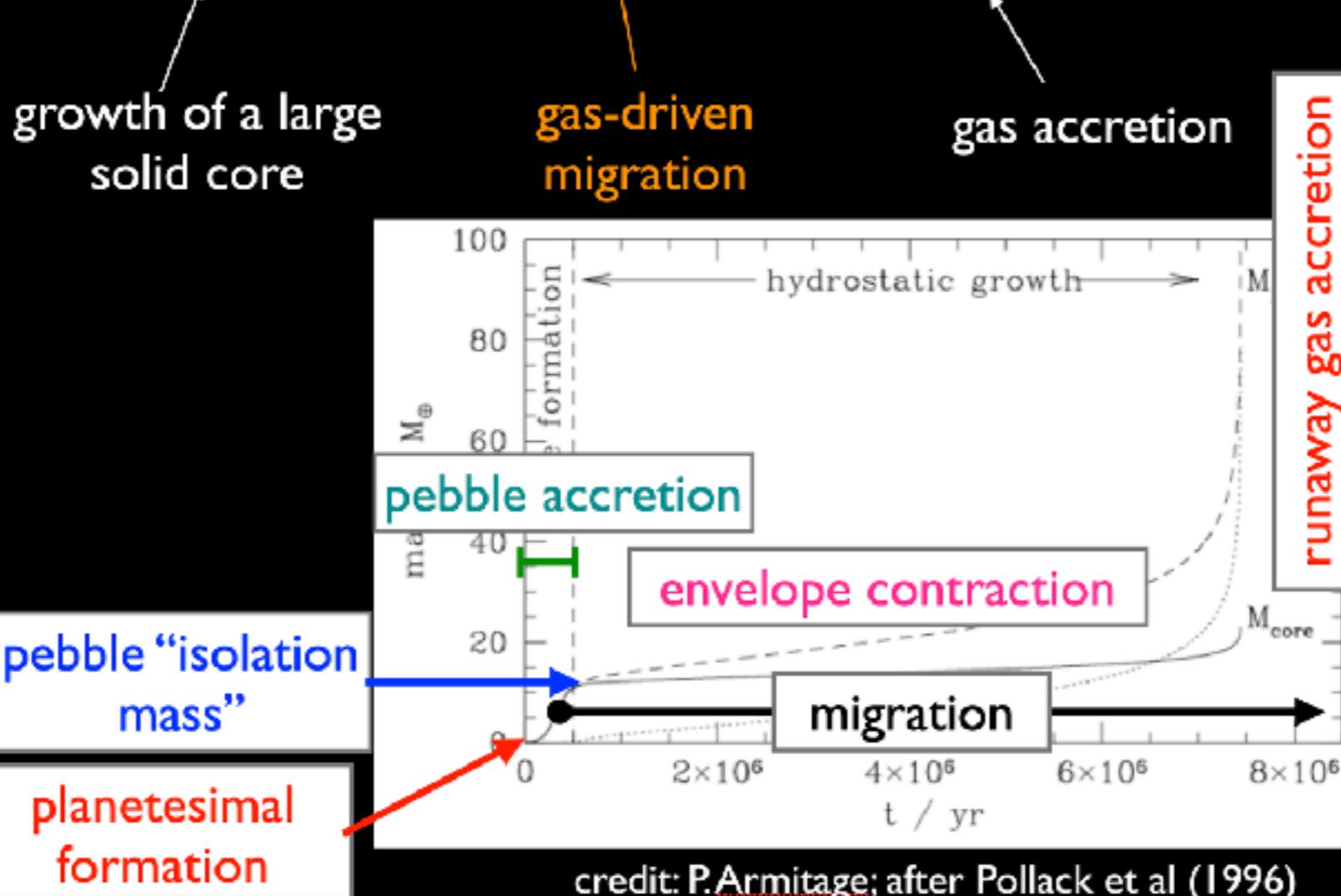


terrestrial planetary embryos:
~Mars-sized

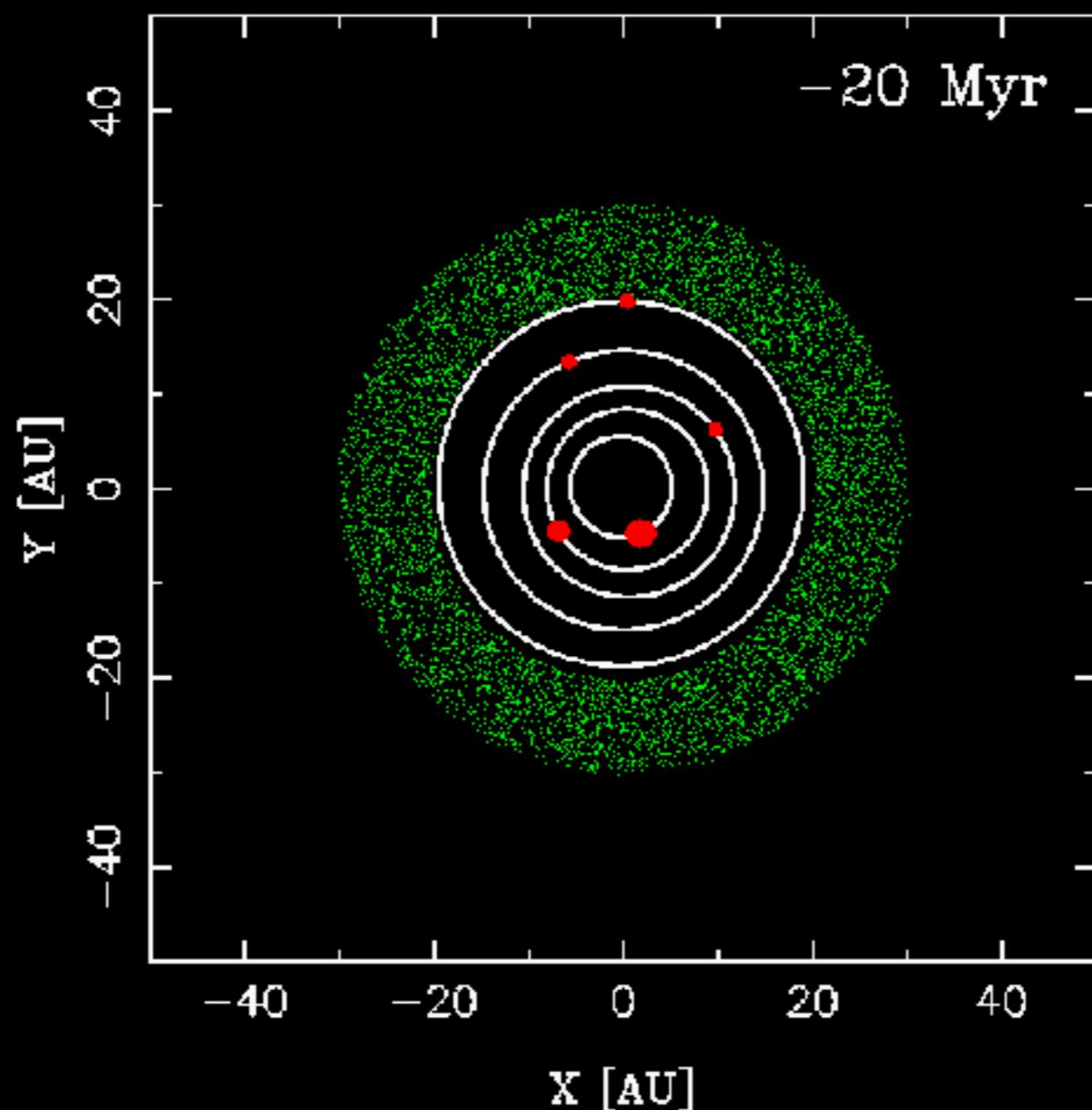
giant planet “cores”:
~Earth-sized or larger

Key event 3: Growth of Jupiter and Saturn

Core migration accretion



Key event 4: the giant planet (dynamical) instability

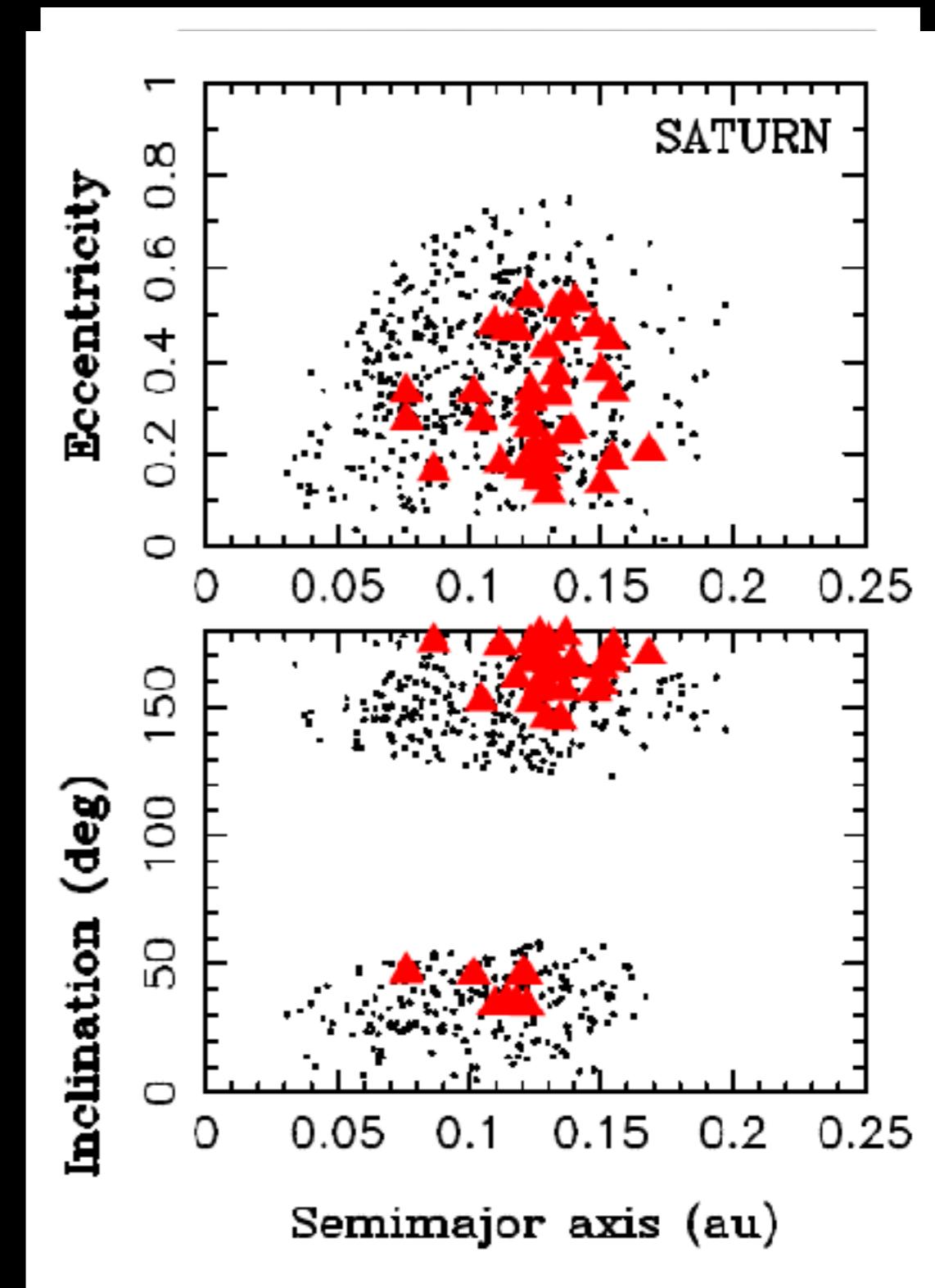


Nesvorný (2011)

also Tsiganis et al (2005), Morbidelli et al (2007), Batygin & Brown (2012), Clement et al (2021)...

The instability explains:

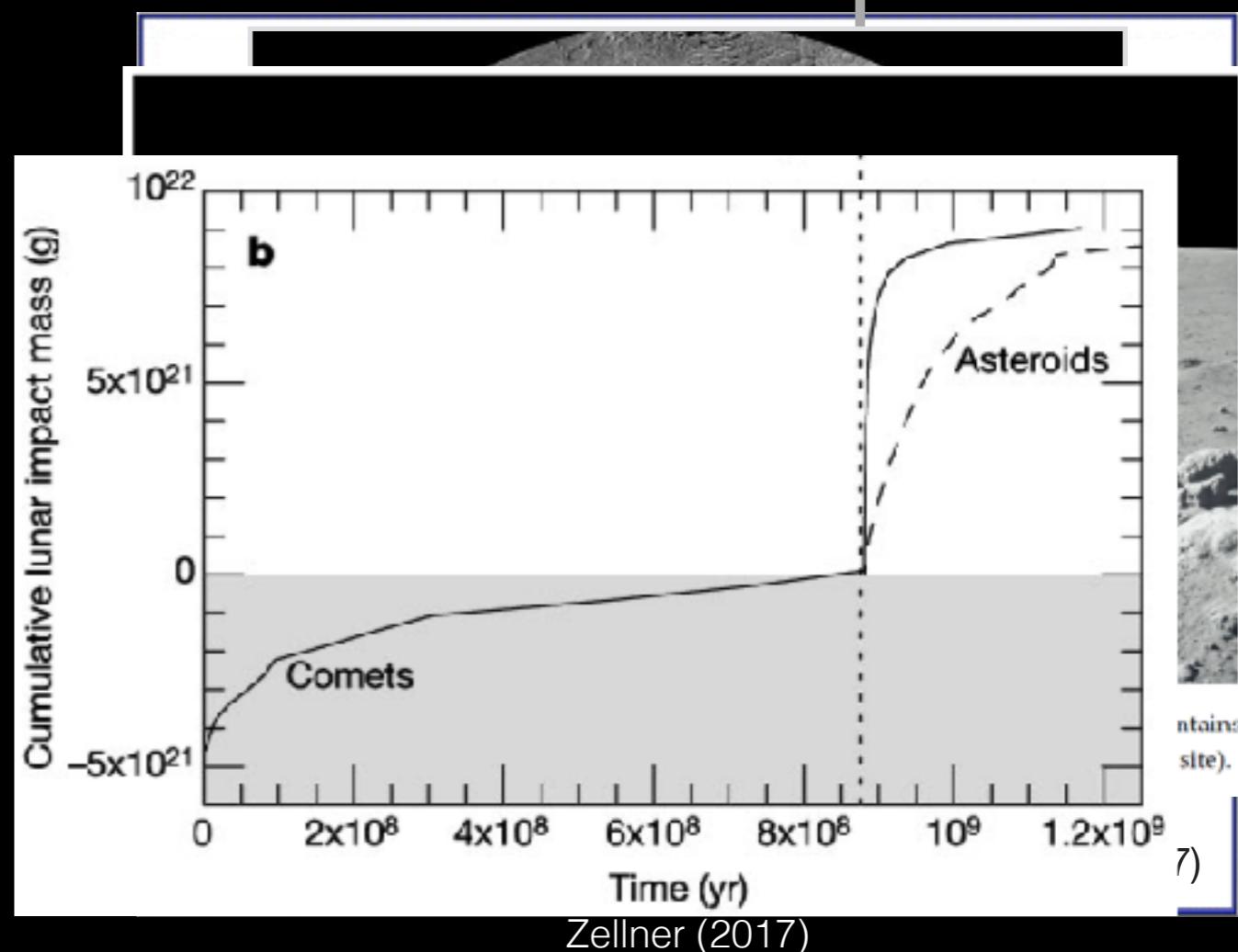
- Giant planets' orbits
- Inclinations of Jupiter's Trojan asteroids
- Capture of irregular satellites of the giant planets
- Orbital structure of the Kuiper belt



When did the instability happen?

- “Terminal lunar cataclysm” likely sampling bias (Chapman et al 2007, Bohnke & Harrison 2016, Zellner 2017, Hartmann 2020)
- New analysis: instability earlier than \sim 100 Myr
 - Binary Jupiter Trojan (Nesvorný et al 2018)
 - Highly siderophile elements++ (Morbidelli et al 2018)
 - Reset ages in meteorite parent bodies (Mojzsis et al 2019)

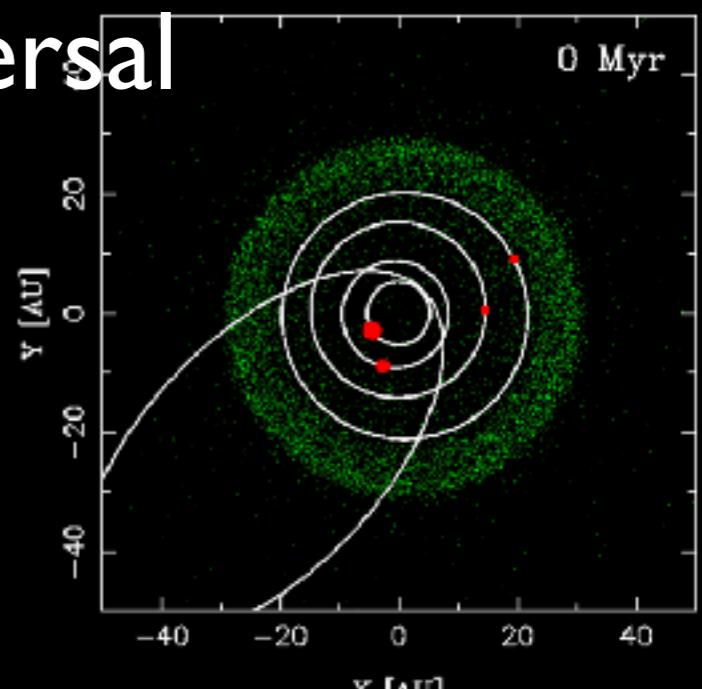
Original “Nice model”
instability timing
(Gomes et al 2005)



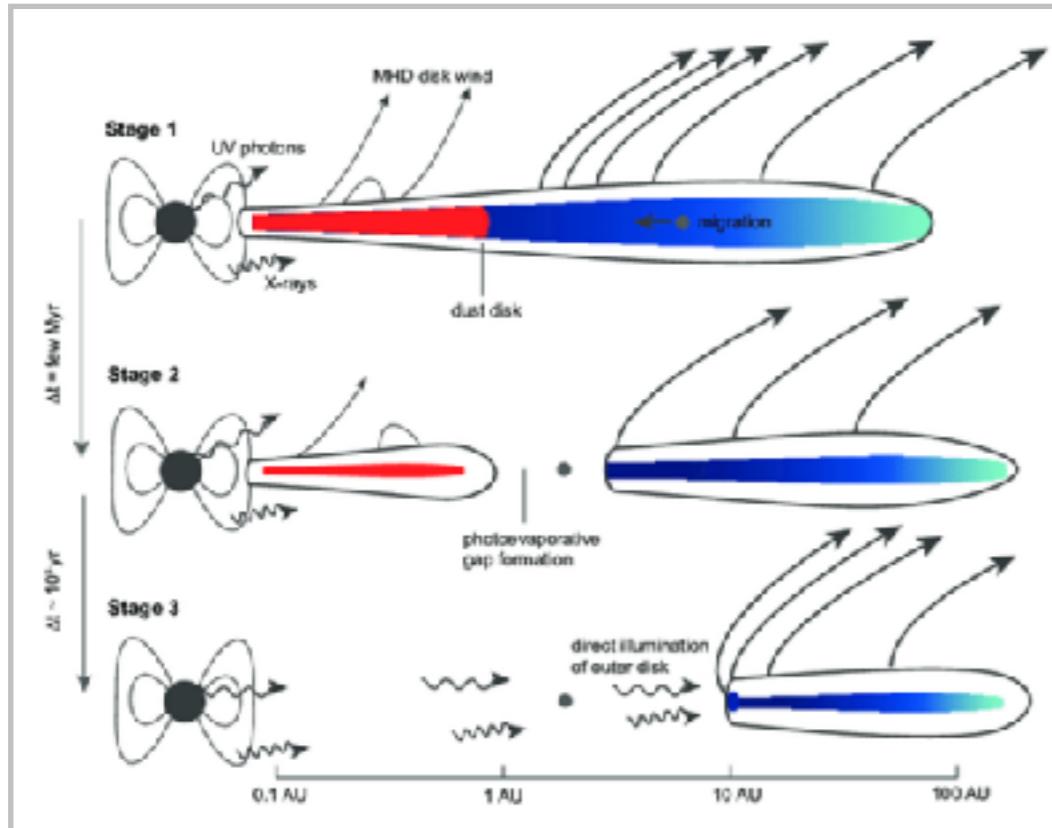
New results based on Pd-Ag isotopes and asteroid reset ages favor instability shortly after gas disk dispersal (Hunt et al 2022; Harper Edwards et al 2024)

Possible instability triggers

1. Gas disk-driven instability: instability happens at gas disk dispersal (Liu et al 2022)
2. Self-triggered instability: instability within few Myr of gas dispersal (Ribeiro de Sousa et al 2020)
3. Planet-planetesimal disk interactions: instability ~30-60 Myr after gas dispersal
(Quarles & Kaib 2019; Ribeiro de Sousa 2020)

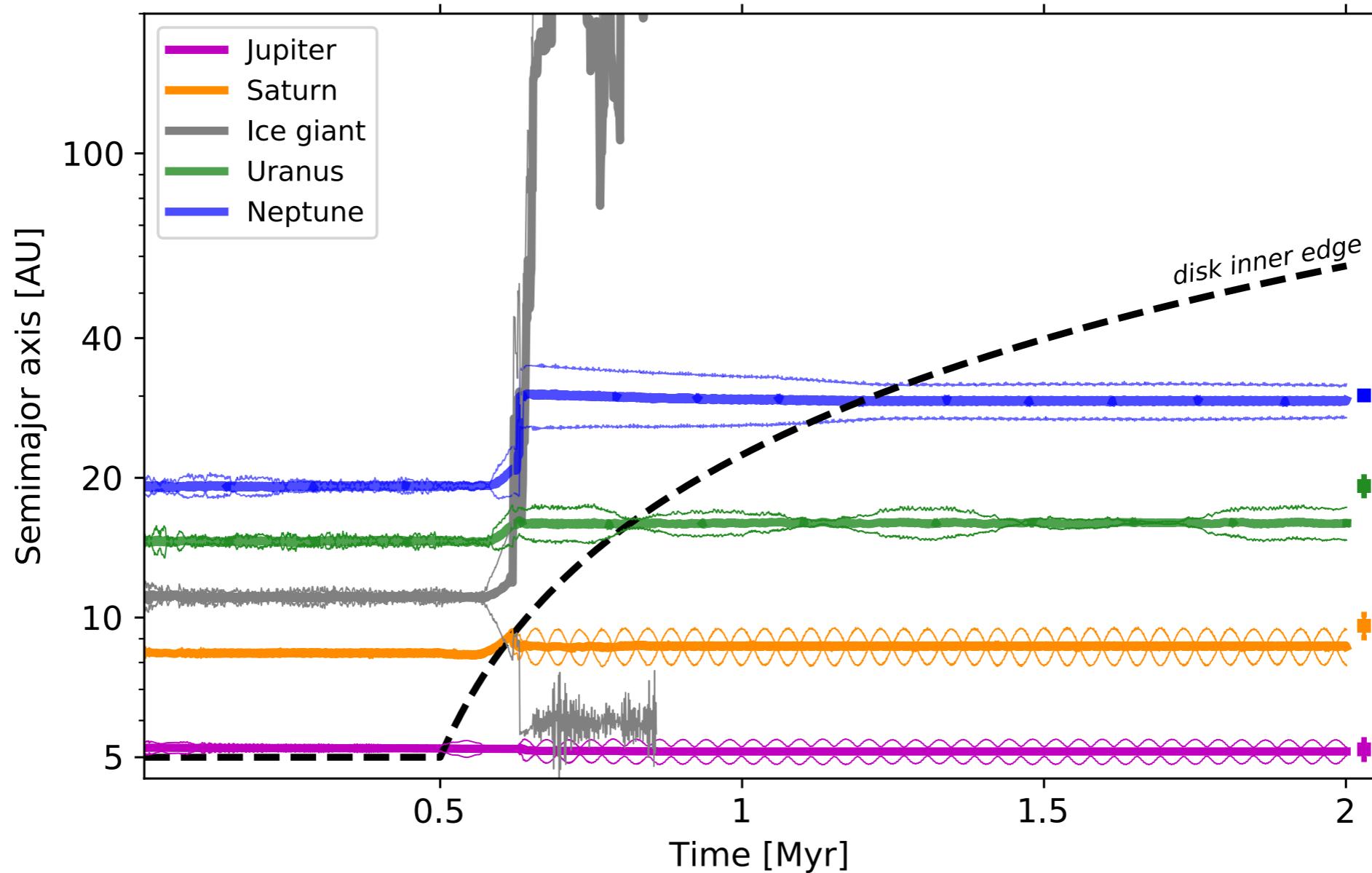


Possible instability trigger: inside-out photo-evaporation of gaseous disk

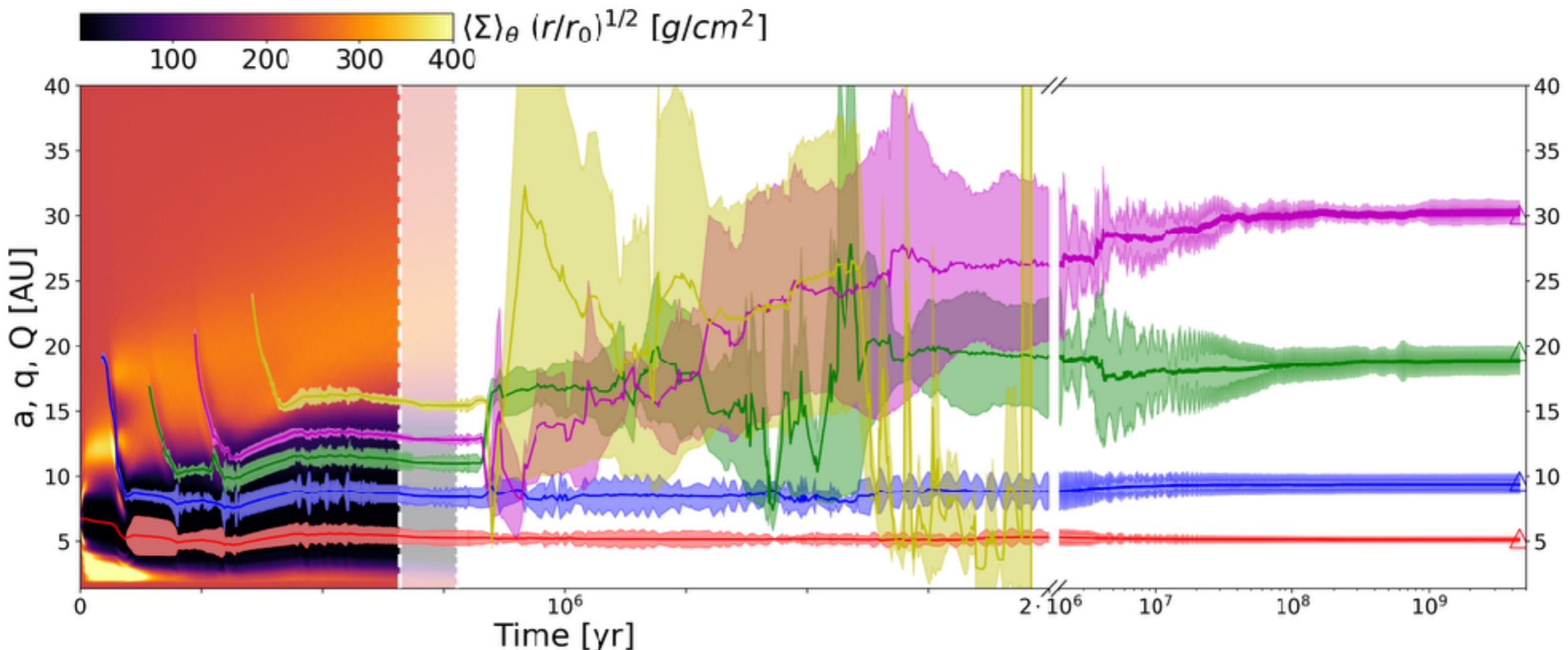


Ercolano & Pascucci (2017)

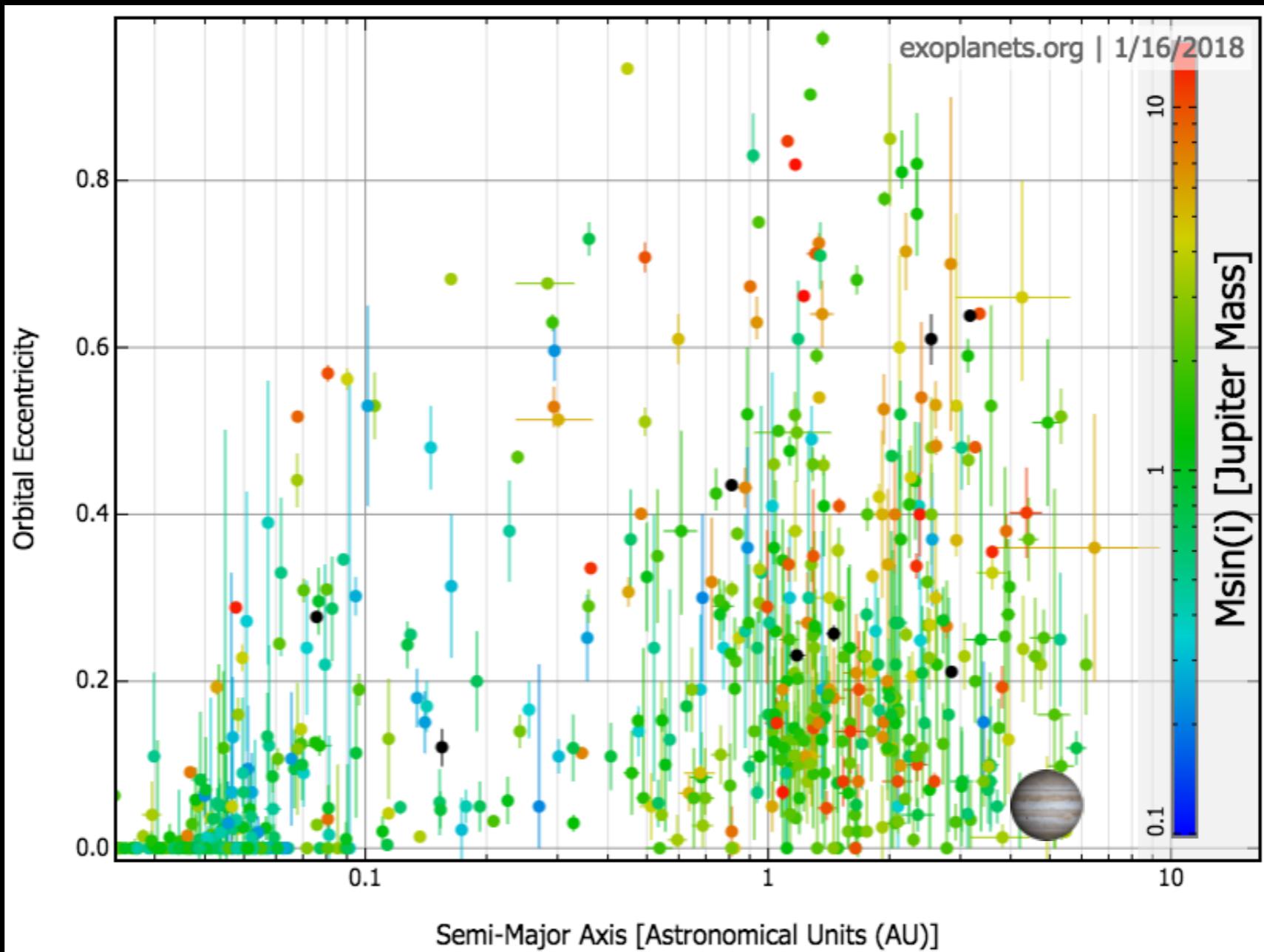
Giant planet instability driven by dispersal of gaseous disk



Another example: self-triggered instability after gas disk dispersal



Remember : the Solar System's dynamical instability was very gentle when compared with exoplanets



Wright et al 2011

Key event 5: the Moon-forming impact

Jacob Kegerreis



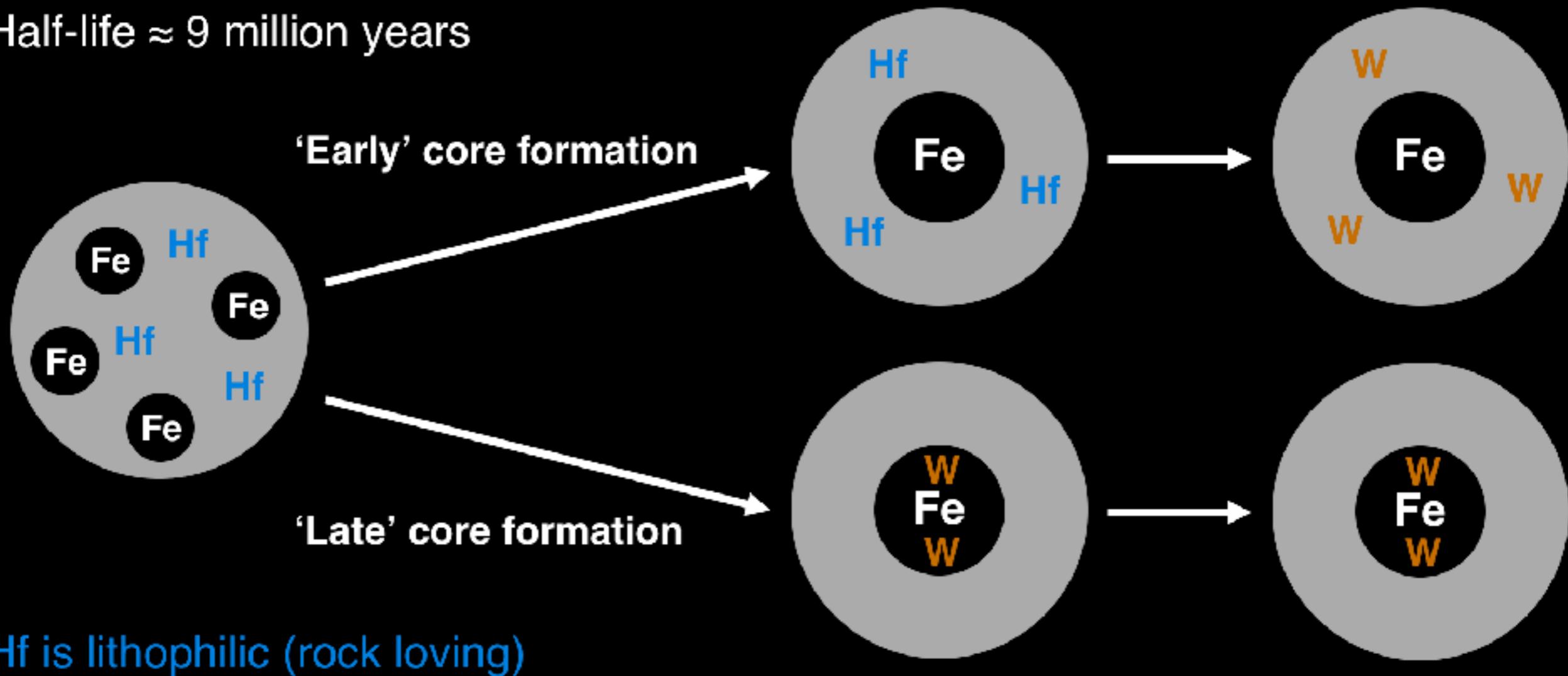
Thought to represent final embryo-embryo impact, at $t \sim 50\text{-}100$ Myr (e.g. Kleine et al 2009)

Credit: Kegerreis et al (2022)

Hafnium–Tungsten Dating



Half-life \approx 9 million years



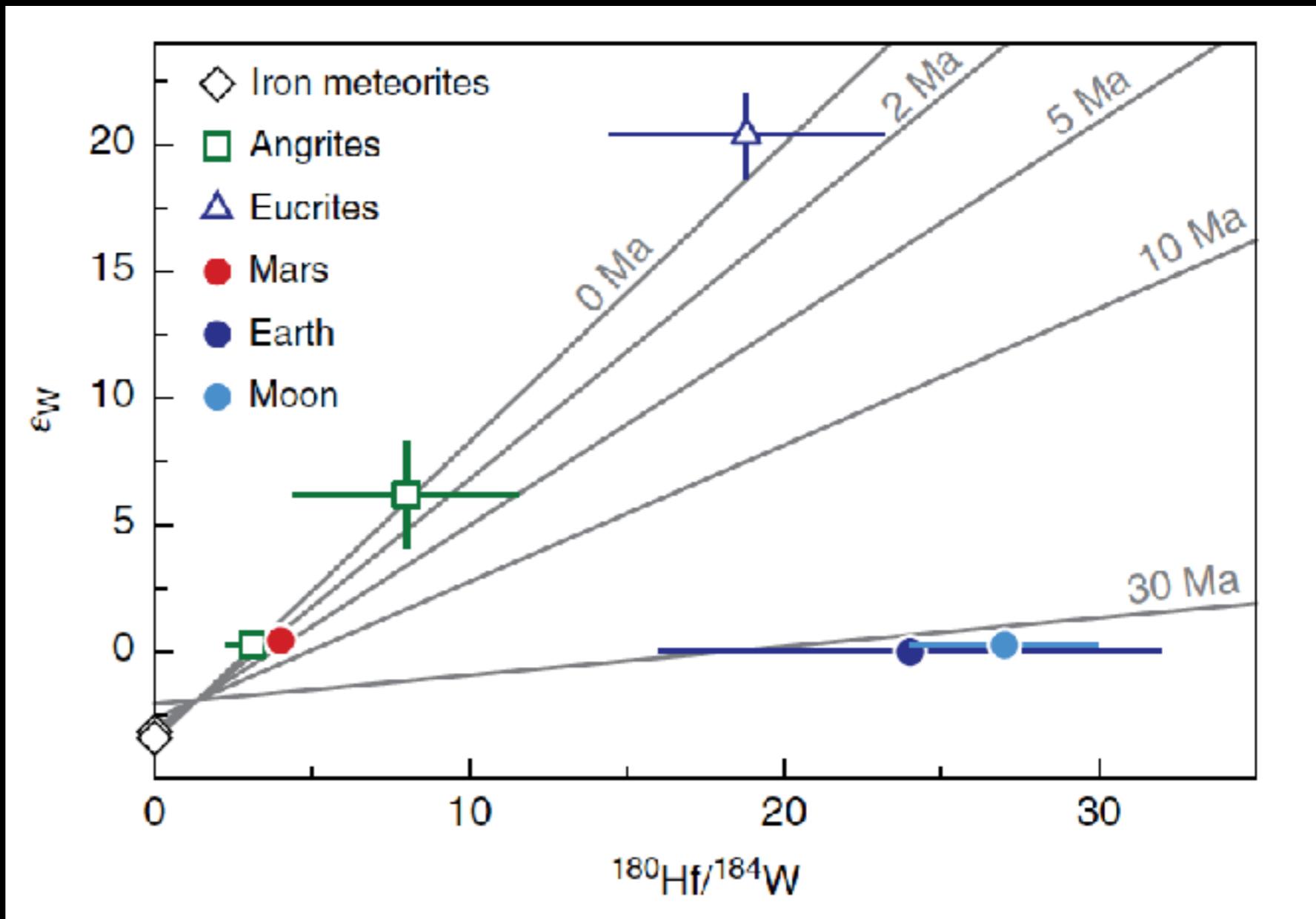
Hf is lithophilic (rock loving)

W is siderophilic (iron loving)

Hf/W isotopes constrain Earth's core formation time (last giant impact)

Half-life of Hf
decay = 8.9 Myr

$$\epsilon_W = \left[\frac{\left(\frac{^{182}\text{W}}{^{184}\text{W}} \right)_{\text{sample}} - 1}{\left(\frac{^{182}\text{W}}{^{184}\text{W}} \right)_{\text{standard}}} \right] \times 10^4$$



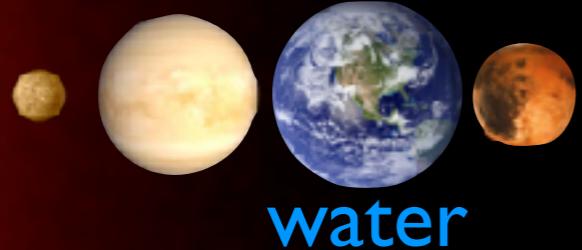
Nimmo & Kleine (2015)

Terrestrial planet formation models



The goal: reproduce the (inner) Solar System

Demeo &
Carry 2014



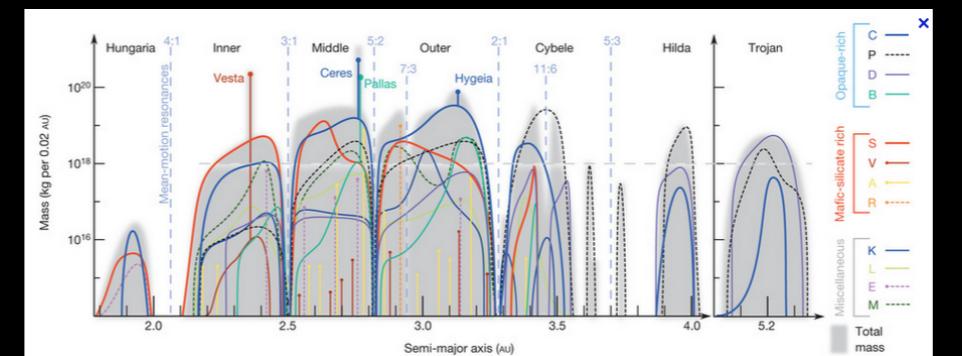
↔

$2 M_{\text{Earth}}$

Number, masses

Orbits

Growth timescales,
compositions,
isotopic ratios



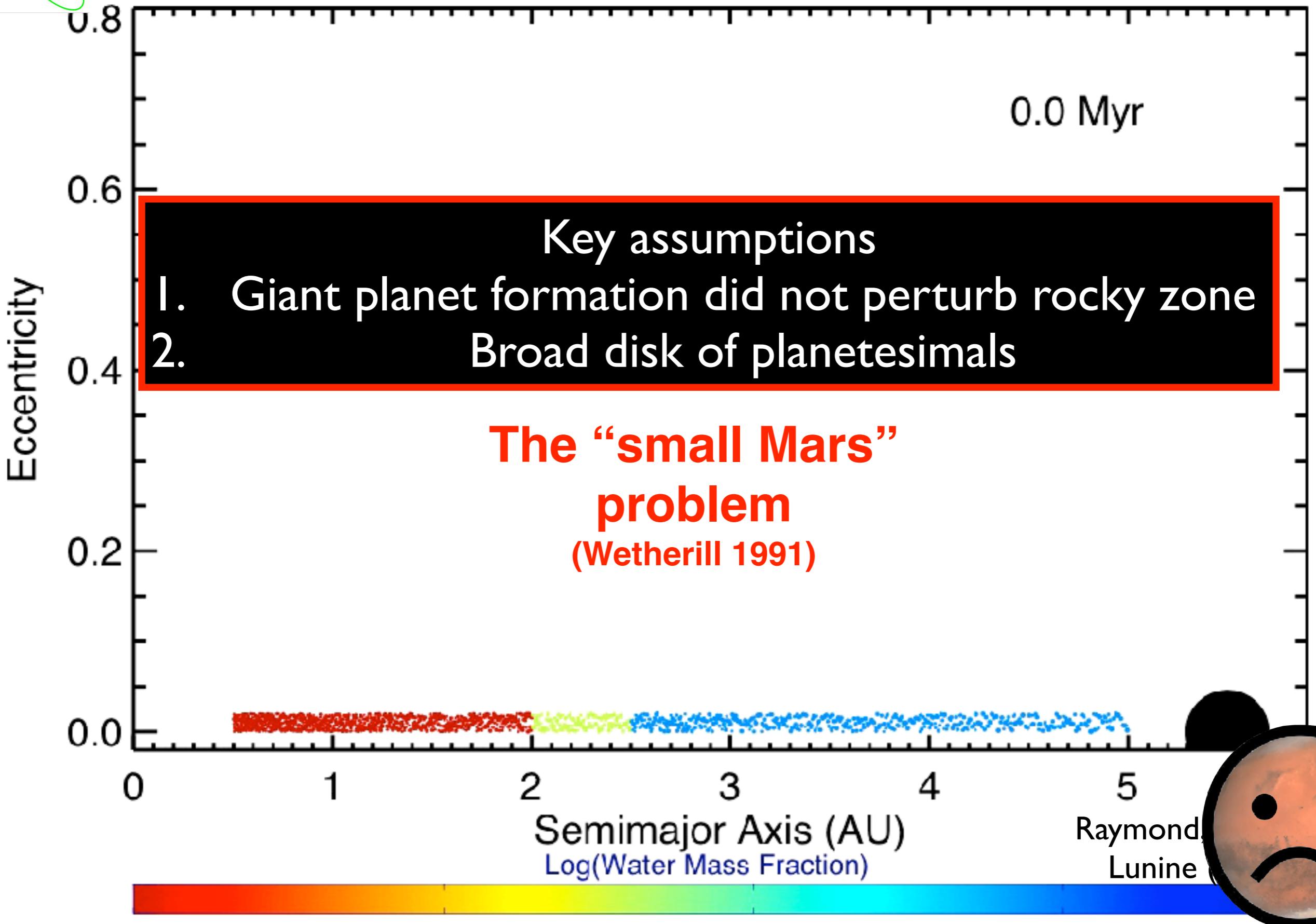
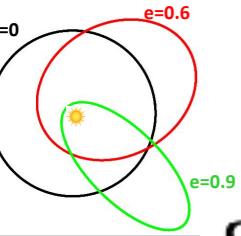
↔

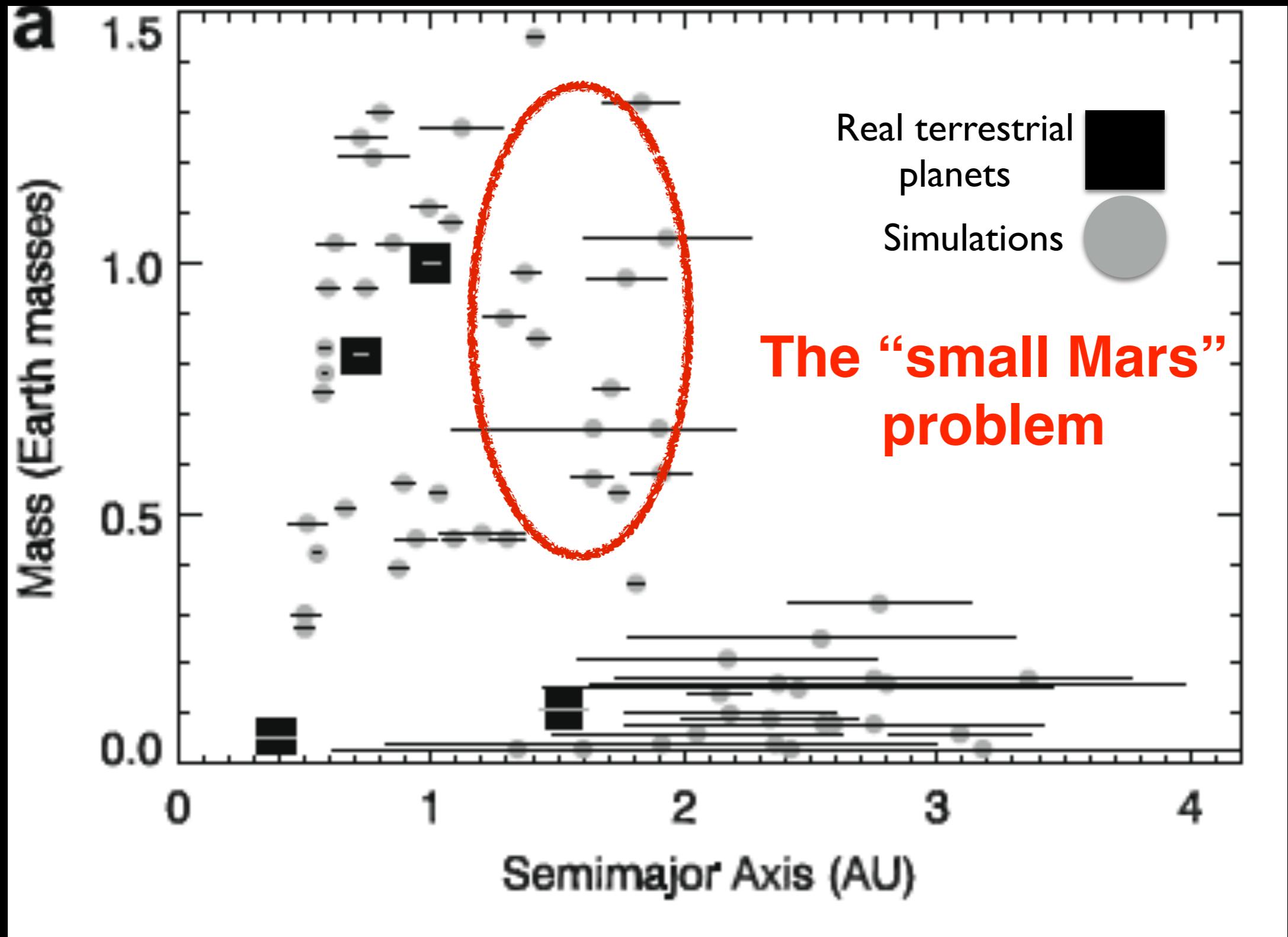
$5 \times 10^{-4} M_{\text{Earth}}$

Total mass
S/C dichotomy
Orbital distribution



The “classical model”





Raymond et al 2009

Wetherill 1991; Chambers 2001; O'Brien et al 2006; Raymond et al 2006, 2009, Morishima et al 2008, 2010; Nagasawa et al 2005, 2007; Thommes et al 2008; Fischer & Ciesla 2014; Izidoro et al 2014, 2015, Kaib & Cowan (2015), Woo et al (2020, 2021)

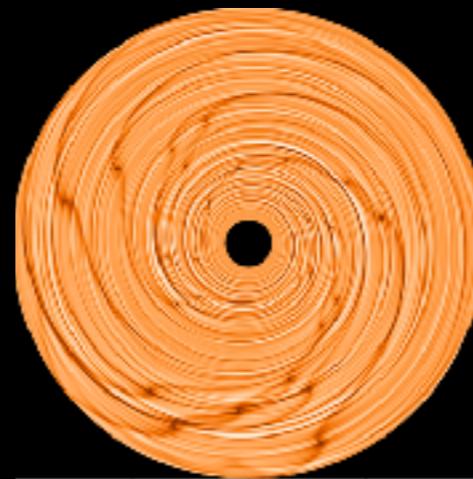
Possible solutions to the small Mars problem



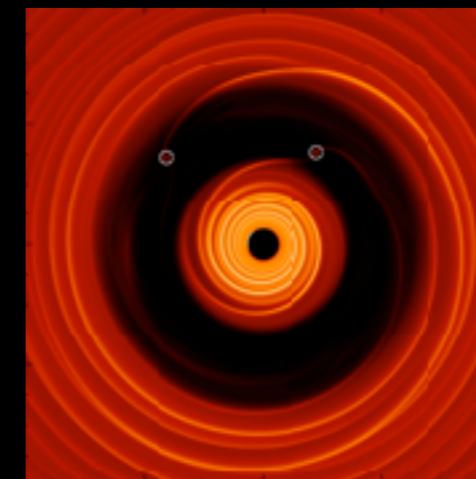
“Empty asteroid belt”



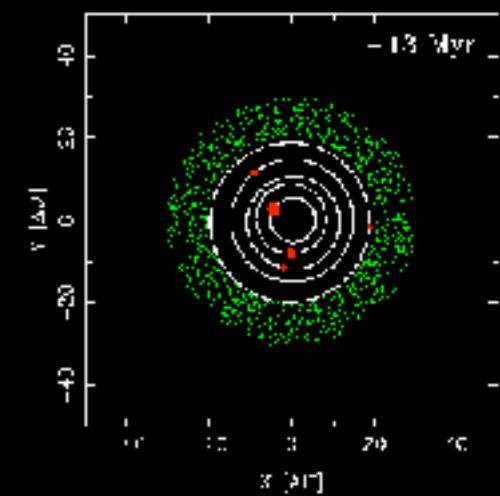
Pebble-driven



Convergent migration



The “Grand Tack”



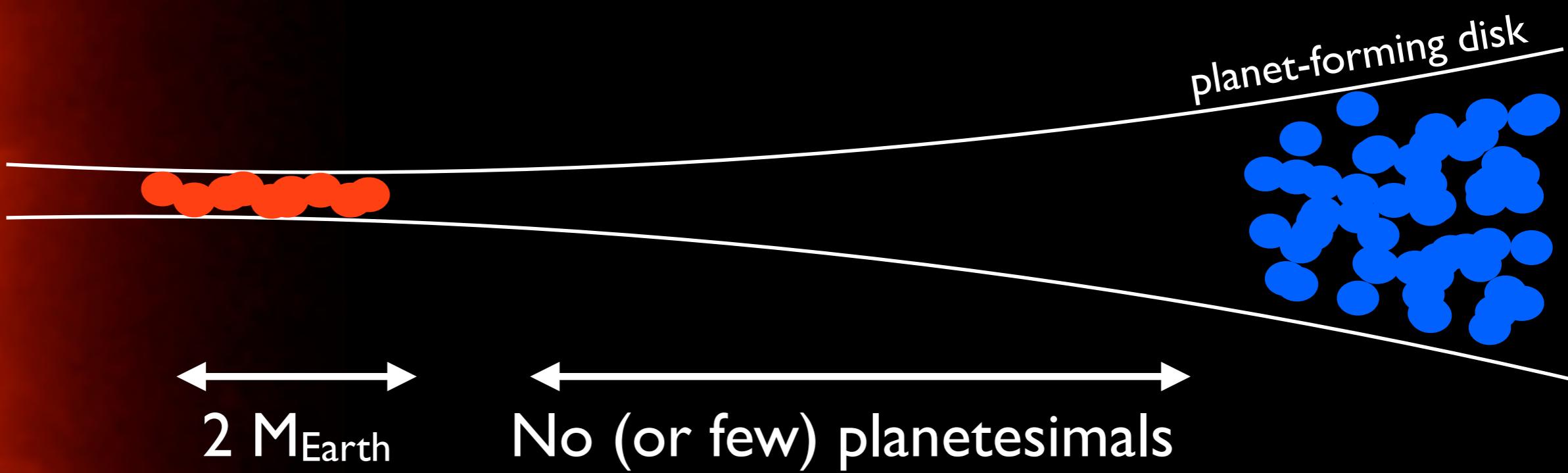
Early instability

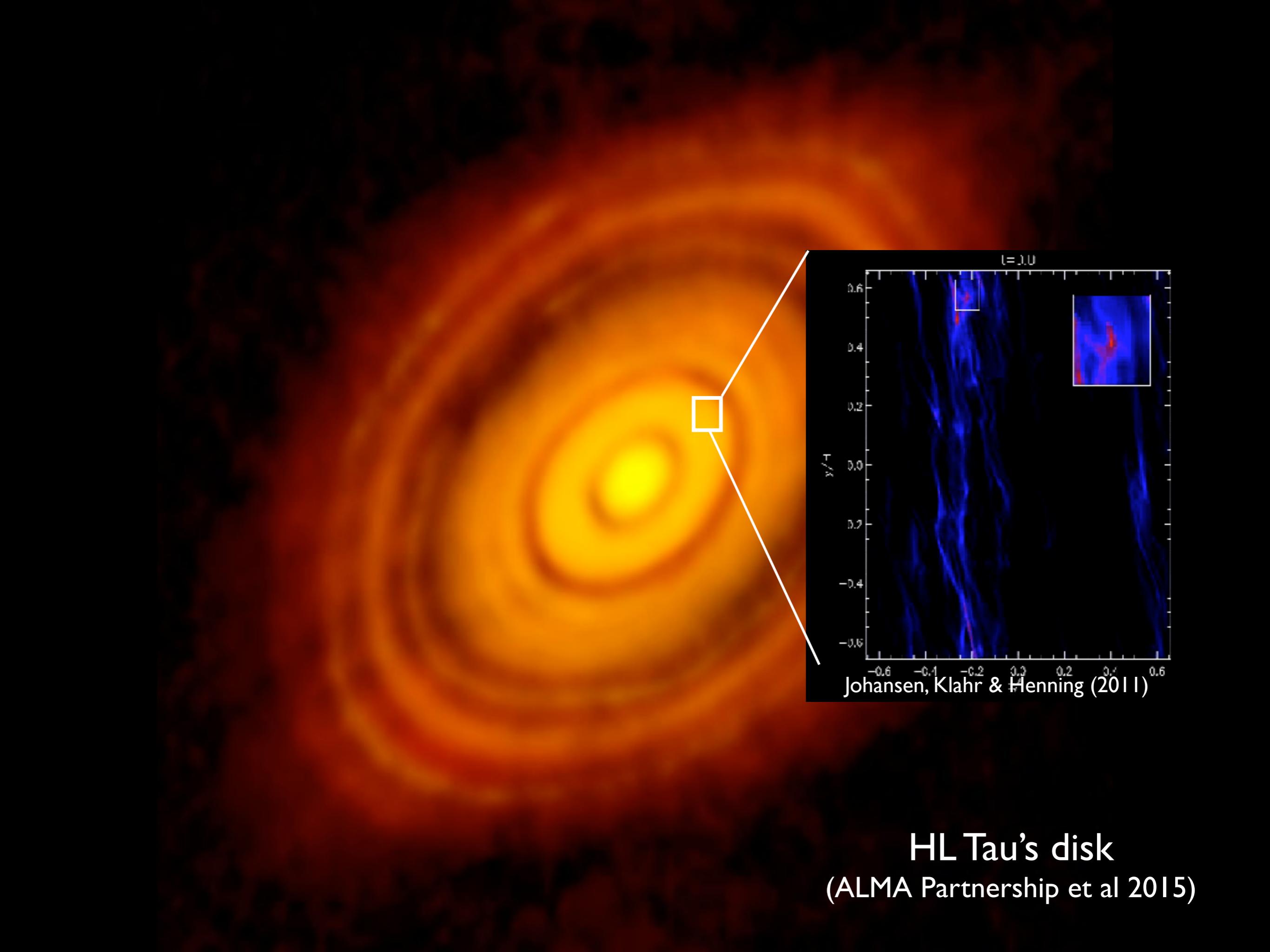


Later dynamical sculpting

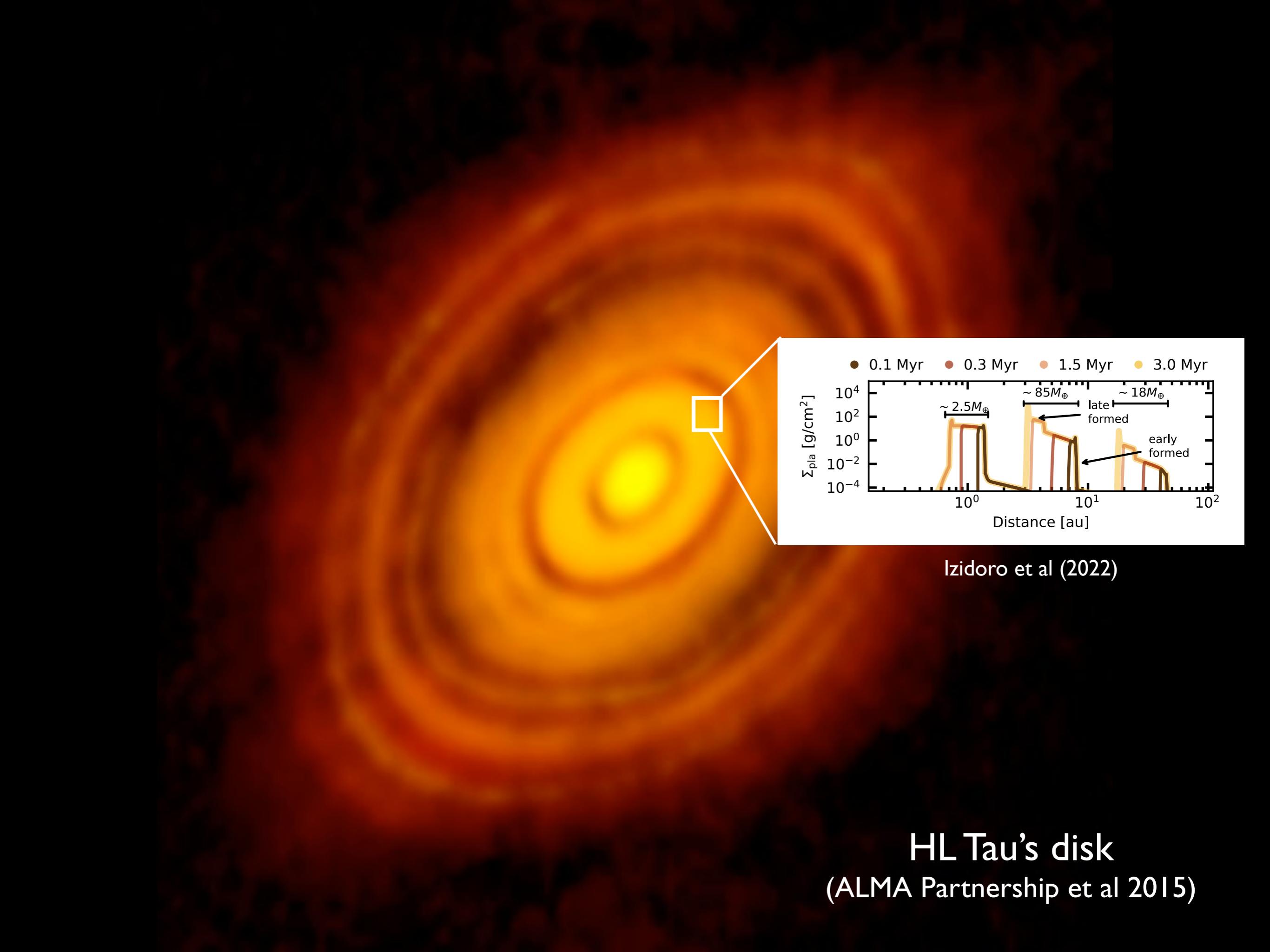
I. Empty asteroid belt

Assumption: few (if any) planetesimals formed
in Mars region/asteroid belt





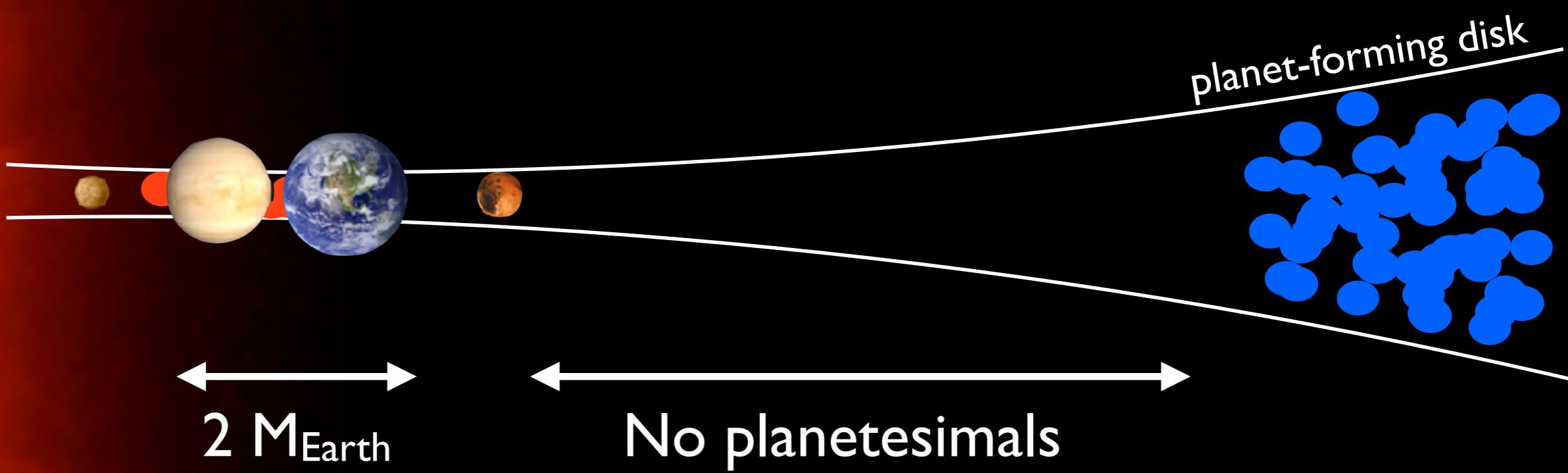
HL Tau's disk
(ALMA Partnership et al 2015)



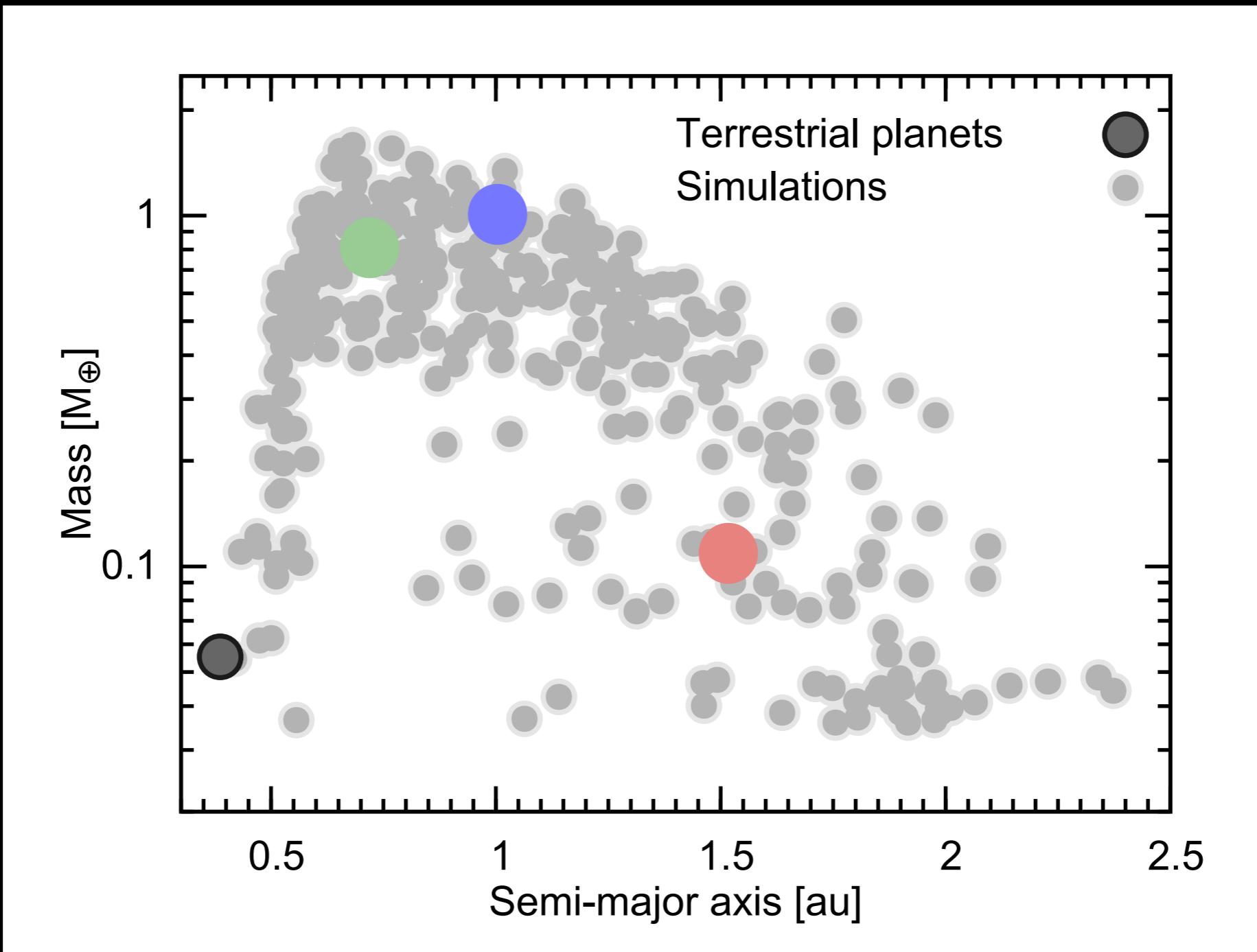
HL Tau's disk
(ALMA Partnership et al 2015)

I. Empty asteroid belt

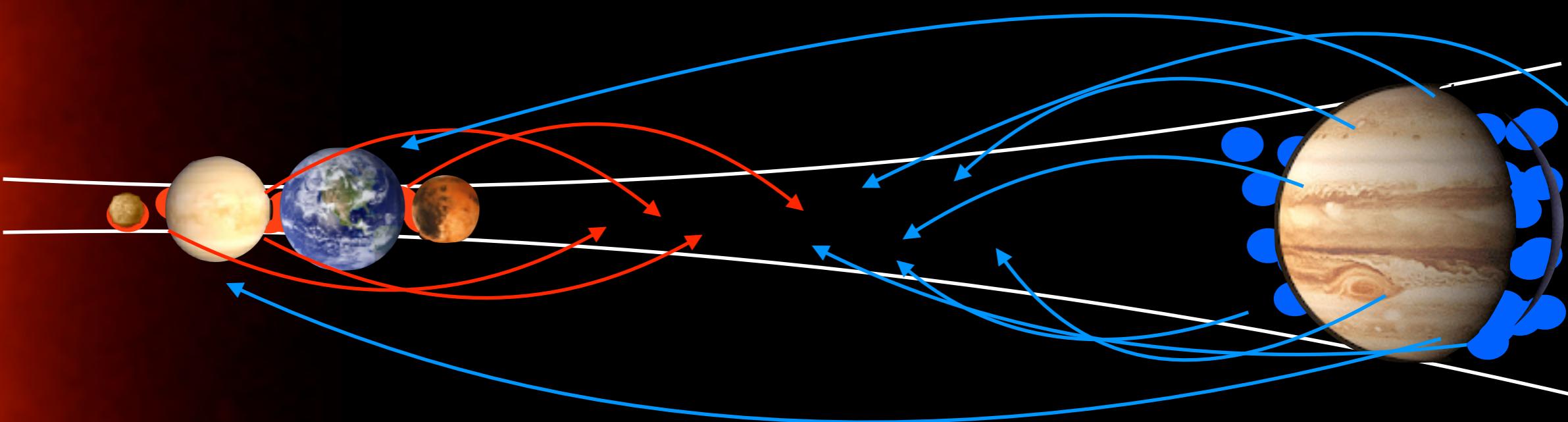
Assumption: few (if any) planetesimals formed in Mars region/asteroid belt



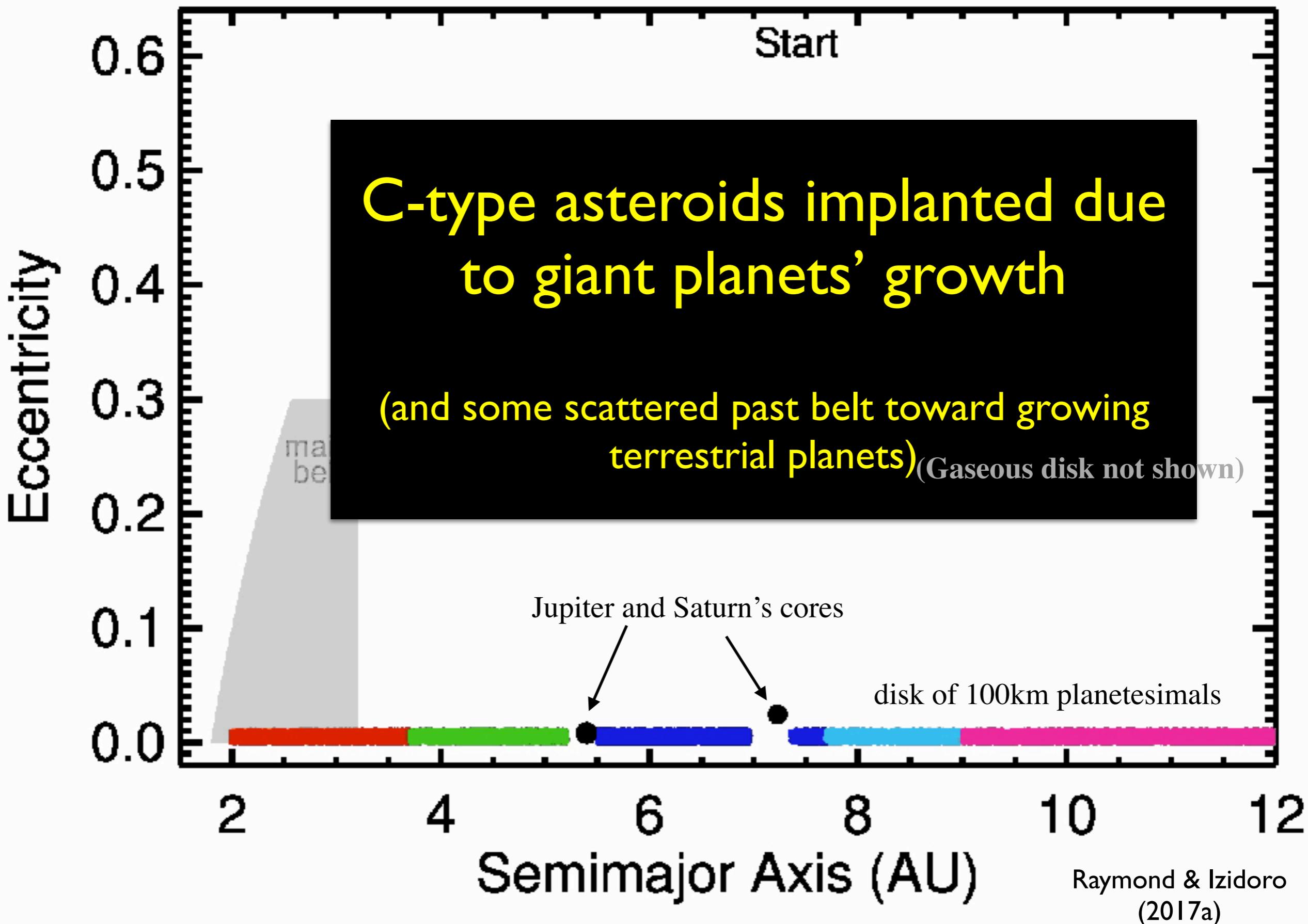
I. Empty asteroid belt



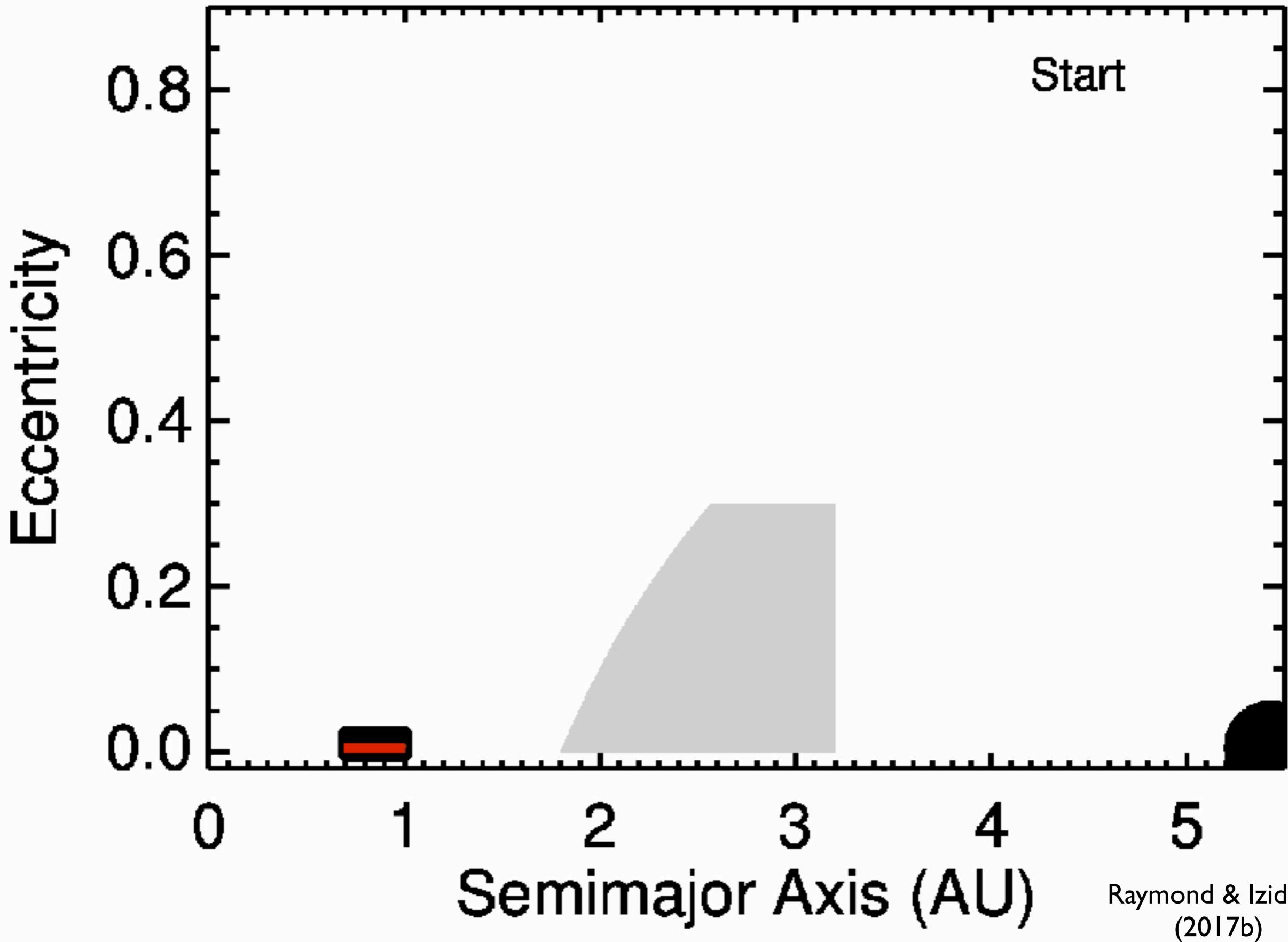
C-types and some of Earth's water from giant planet region



NC asteroids (Vesta, Irons, S-types, ...) scattered out from terrestrial planet region

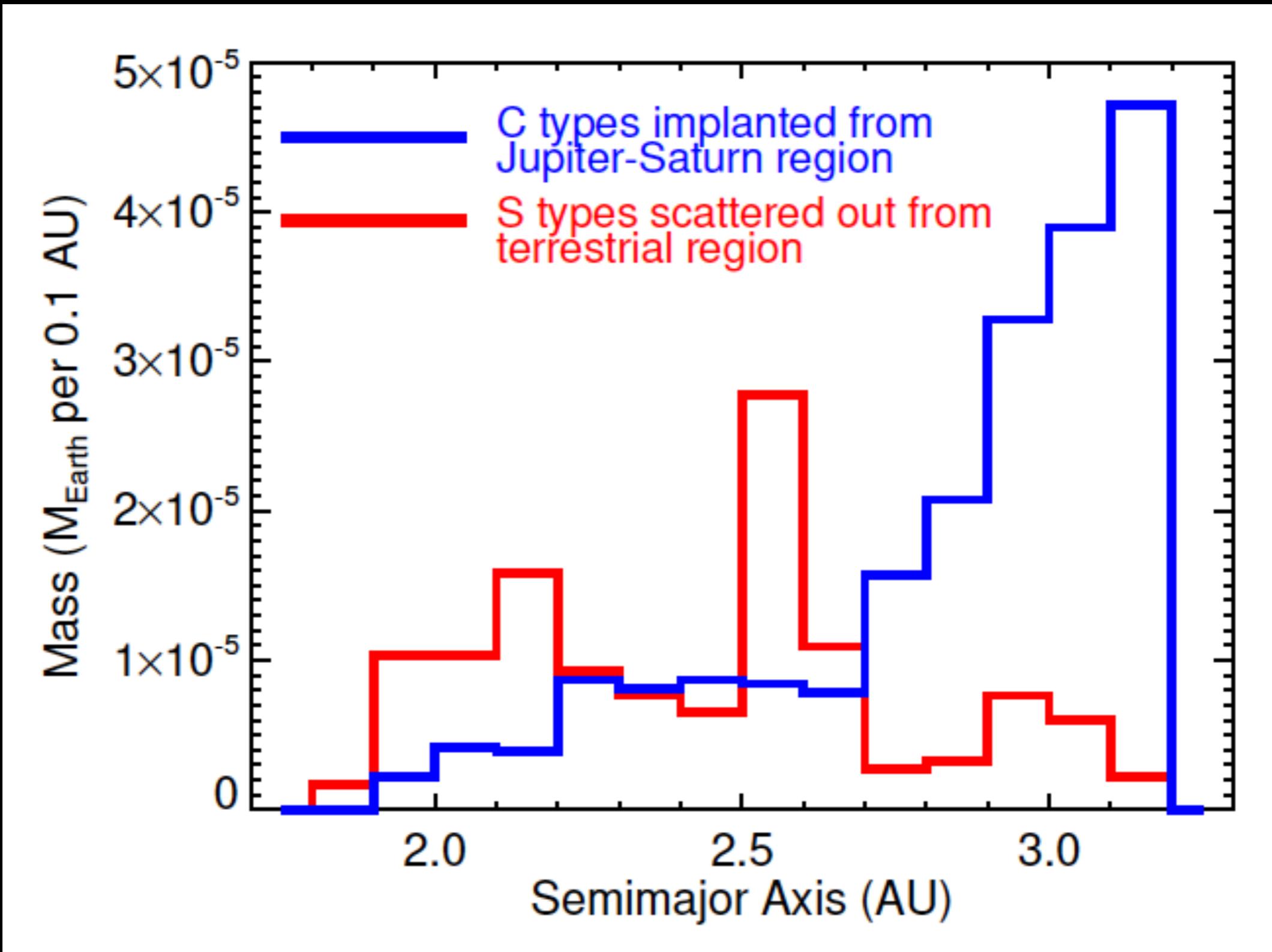


50 simulations of terrestrial planet formation

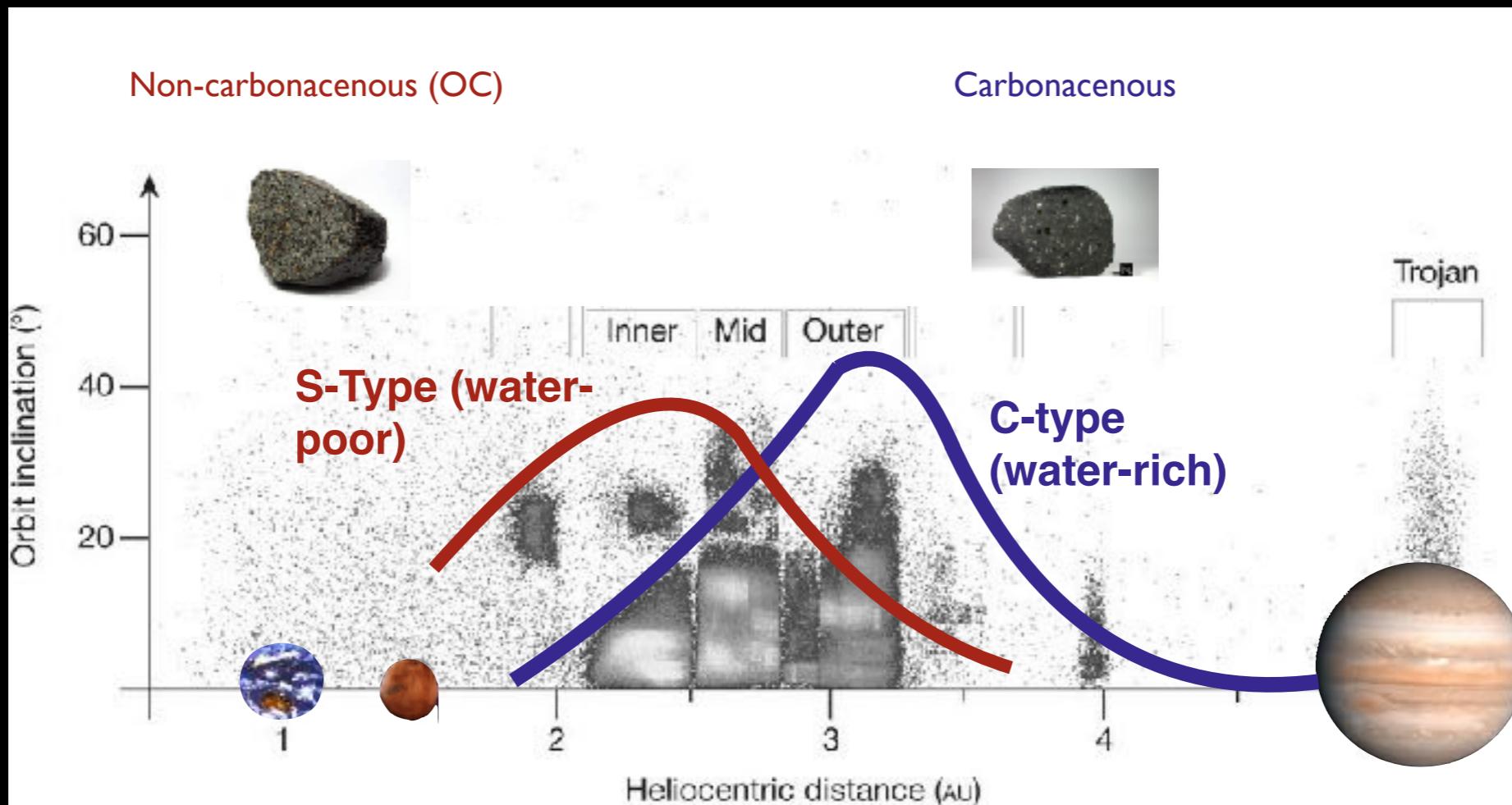


Raymond & Izidoro
(2017b)

100% implanted asteroid belt



NC and CC planetesimals formed far apart but were brought together by the planets' growth



Gradie & Tedesco 1982; Demeo & Carry 2014

Empty asteroid belt

- Inner ring = terrestrial planets
- Middle ring = giant planet cores
- Outer ring = primordial Kuiper belt

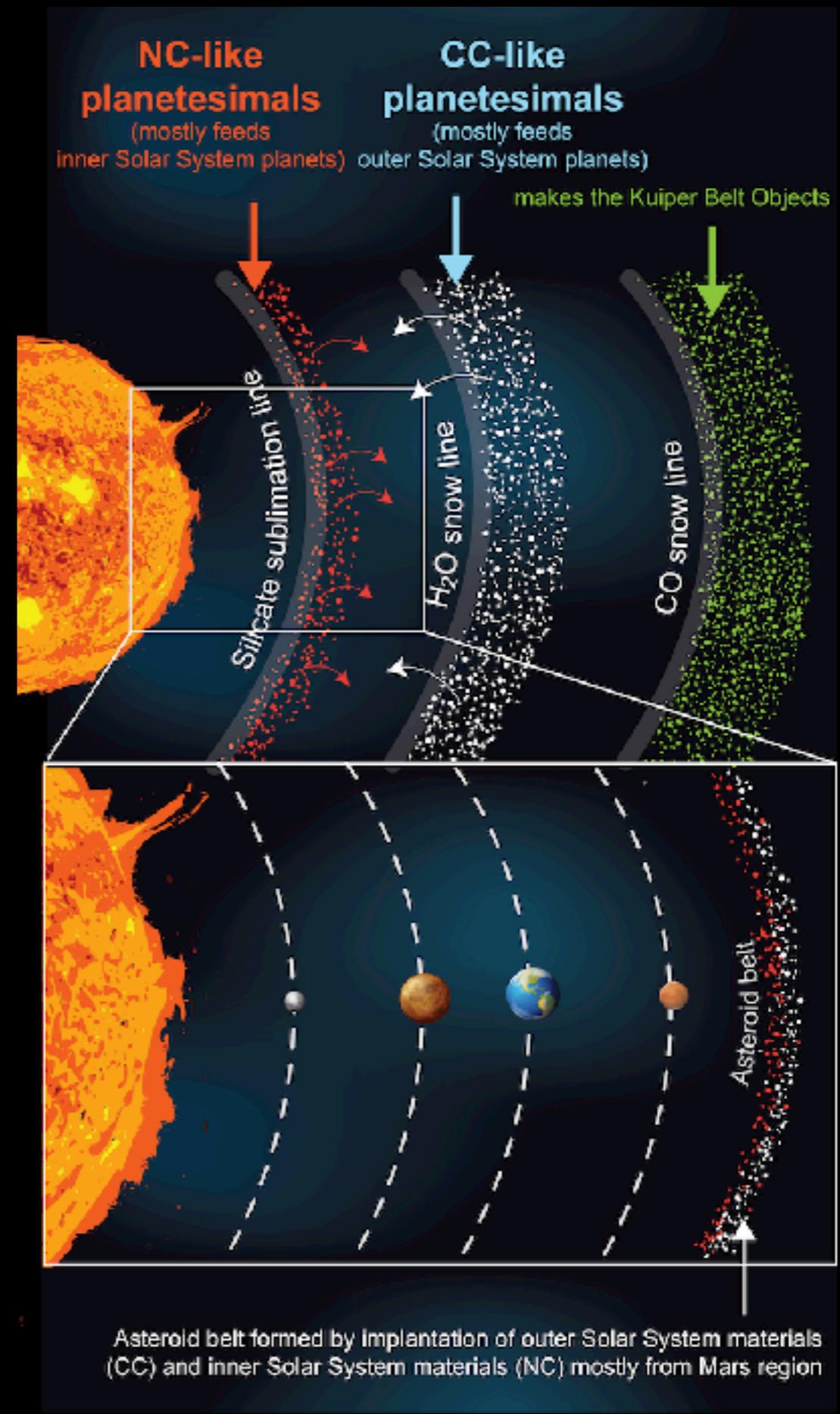
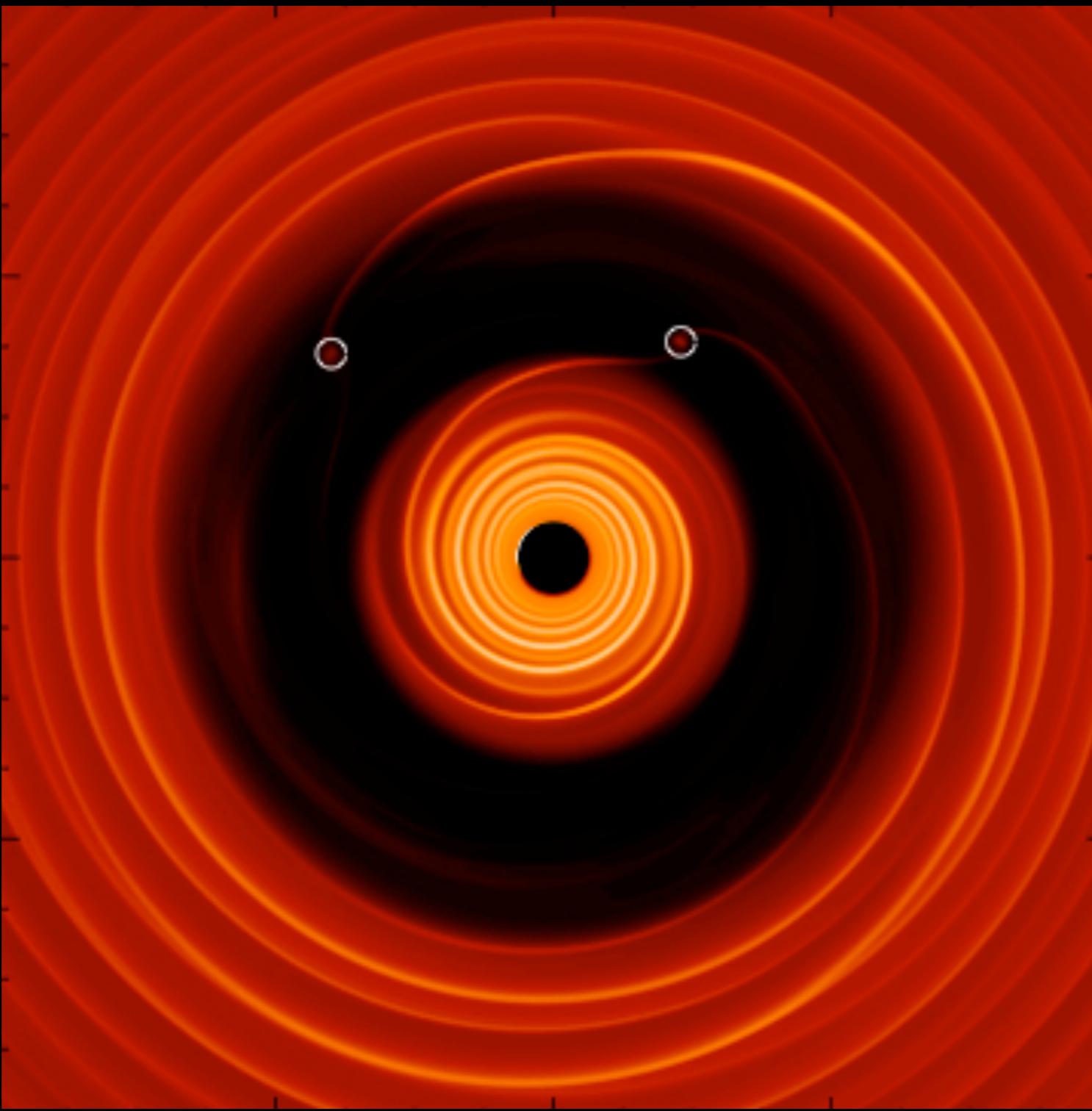


image from Izidoro et al (2022), but representative of lots of models (e.g., Morbidelli et al 2022)

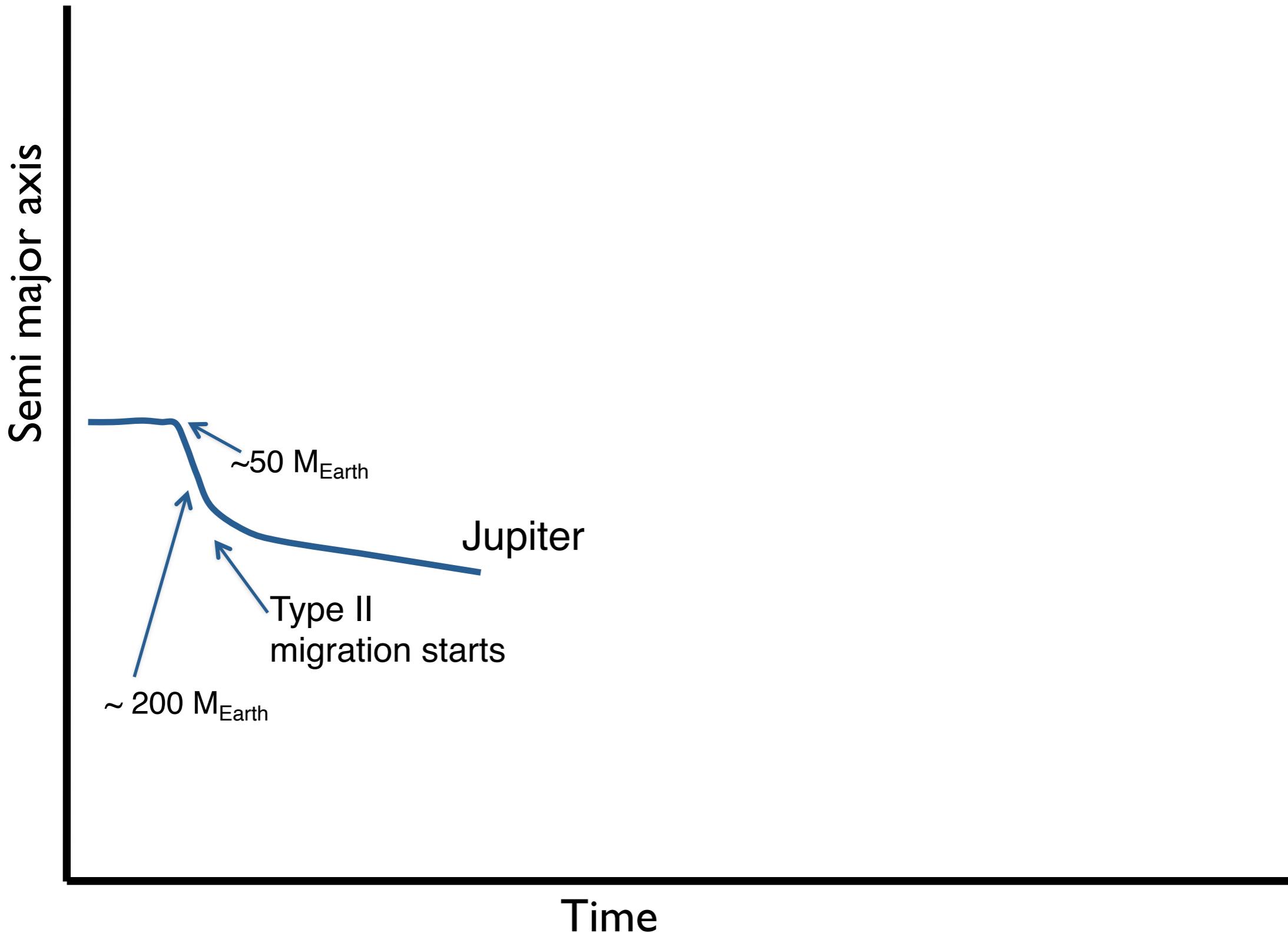
2. The Grand Tack

(Walsh et al 2011)

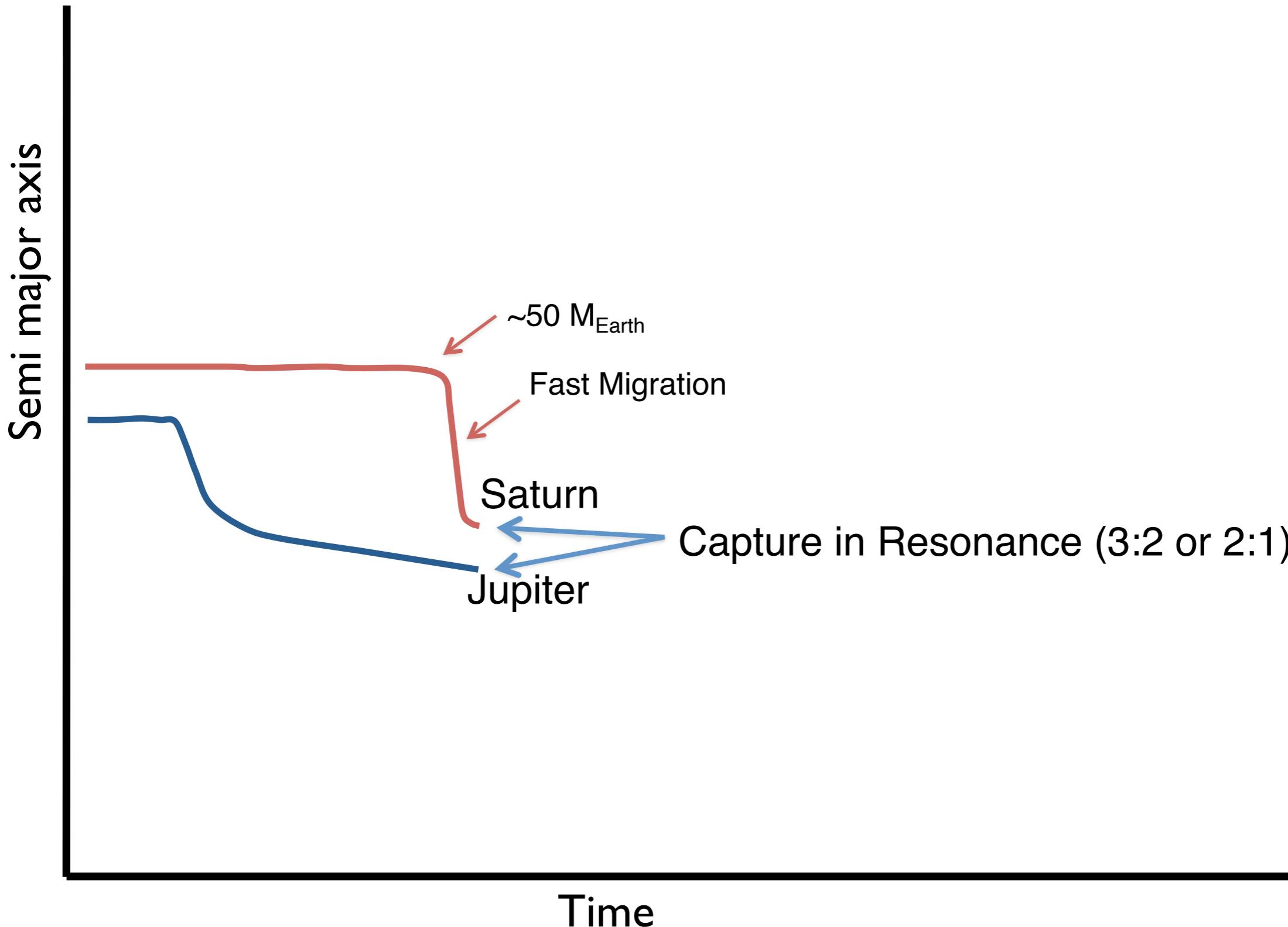


Pierens & Raymond
(2011)

Jupiter in the gaseous disk

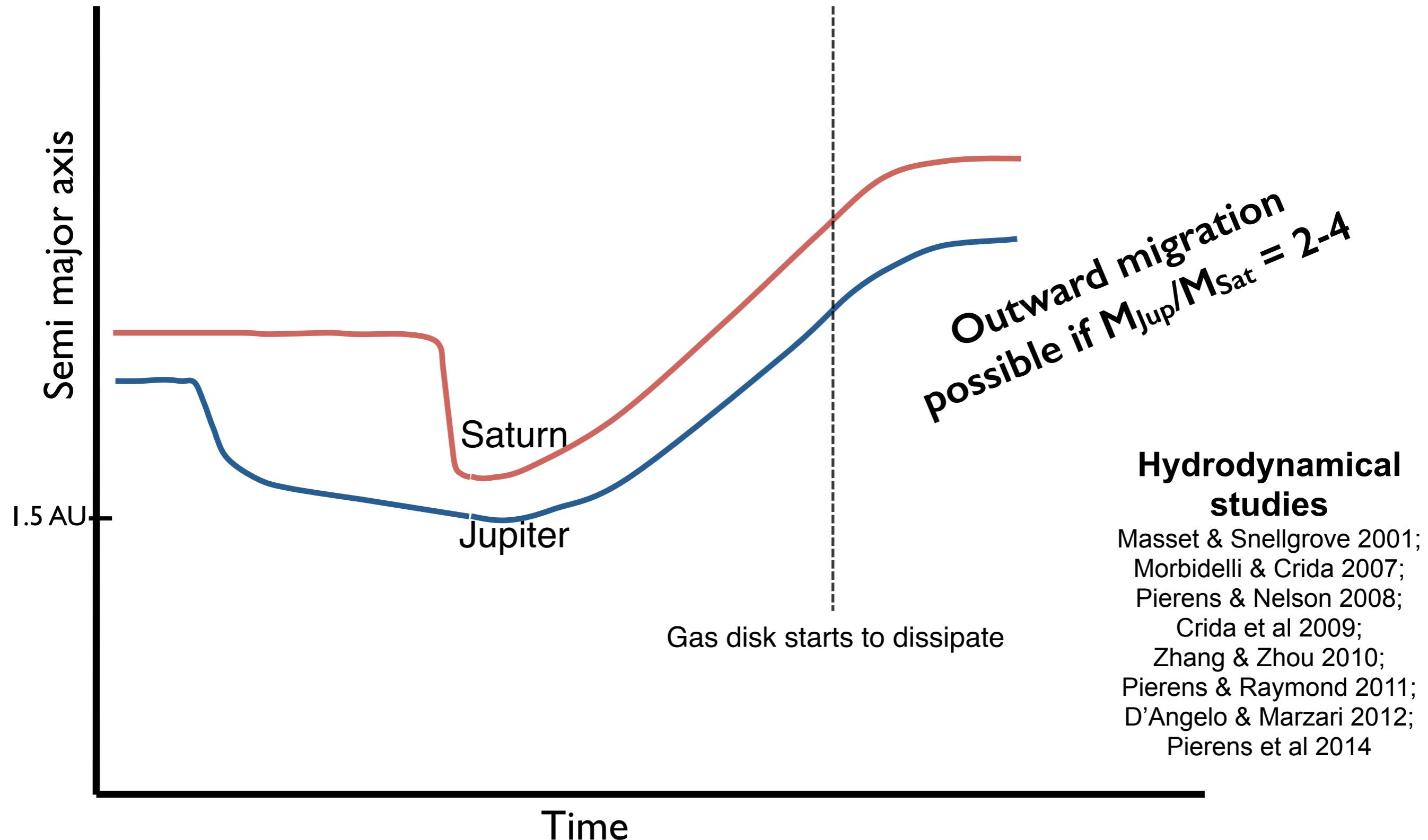


Jupiter and Saturn in the gaseous disk



The Grand Tack model

(Walsh et al 2011)



The Grand Tack model

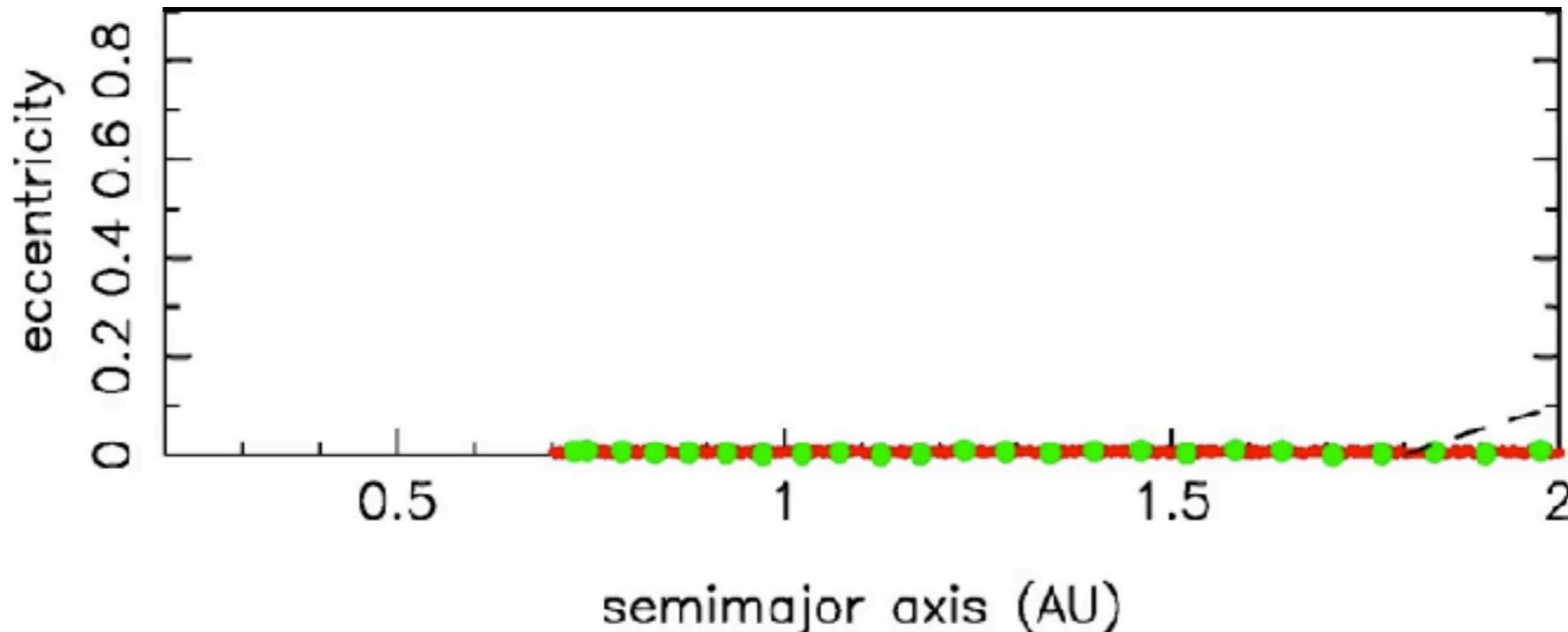
T= 0.000 My



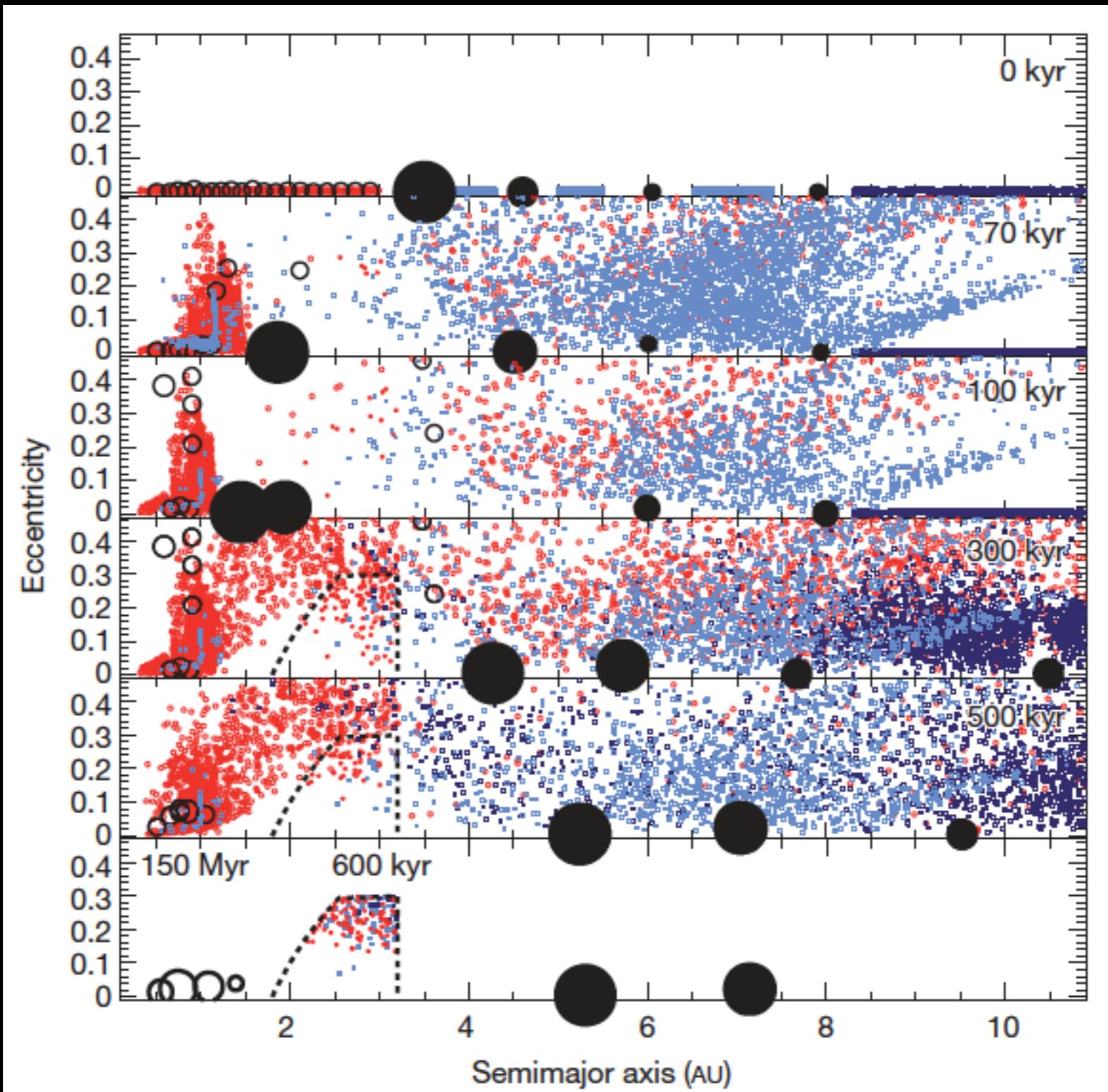
Planetary embryos



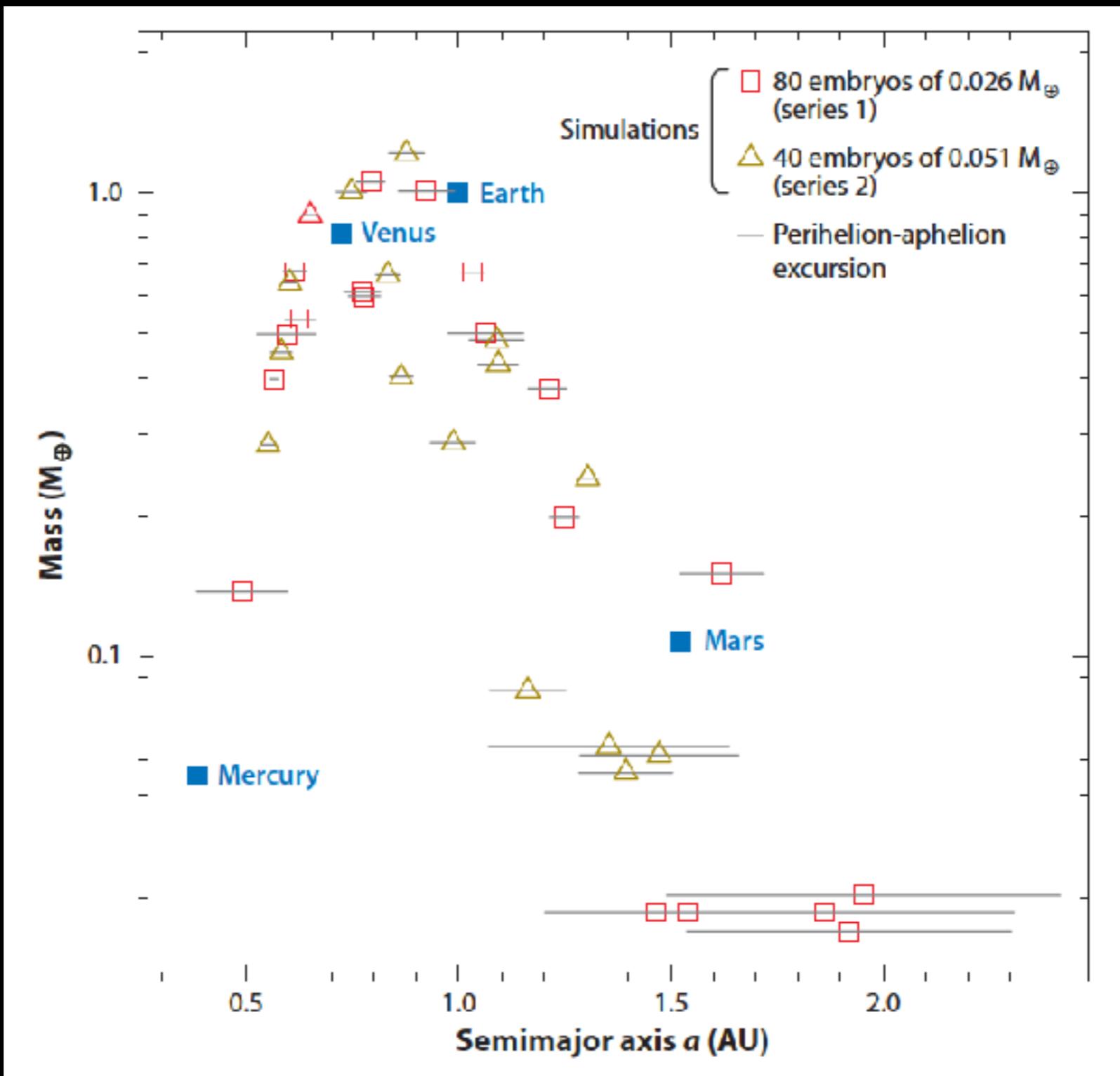
Planetesimals



The Grand Tack

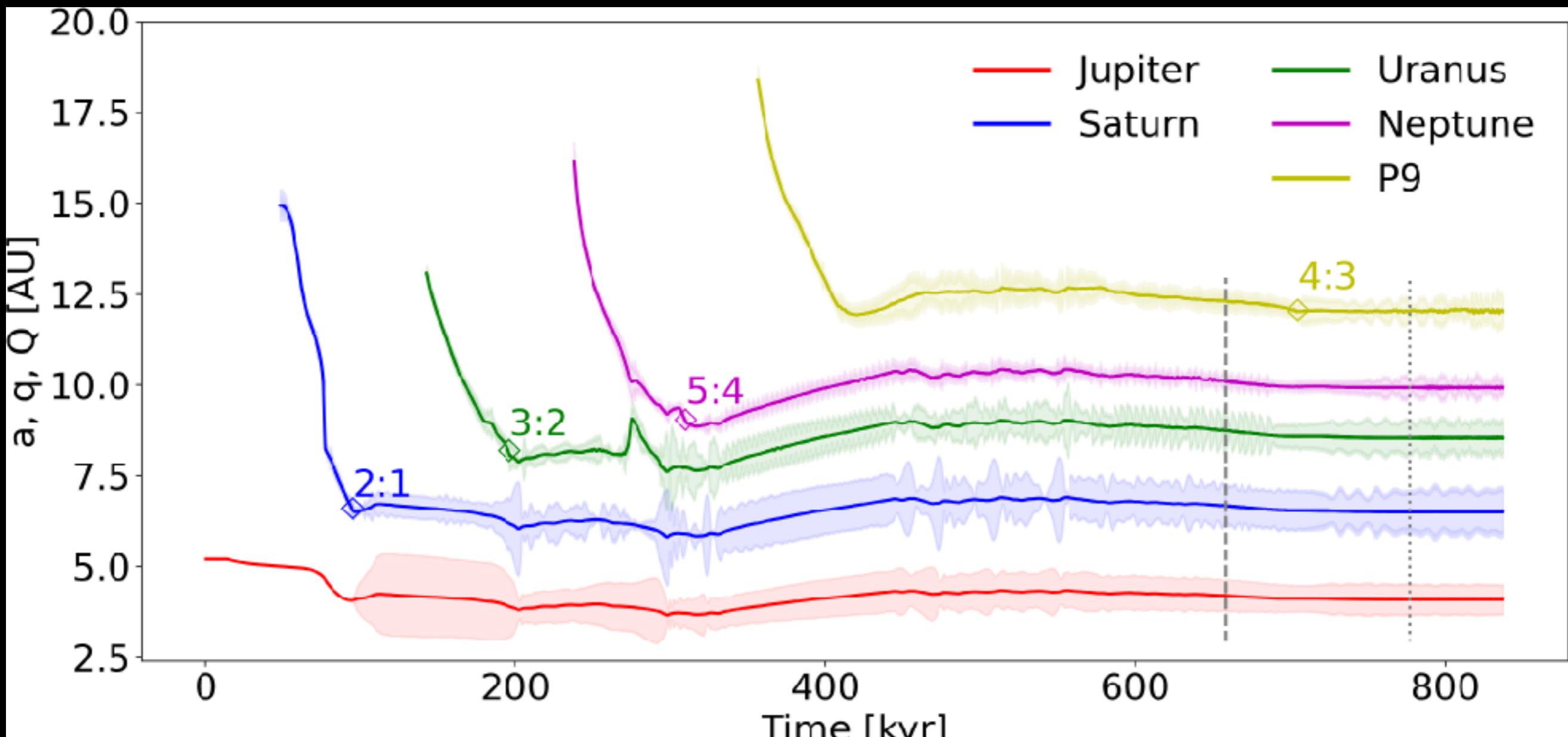


Grand Tack terrestrial planets



Morbidelli et al (2012)

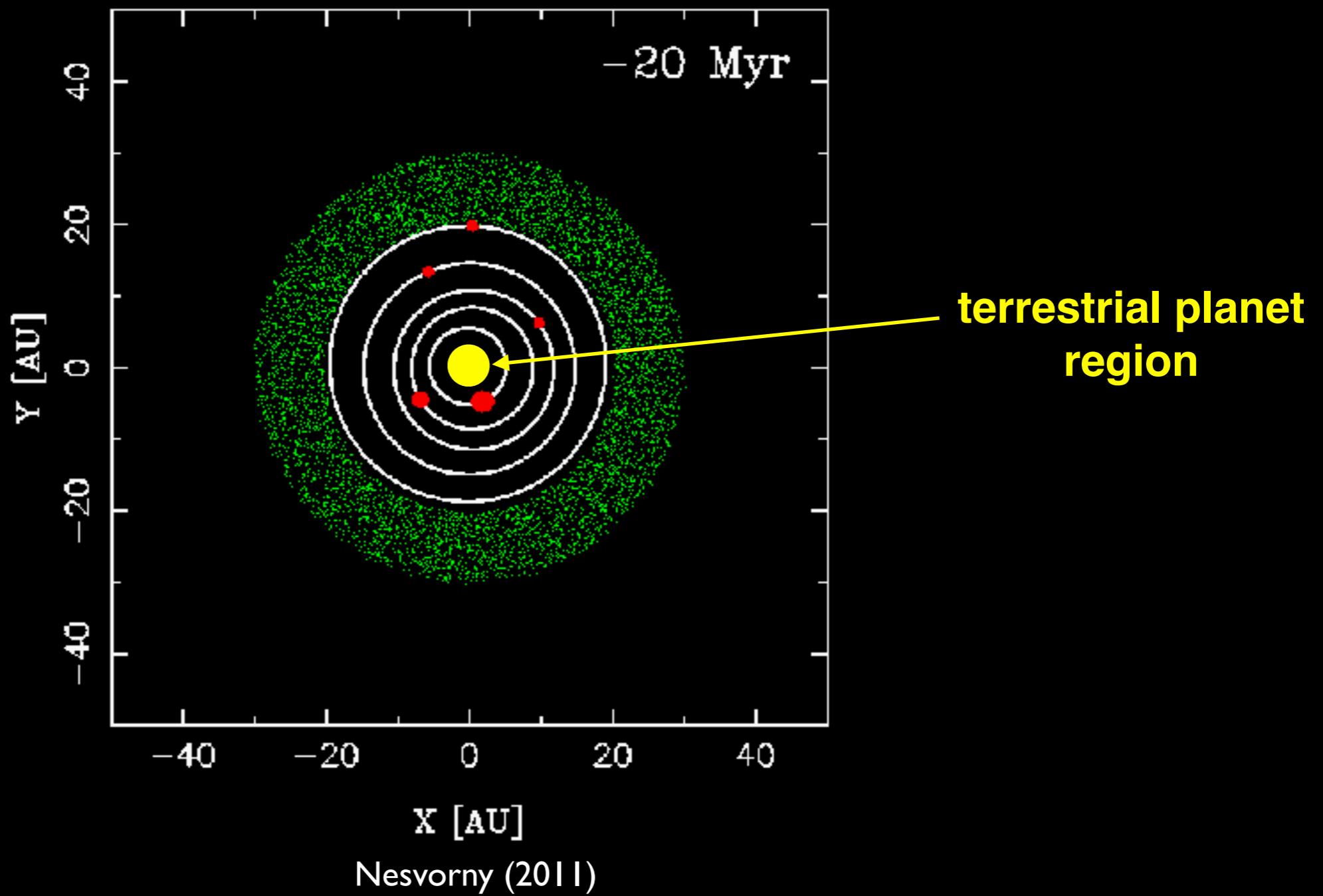
Can Jup and Sat really migrate outward? (maybe not)



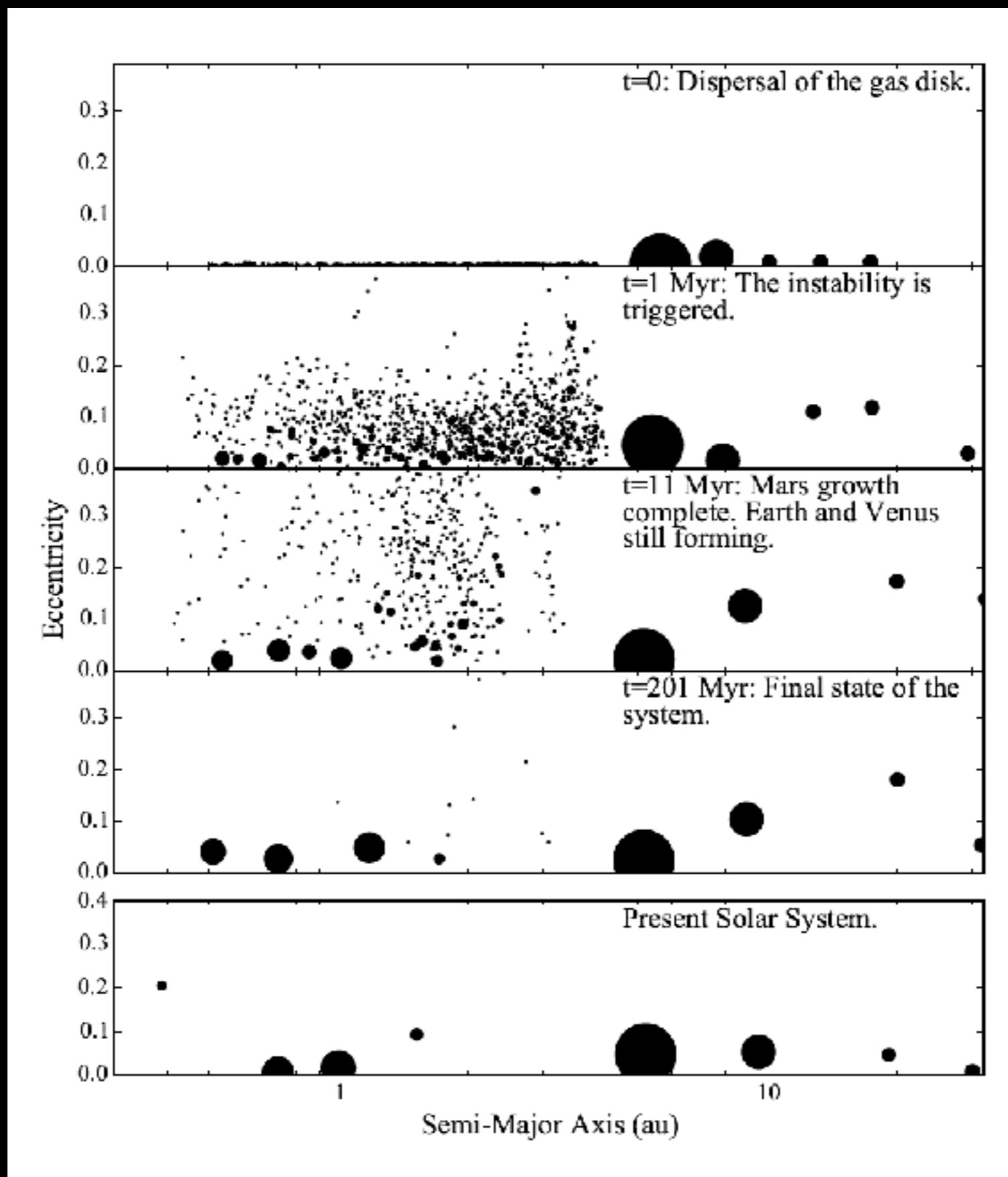
(assumption: very low-viscosity disk)

What if the giant planet instability happened early?

(true for instability triggers I and 2)

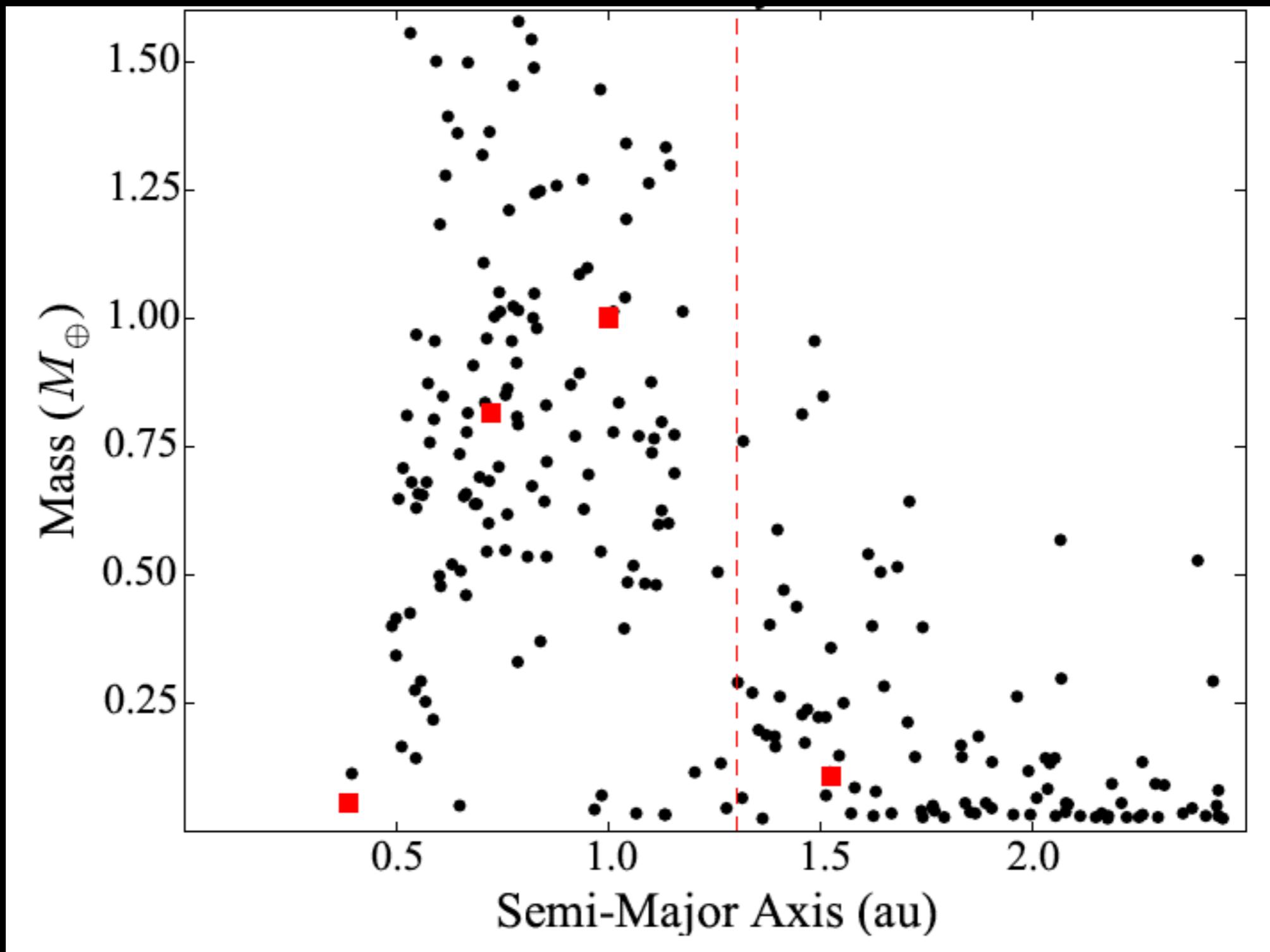


The Early Instability model



Clement et al
(2018, 2019, 2021)
(also Nesvorný et al
2021; Joiret et al 2023,
2024)

Early instability terrestrial planets



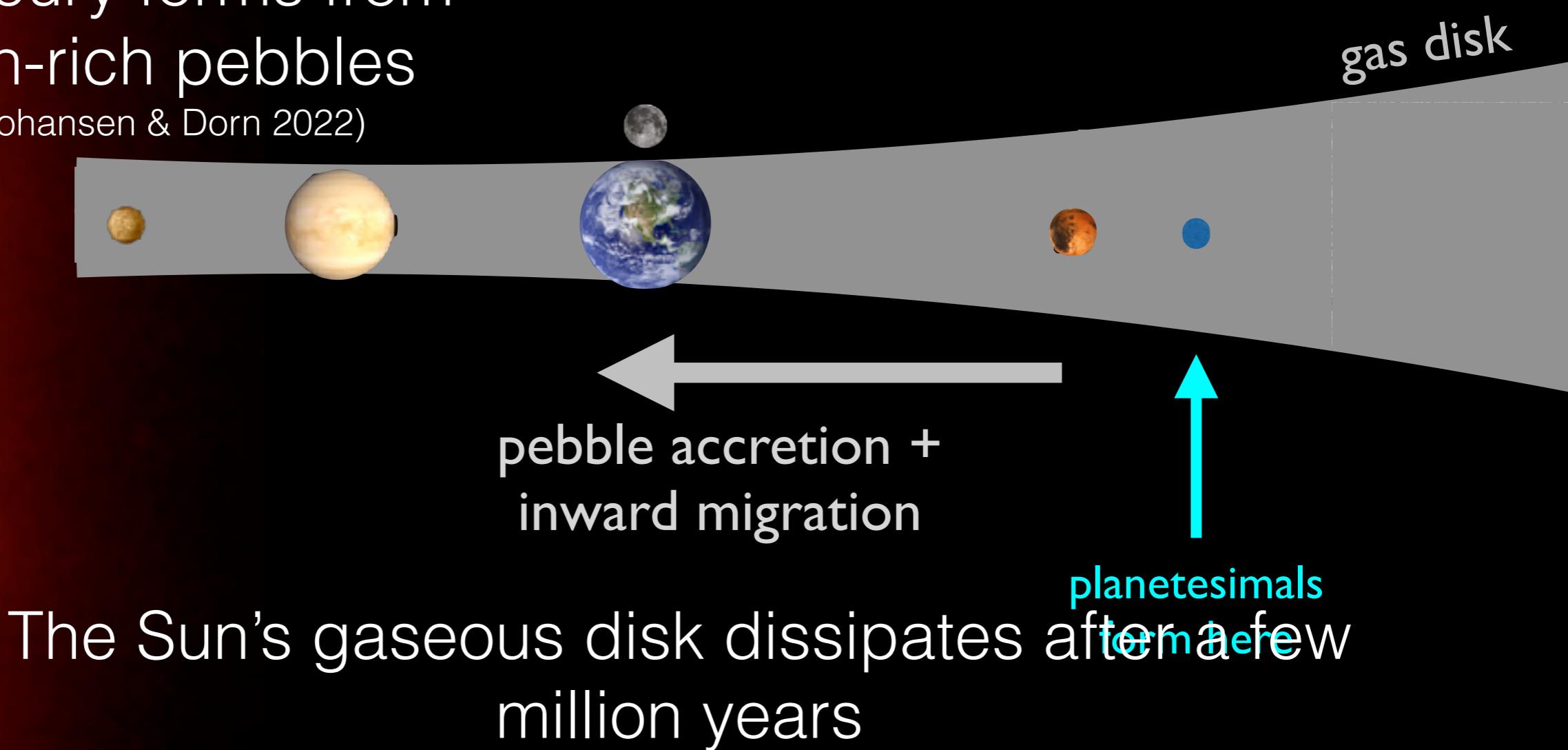
Clement et al (2018, 2019, 2021, 2023)

4. Pebble-accretion scenario

(Johansen et al 2021)

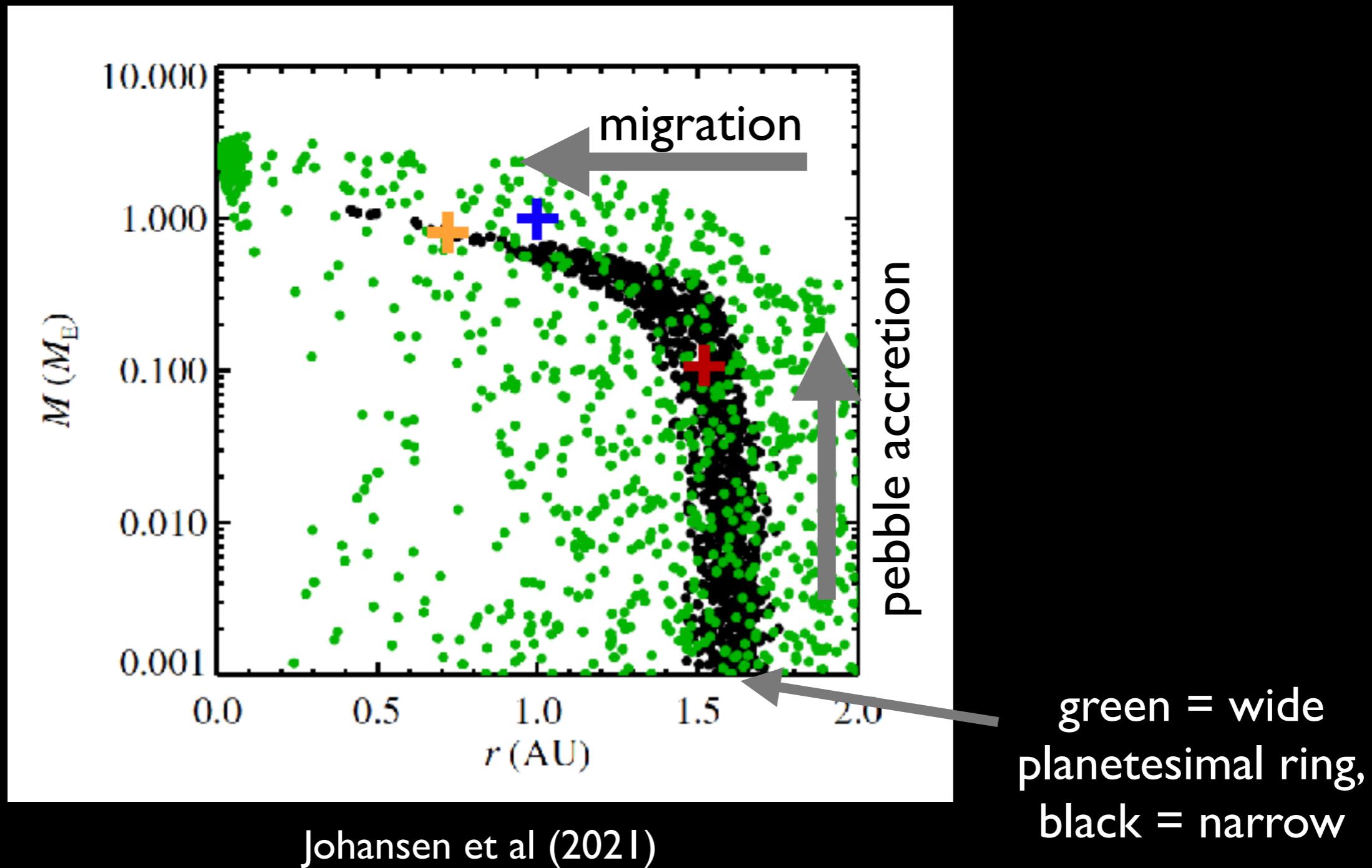
Assumption: large planetesimals only form in
Late giant impact preferred location
Mercury forms from
iron-rich pebbles

(Johansen & Dorn 2022)

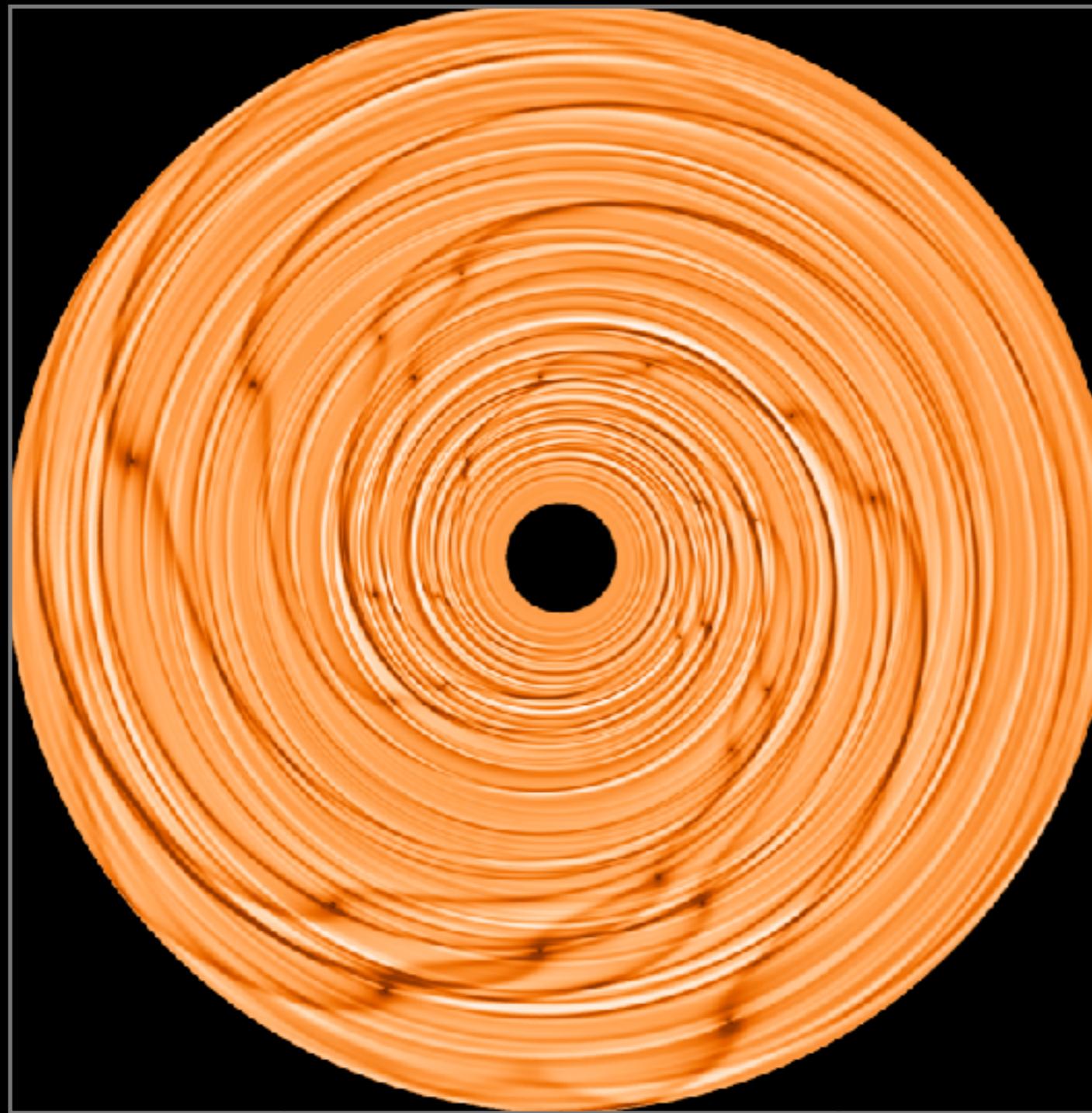


Pebble-accretion scenario

Key assumption: large planetesimals only form in preferred location

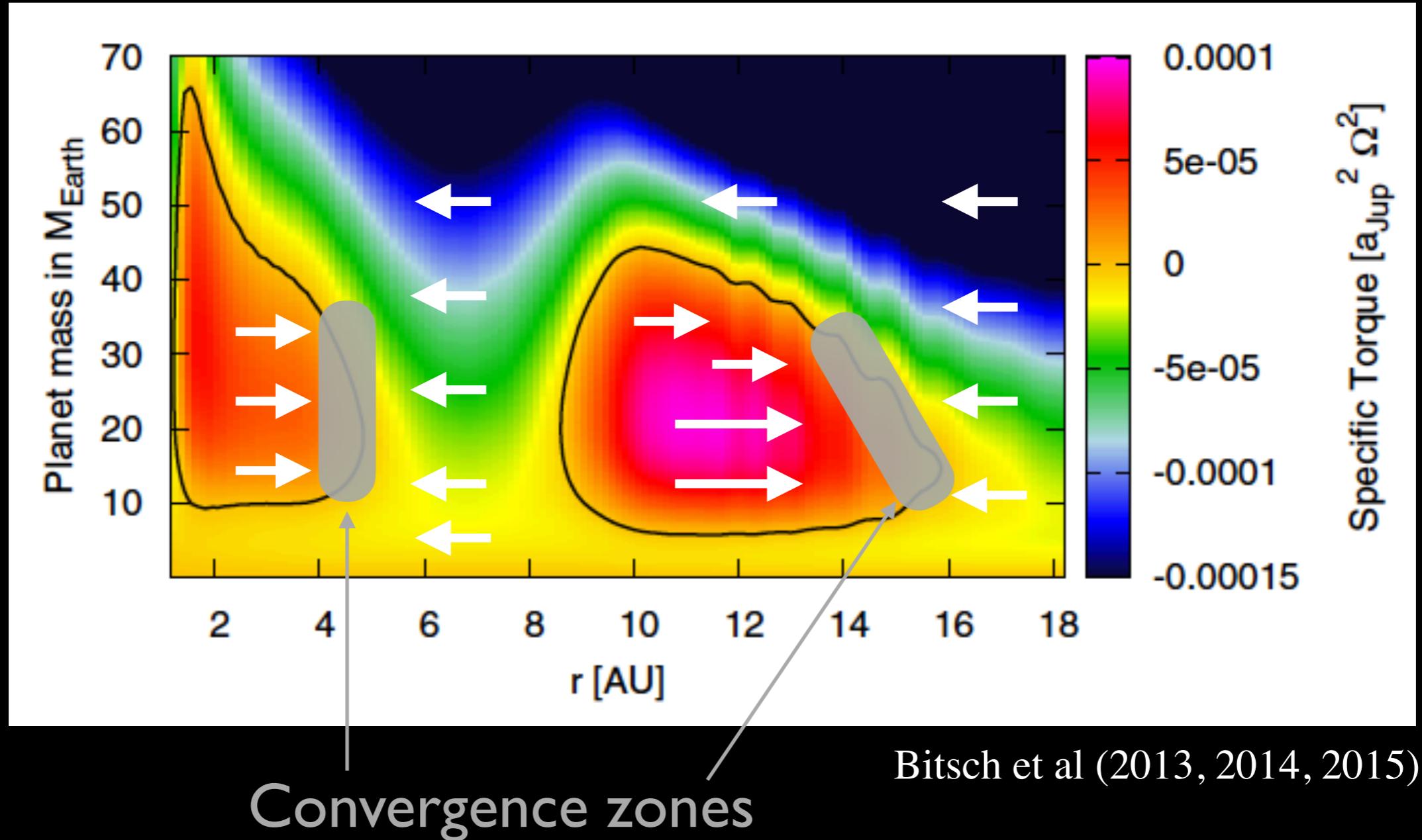


5. Convergent migration of planetary embryos

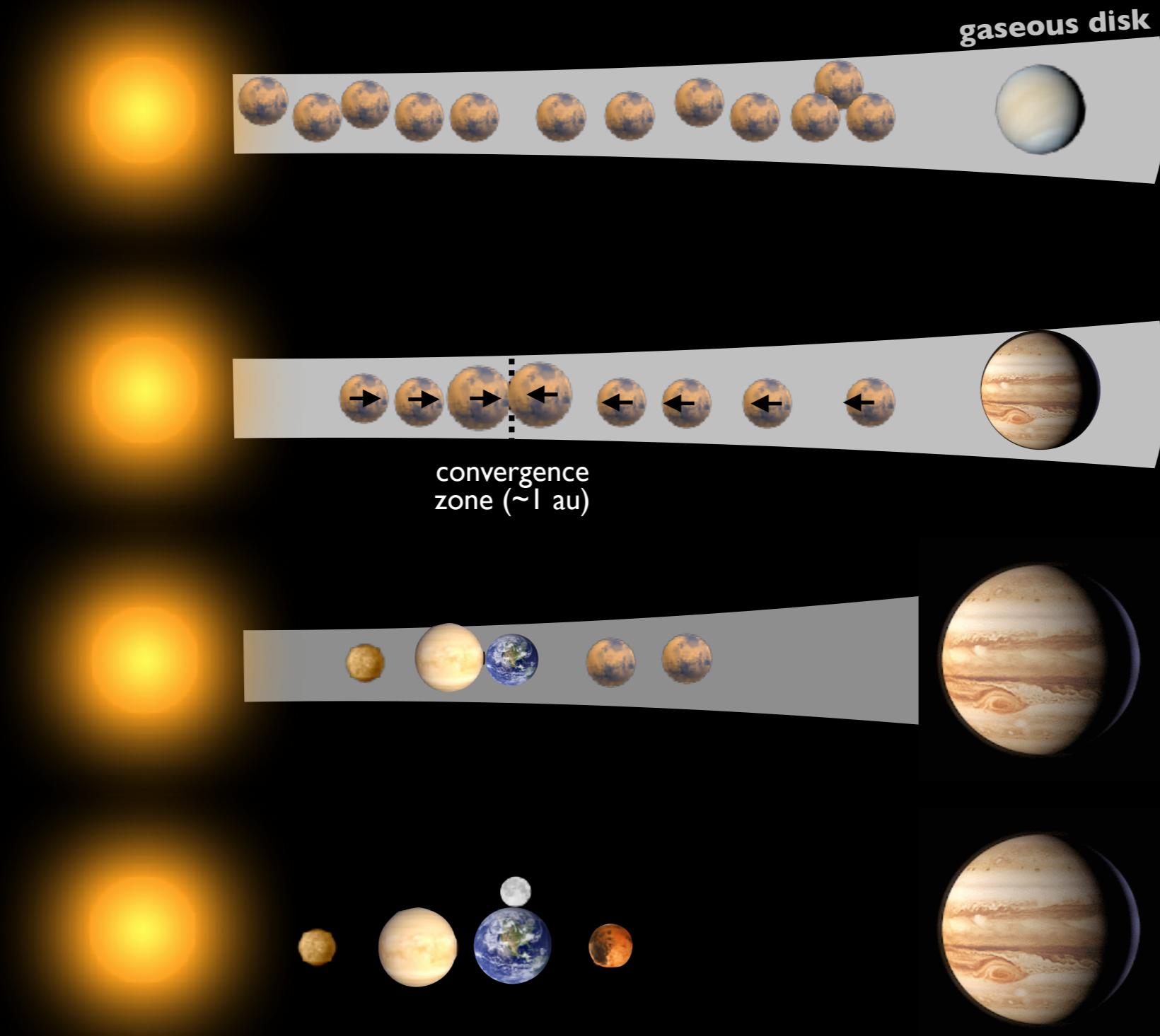


Broz et al (2021)

A migration “map” (for a specified disk model)

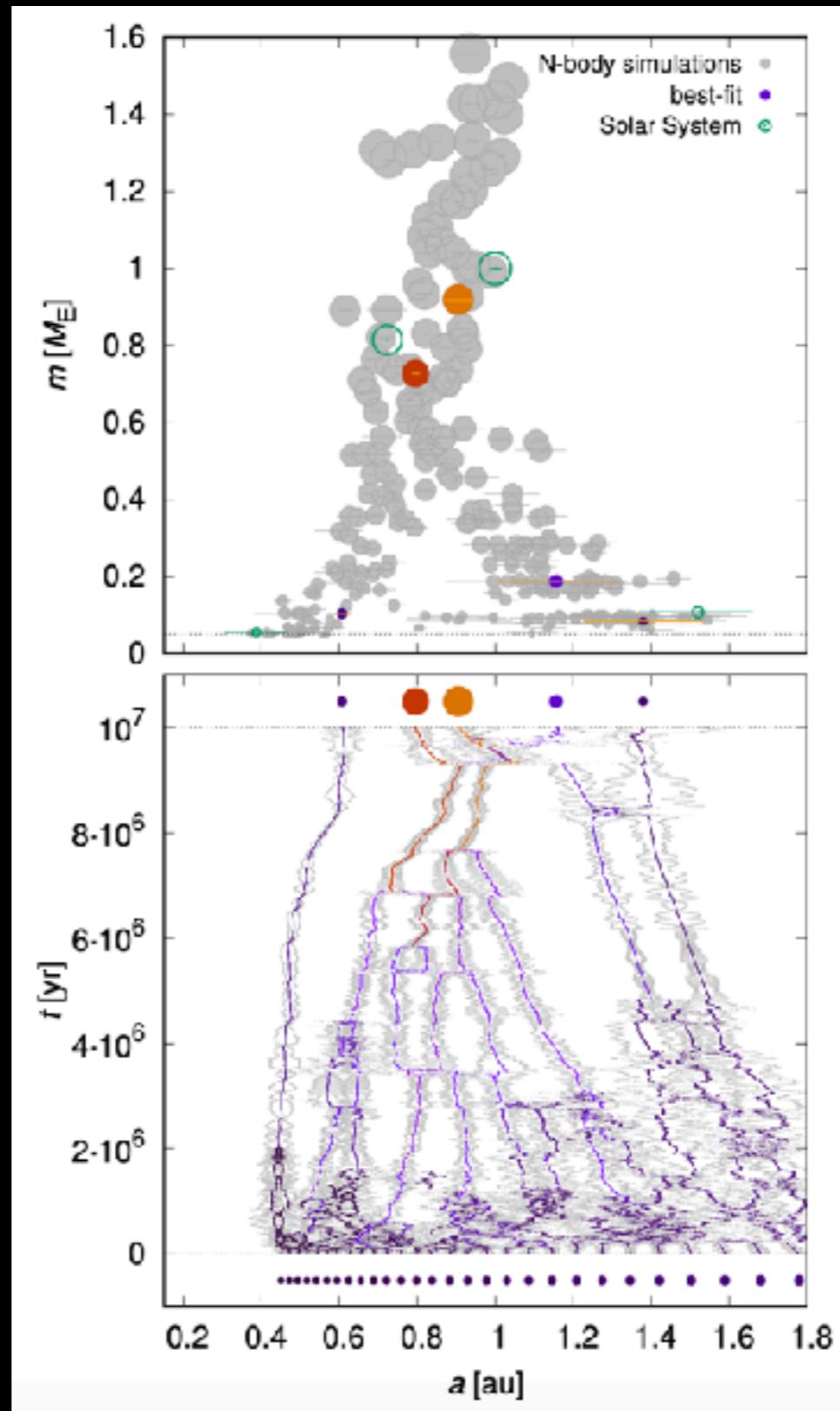


Convergent migration model



Broz et al (2021)
(image from news & views by Raymond 2021)

Convergent migration model



Possible solutions to the small Mars problem

Is a narrow annulus of planetesimals realistic?

“Empty asteroid belt”

How efficient is pebble accretion in terrestrial zone?

Pebble-driven

Are convergent migration zones common?

Convergent migration

Does outward migration work with gas accretion?

The “Grand Tack”

When did the instability really happen?

Early instability



Later dynamical sculpting

Additional resources

- *Planet Formation: key processes and global models*
Raymond & Morbidelli 2022 ([arxiv:2002.05756](https://arxiv.org/abs/2002.05756))
- The Solar System's Story (planetplanet.net)

